

### SPECIAL RELATIVITY HOMEWORK – WEEK 3

**Exercise 1.** *A neutron in isolation is unstable, with a half-life of several minutes. It eventually decays into a proton, an electron and an anti-neutrino – a process known as  $\beta$ -decay. You can look up the masses of the neutron, the proton and the electron. The mass of the anti-neutrino is negligible (and unknown; and ill-defined; long story). In the rest frame of the original neutron, what is the maximal energy of the outgoing anti-neutrino?*

In the lecture, I slightly messed up the definition of Mandelstam variables. Here, we'll introduce the correct one and play with it. For incoming 4-momenta  $p_1^\mu, p_2^\mu$  and outgoing 4-momenta  $p_1'^\mu, p_2'^\mu$ , the Mandelstam variables are defined as:

$$s = -(p_1 + p_2)^2 ; \quad t = -(p_1' - p_1)^2 ; \quad u = -(p_2' - p_1)^2 . \quad (1)$$

**Exercise 2.** *Understand why these are equivalent to:*

$$s = -(p_1' + p_2')^2 ; \quad t = -(p_2' - p_2)^2 ; \quad u = -(p_1' - p_2)^2 \quad (2)$$

*Then, express  $s + t + u$  in terms of the particles' masses  $m_1, m_2$ .*