

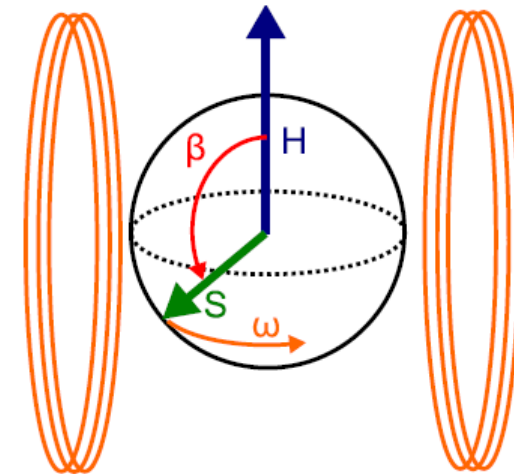
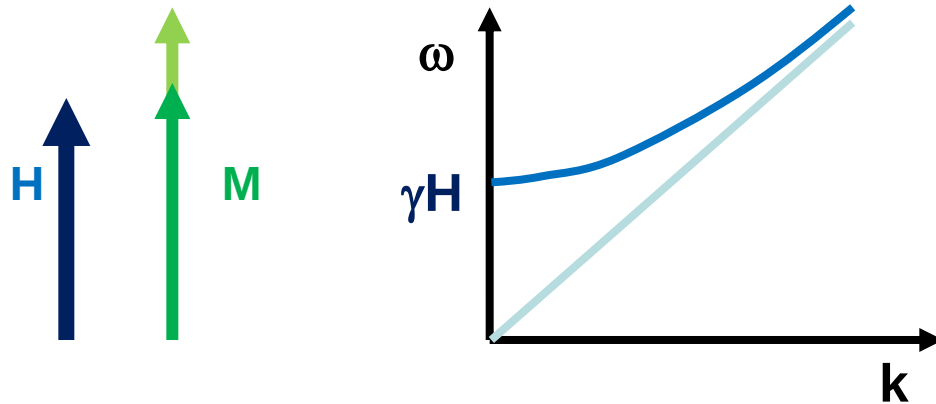
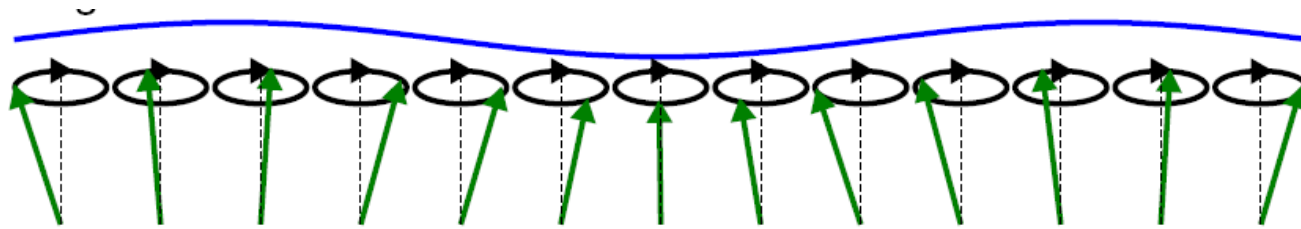
Spin superfluidity in antiferromagnets

Yu. M. Bunkov

Institute Neel, CNRS, Grenoble, France

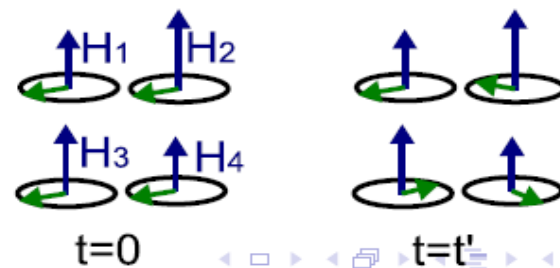
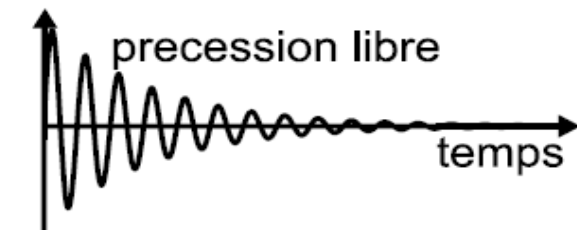


Spin waves

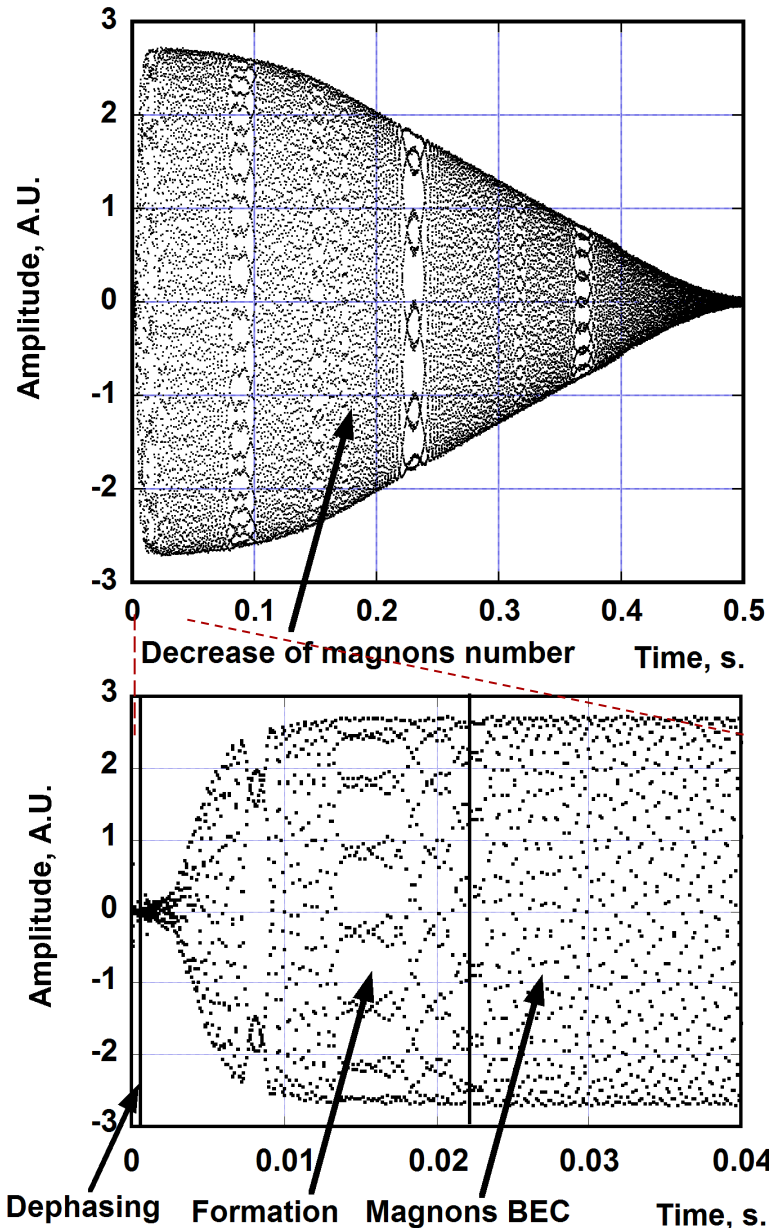


Holstein-Primakoff transformation

$$\begin{cases} \hat{S}_+ = \sqrt{2S\hbar} \hat{a}_0 \sqrt{1 - \frac{\hbar \hat{a}_0^\dagger \hat{a}_0}{2S}} \\ \hat{S}_- = \sqrt{2S\hbar} \sqrt{1 - \frac{\hbar \hat{a}_0^\dagger \hat{a}_0}{2S}} \hat{a}_0^\dagger \\ \hat{S}_z = S - \hbar \hat{a}_0^\dagger \hat{a}_0 = S - \hbar \hat{N}_0 \end{cases}$$

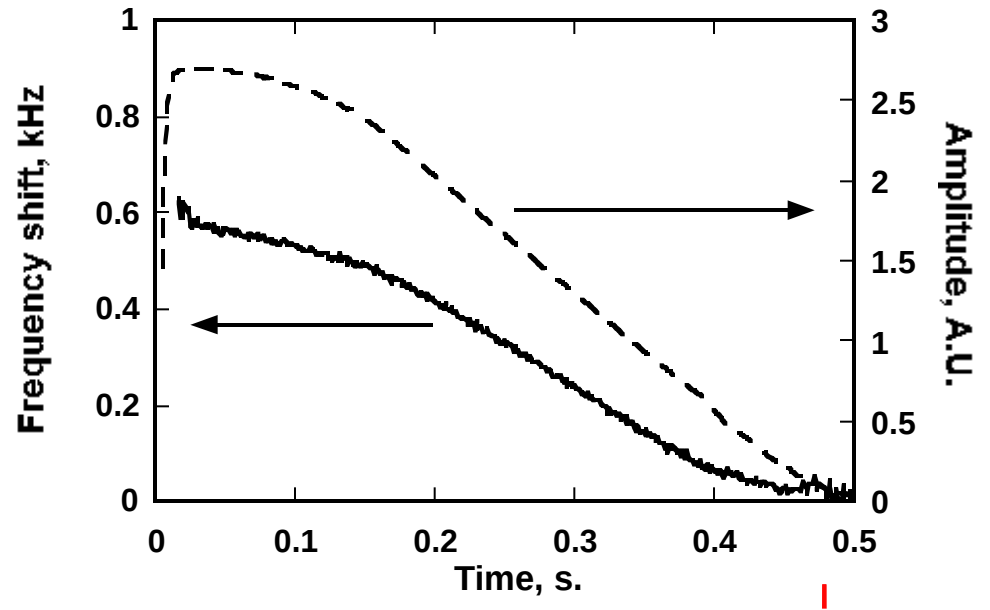


Grenoble, 2003



A

Signal in the time domain

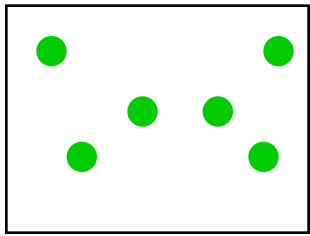


The main landmark of BEC is the changing of frequency at relaxation. The magnon density decay changes the chemical potential!

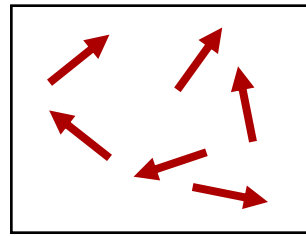
The first observation:

A.S.Borovik-Romanov, Yu.M.Bunkov, V.V.Dmitriev, Yu.M.Mukharskiy, JETP Letters v.40, p.1033, (1984).

I.A.Fomin, JETP Letters v.40, p.1036, (1984).

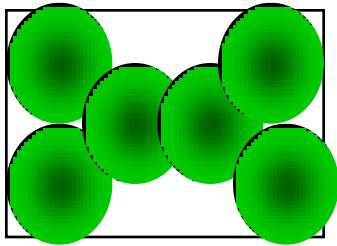


Ideal gas

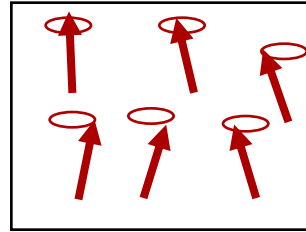


$$\omega = \gamma H_{\text{loc}}$$

Paramagnetic, Fermi liquid

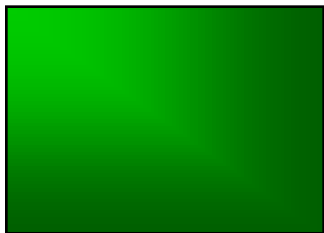


Quantum gas

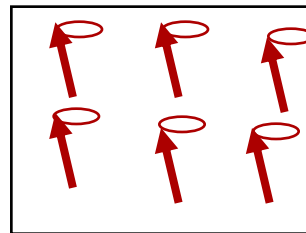


$$i\hbar \frac{\partial}{\partial t} \psi = -\frac{\hbar^2}{2m} \nabla^2 \psi + V\psi$$

Magnetically ordered



BEC, superfluidity



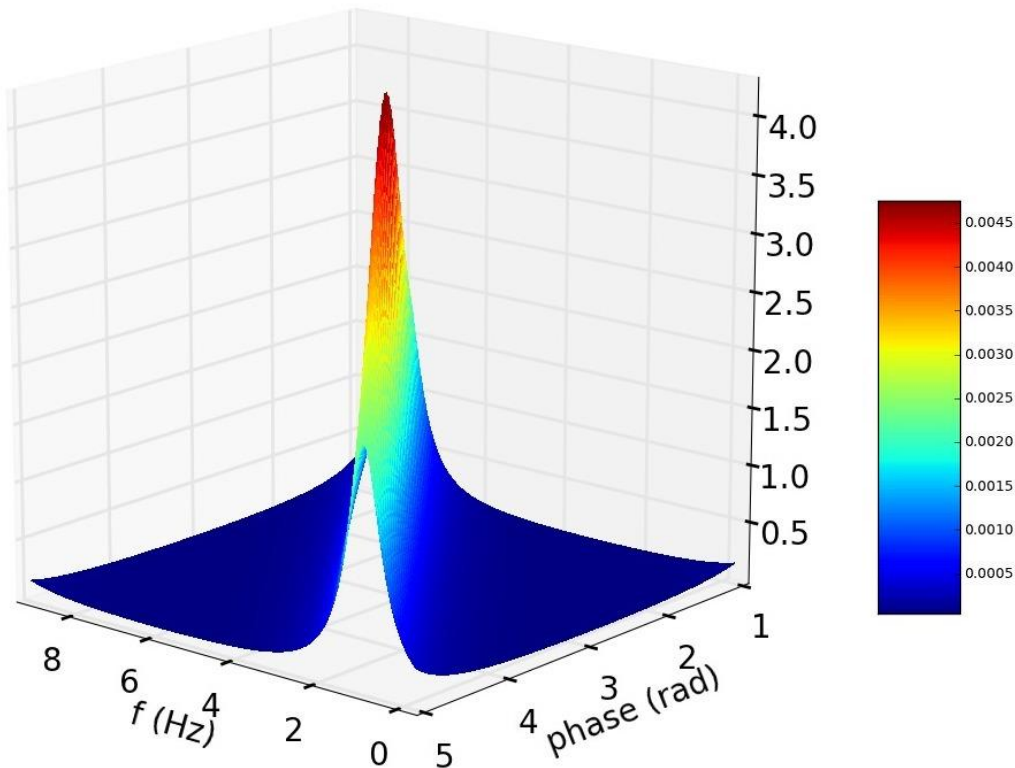
$$\omega = \omega_0$$

$$S_x + iS_y = S \sin \beta e^{i\omega t + i\alpha}$$

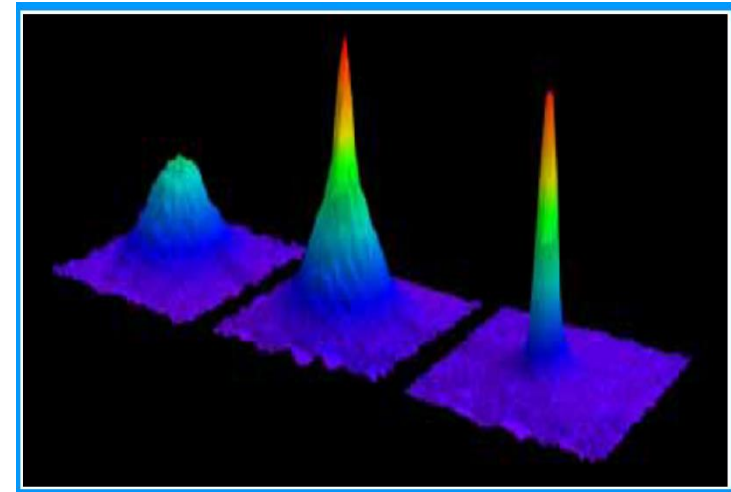
Coherent precession

Spin superfluidity and BEC of magnons was found in a 5 different states of superfluid ^3He . In one of this states the induction signal can live more than one hour. It corresponds to a 99.999% of magnons to be condensed! For an atomic BEC the 30% condensation was only achieved!

$$S_x + iS_y = S \sin \beta e^{i\omega t + i\alpha}$$

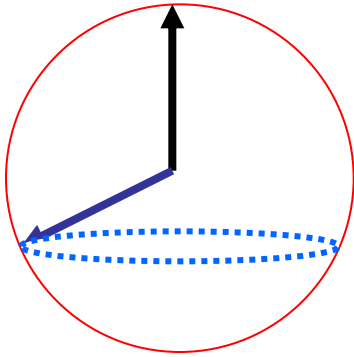


Magnon BEC



Atomic BEC

Spin waves in superfluid ^3He are ready to be condensed!



$$N_M = \int d^3r |\Psi|^2 = \int d^3r \frac{S - S_z}{\hbar}$$

$$\Psi = \sqrt{2S/\hbar} \sin \frac{\beta}{2} e^{i\omega t + i\alpha},$$

$$\omega(k) = \omega_L - \omega + \frac{c^2 k^2}{\omega_L} \equiv \omega_L - \omega + \frac{k^2}{2m_M}$$

Magnon spectrum

Magnon mass

$$m_M \sim \frac{\omega_L}{v_F^2} \sim m_3 \frac{\omega_L}{E_F} \quad (\hbar = 1; \quad c \sim v_F)$$

Magnon density

$$n_M \sim S \sim \chi H / \gamma \sim \omega_L N_F \sim n_3 \omega_L / E_F$$

where $N_F \sim m_3 p_F$ is the density of states and $n_3 \sim p_F^3$ is the density of atoms.

Temperature of BEC

$$T_{\text{BEC}} \sim \left(\frac{n c^3}{\omega_L} \right)^{1/2} \sim E_F$$

$$T_F = 0.1\text{K}, \quad T_{\text{exp}} = 0.0003\text{K}$$

G.Volovik

Gross-Pitaevskii equation

I.A. Fomin, Physica B 169, 153 (1991).

$$\frac{\delta F}{\delta \Psi^*} = 0$$

$$F = \int d^3r \left(\frac{|\nabla \Psi|^2}{2m_M} + (\omega_L(z) - \omega)|\Psi|^2 + F_D \right)$$

Dipole-dipole spin-orbit energy

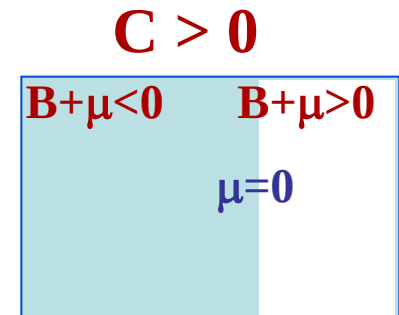
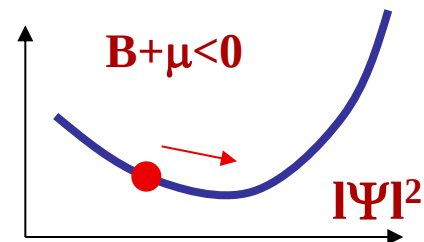
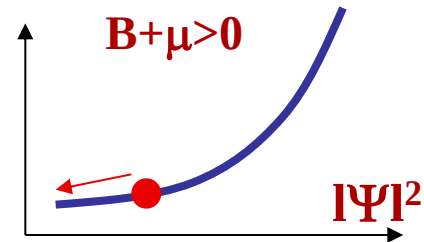
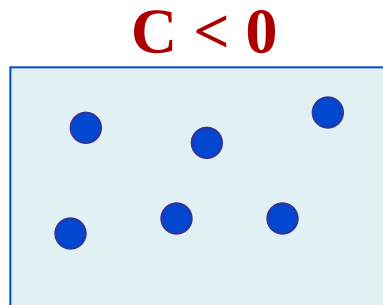
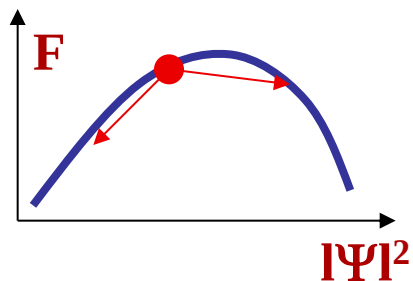
Gradient energy

Spectroscopic energy

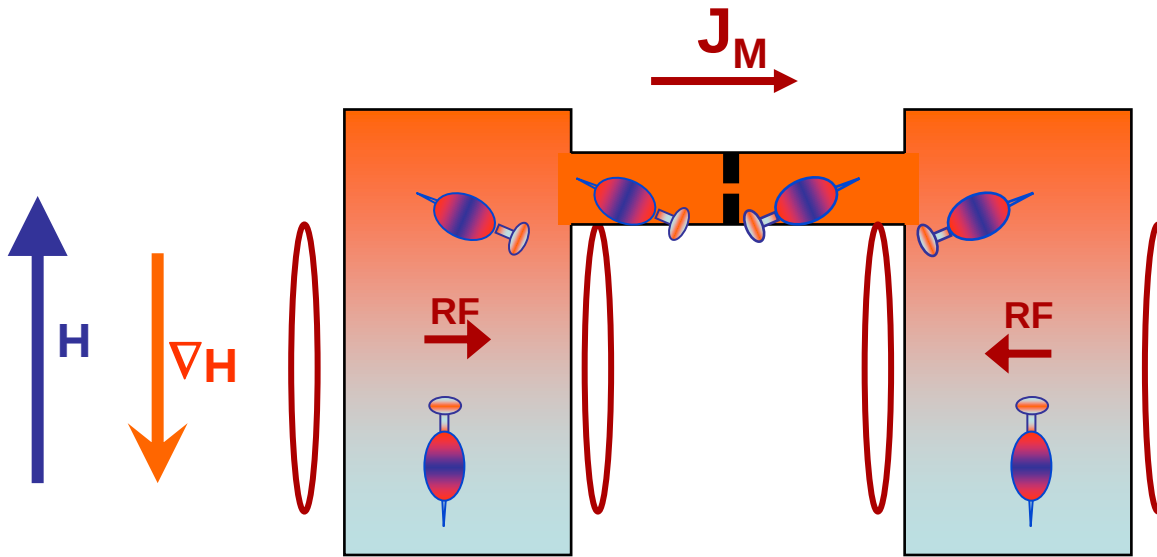
Spin Supercurrent

True energy at the rotating frame
Chemical potential $\mu = \omega_L(z) - \omega$

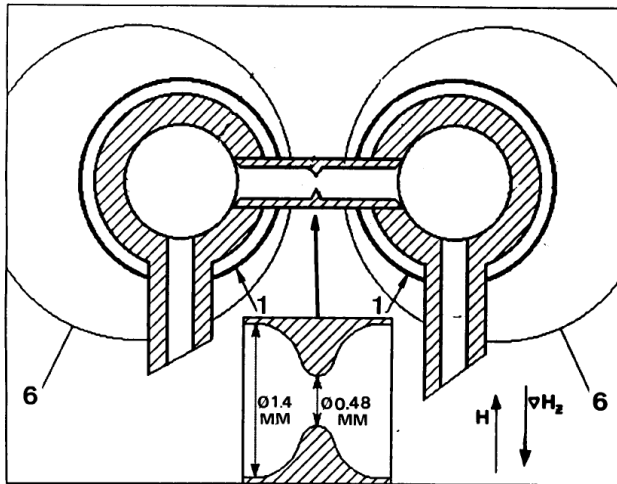
$$F = A + (B + \mu) |\Psi|^2 + C |\Psi|^4$$



Josephson effect

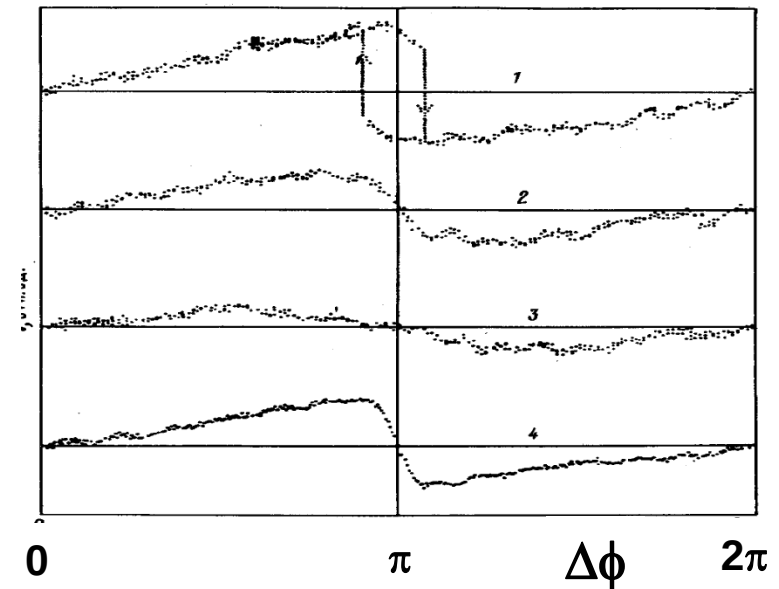


$$\xi = 1.088 c_{\parallel} / \sqrt{\omega(\omega - \gamma H)}$$



JETPh Letters, v.47, p.478, (1988).

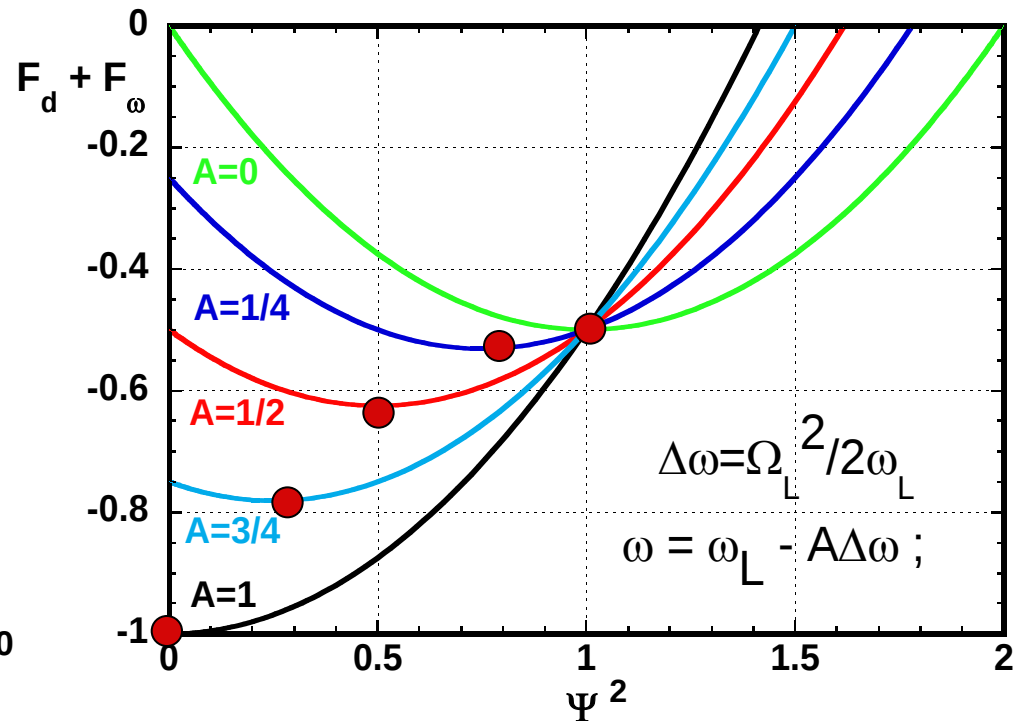
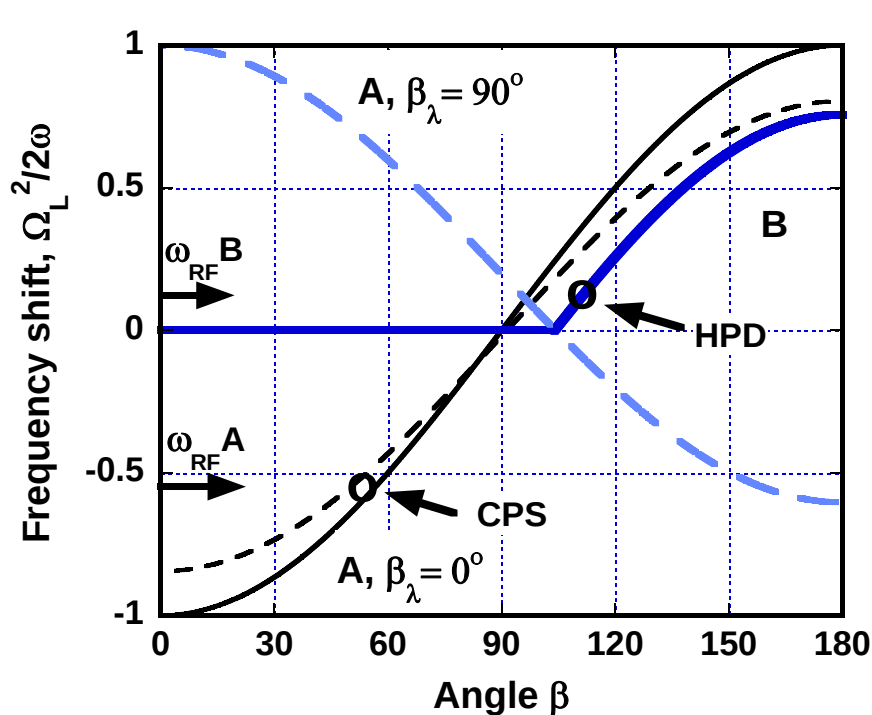
QFS Florida 1989, AIP Conf. Proc., v.194, p.27.



Superfluid $^3\text{He-A}$ in squeezed aerogel

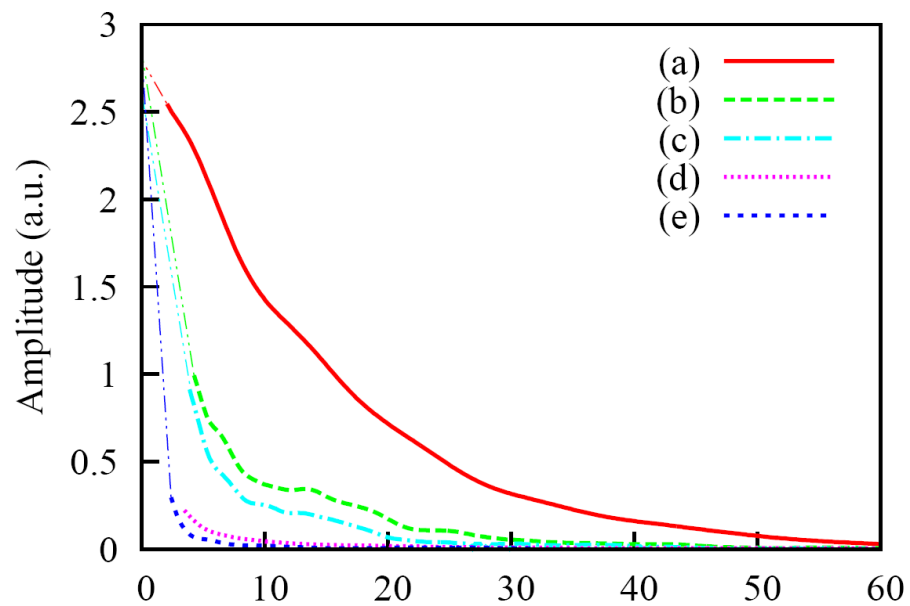
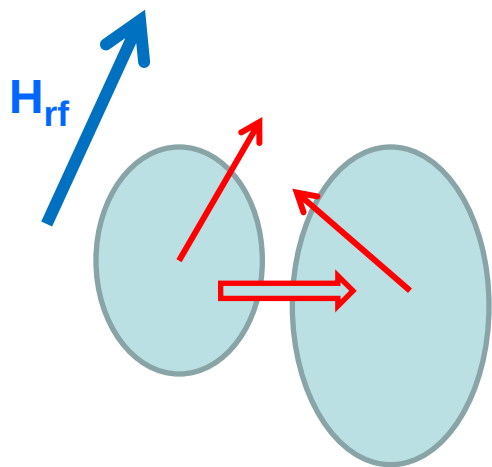
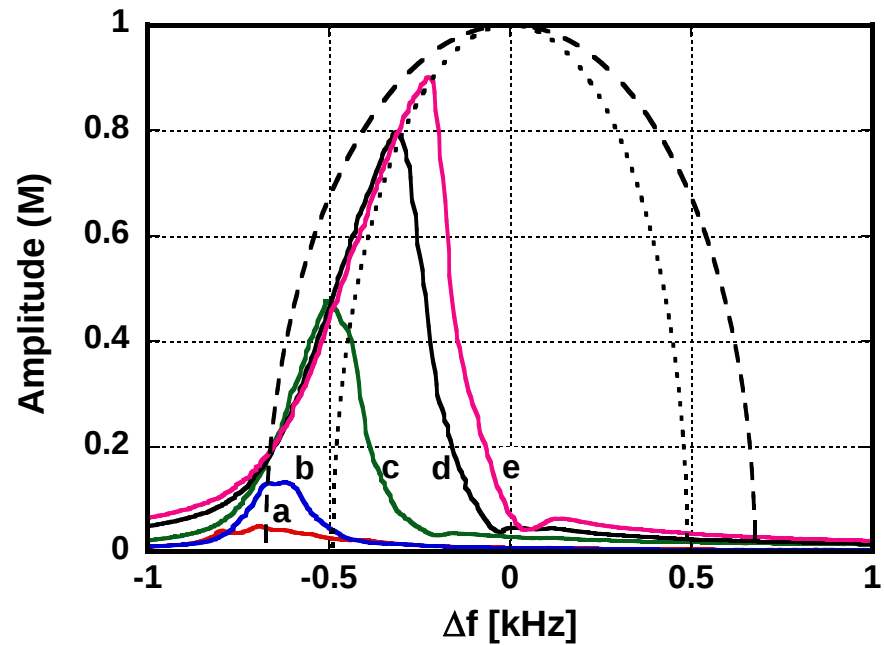
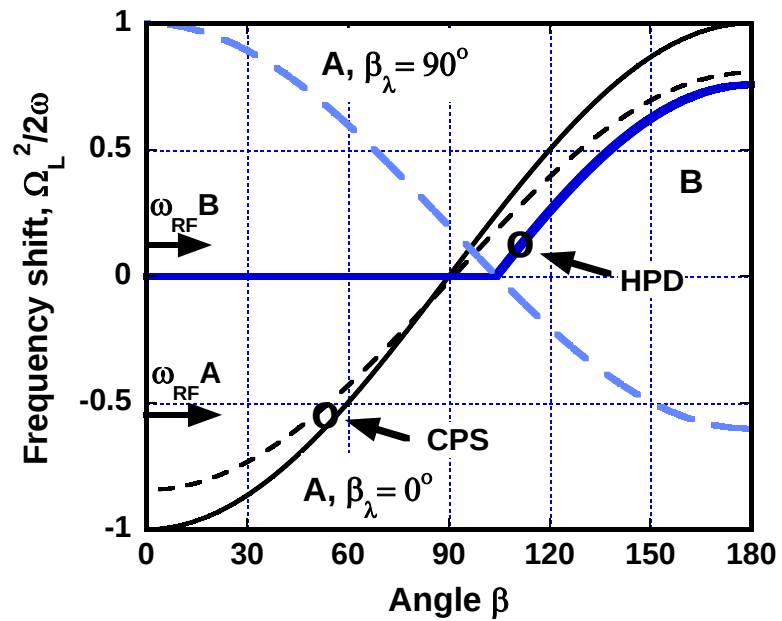
$$F = \int d^3r \left(\frac{|\nabla \Psi|^2}{2m_M} + (\omega_L(z) - \omega)|\Psi|^2 + F_D \right)$$

$$F_D = \frac{\chi \Omega_L^2}{4} \left[-2 \frac{|\Psi|^2}{S} + \frac{|\Psi|^4}{S^2} + \left(-2 + 4 \frac{|\Psi|^2}{S} - \frac{7}{4} \frac{|\Psi|^4}{S^2} \right) \sin^2 \beta_L \right]$$

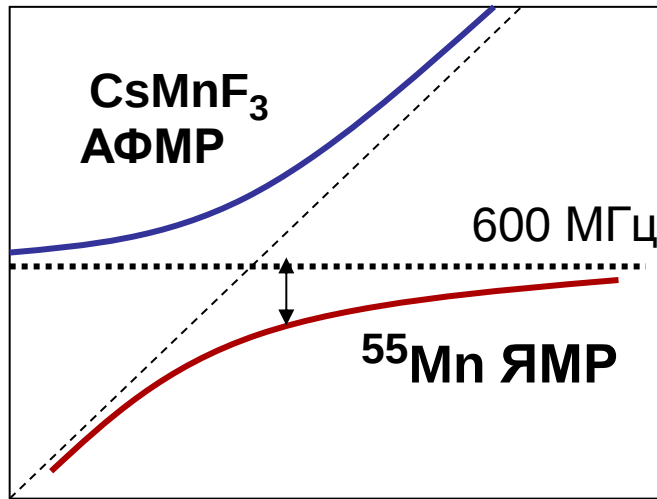


T. Kunimatsu, T. Sato, K. Izumina, A. Matsubara, Y. Sasaki, M. Kubota, O. Ishikawa,
T. Mizusaki, Yu.M. Bunkov Pisma v ZhETP, 86, 244 (2007)

T. Sato, T. Kunimatsu, K. Izumina, A. Matsubara, M. Kubota, T. Mizusaki, and Yu.M. Bunkov
Phys. Rev. Lett. 101, 055301 (2008)

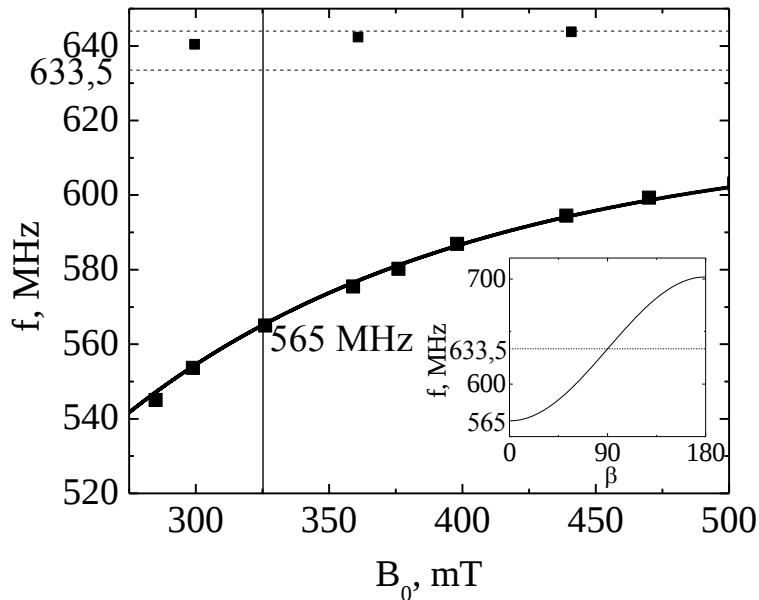


CsMnF₃



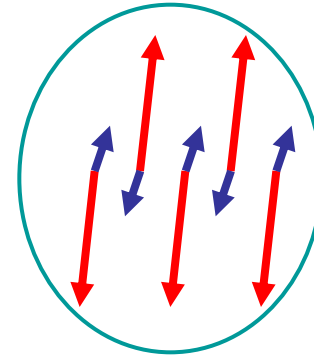
a

H



BEC in antiferromagnet with Pulling

Coupled Nuclear electron precession



Yu.M. Bunkov, E.M. Alakshin, R.R. Gazizulin, A.V. Klochkov,
V.V. Kuzmin, T.R. Safin, M.S. Tagirov.

« Discovery of the Classical Bose–Einstein Condensation
of Magnons in Solid Antiferromagnets »

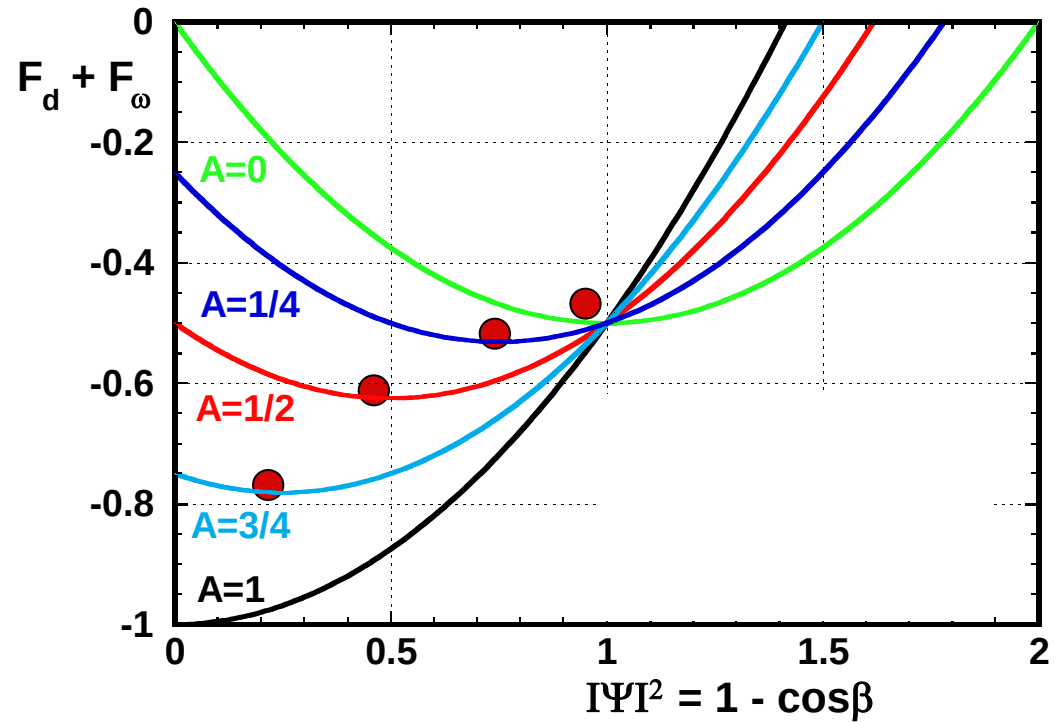
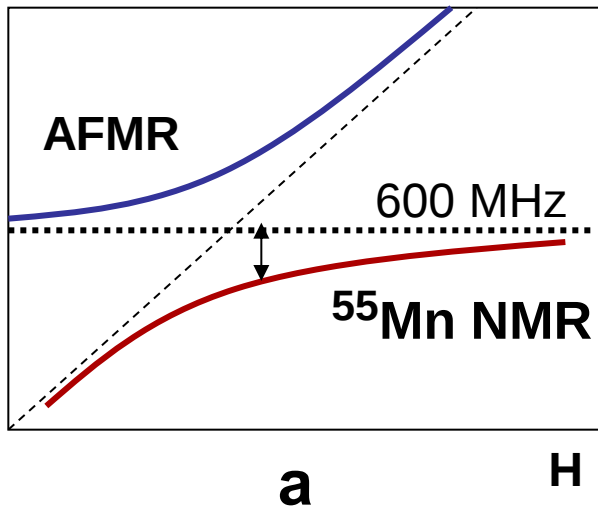
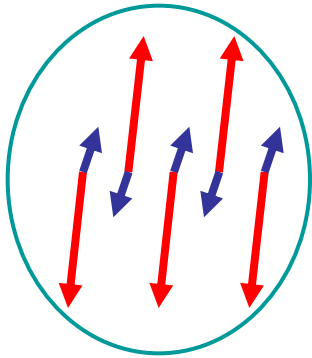
JETP Letters, **94**, 68–72 (2011)

“High T_c spin superfluidity in antiferromagnets”

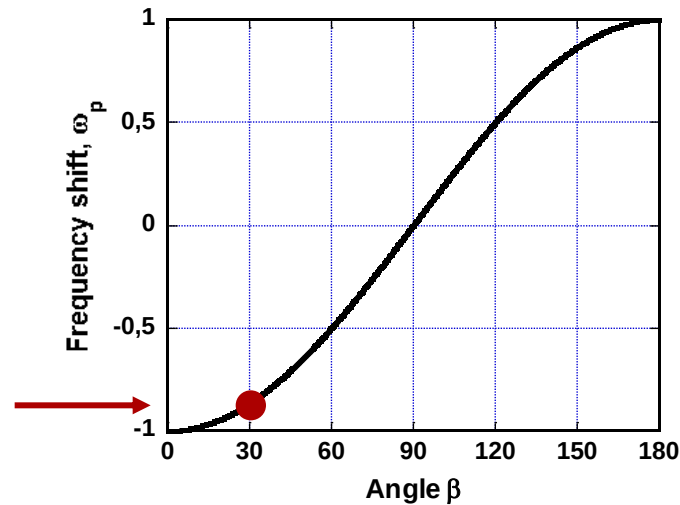
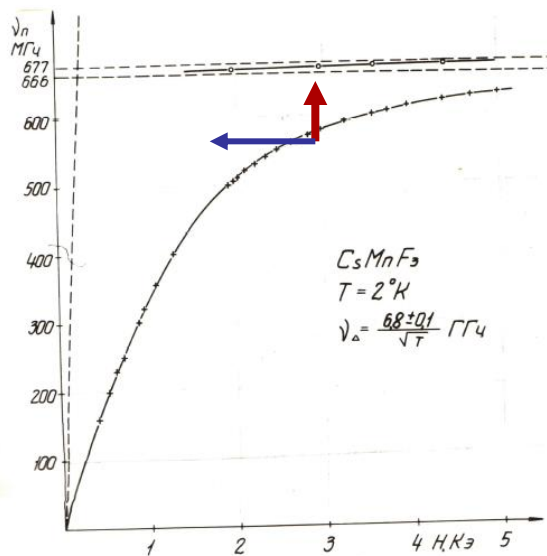
Yu. M. Bunkov, E.M. Alakshin, R.R. Gazizulin,
A.V. Klochkov, V.V. Kuzmin, V.S. L'vov, and M.S. Tagirov
PRL, Avril 2012.

Suhl – Nacamura interaction

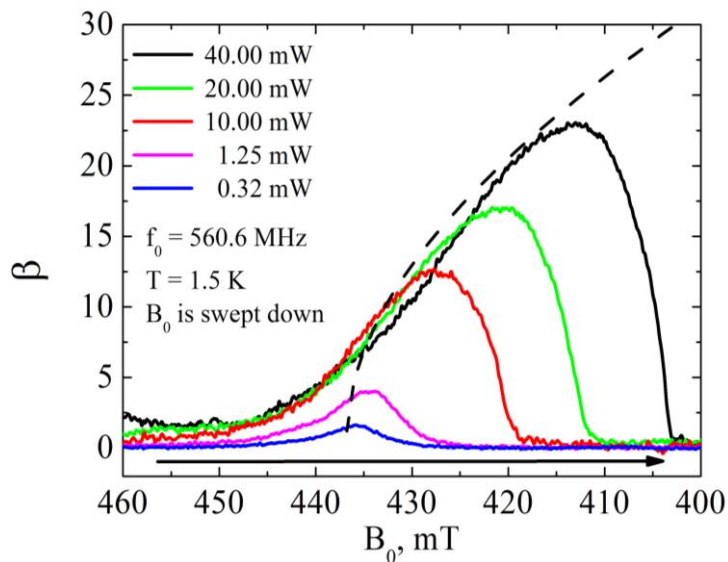
$$F = \int d^3r \left(\frac{|\nabla \Psi|^2}{2m_M} + (\omega_L(z) - \omega)|\Psi|^2 + F_{\text{SN}} \right)$$



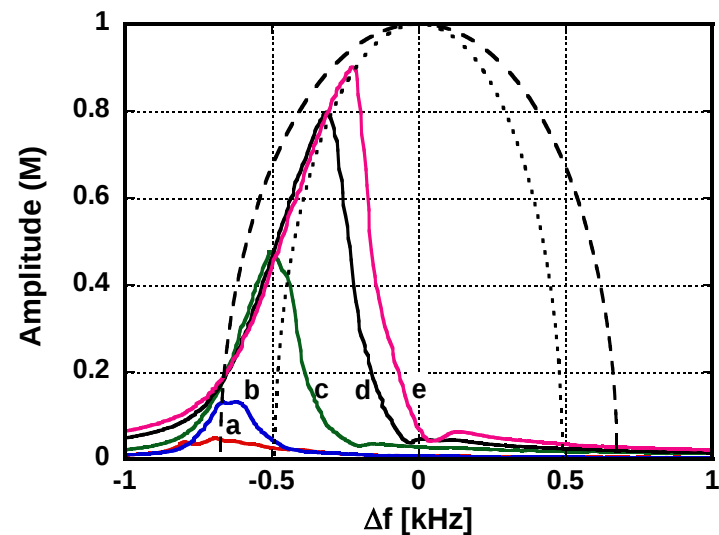
CW NMR experiments



Broadening was about 2 MHz and RF field was only about 300 kHz

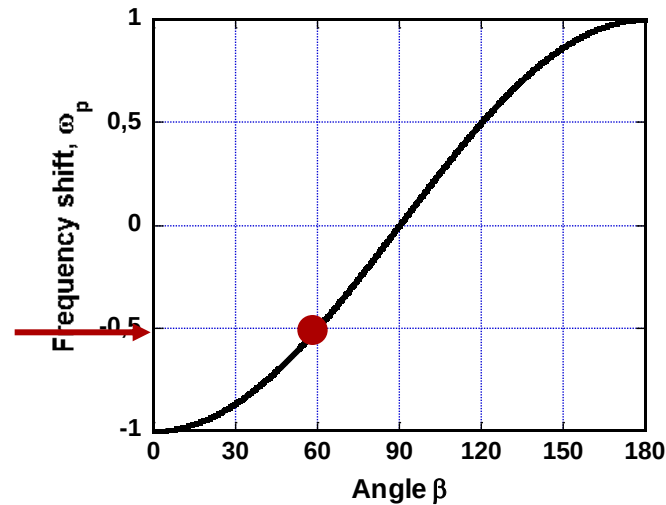
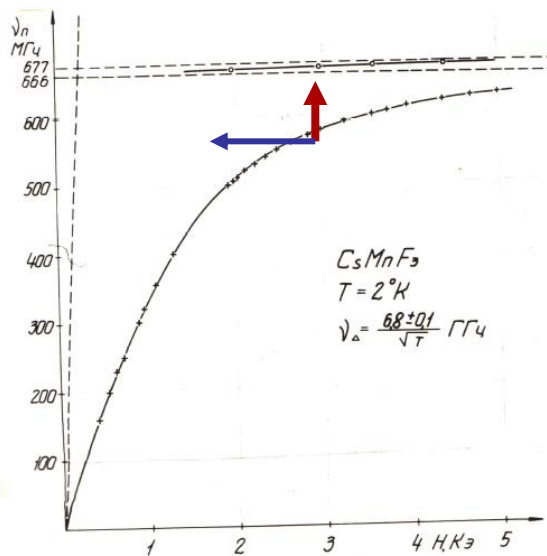


$CsMnF_3$

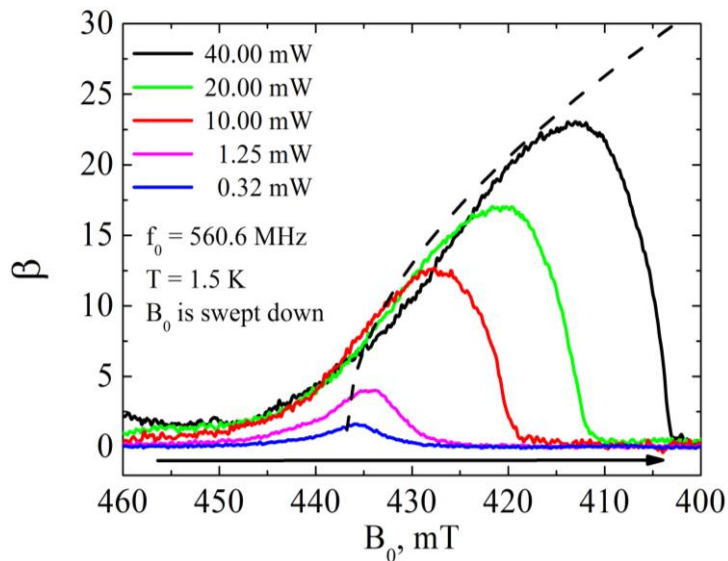


$^3\text{He-A}$ in aerogel

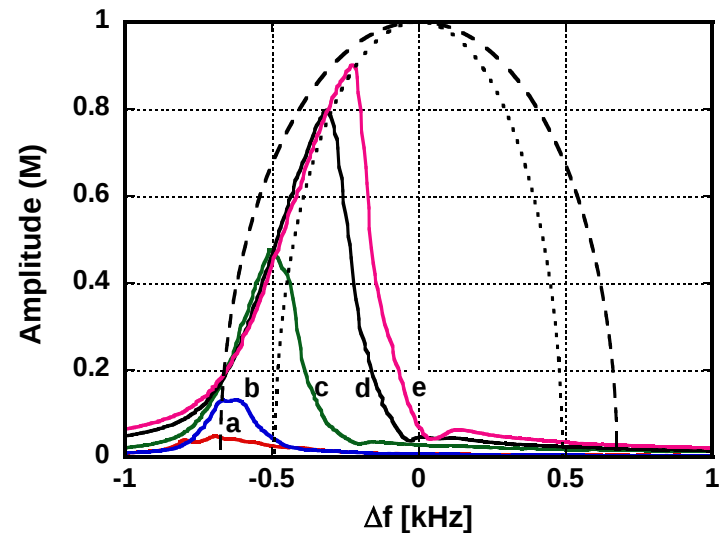
CW NMR experiments



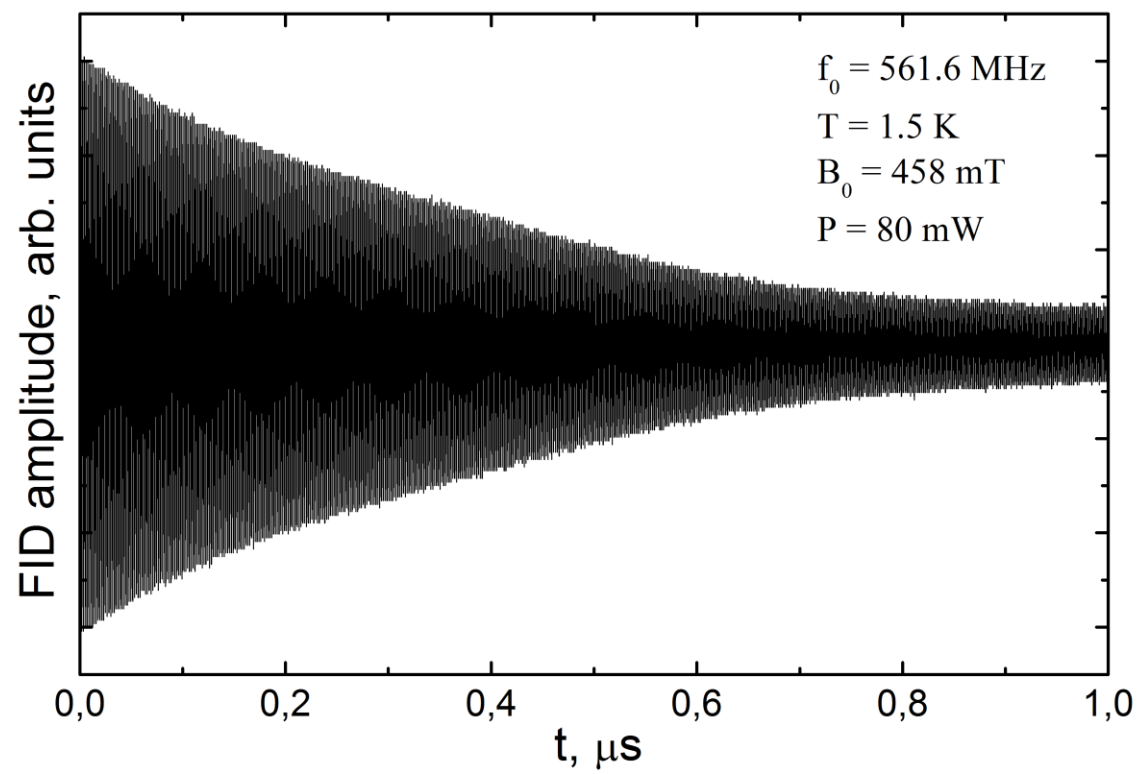
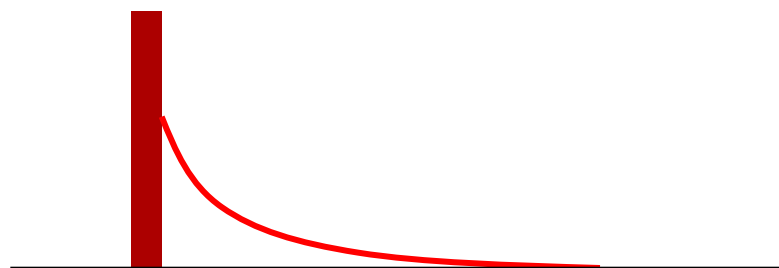
Broadening was about 2 MHz and RF field was only about 300 kHz

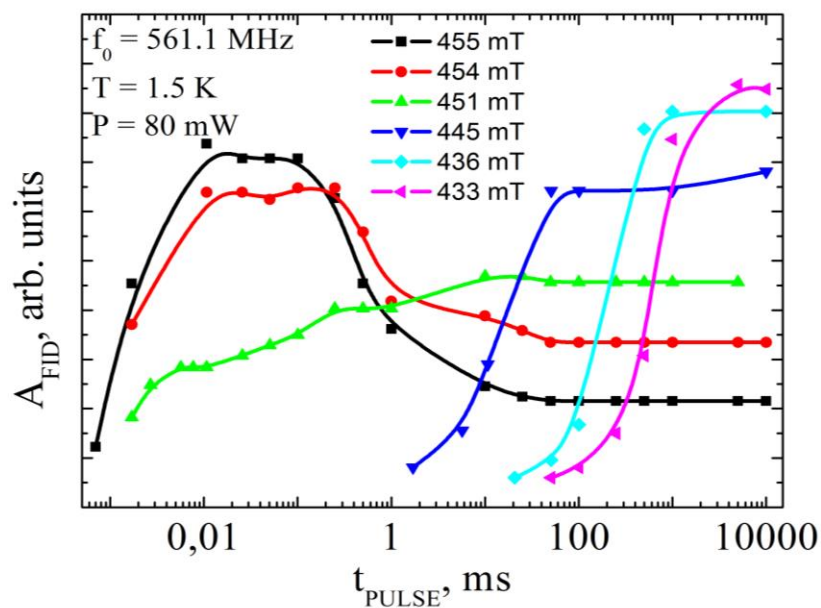
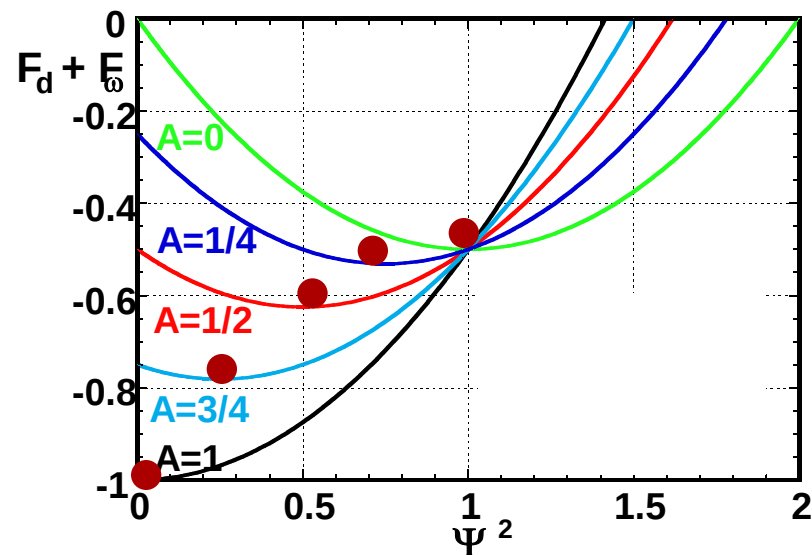
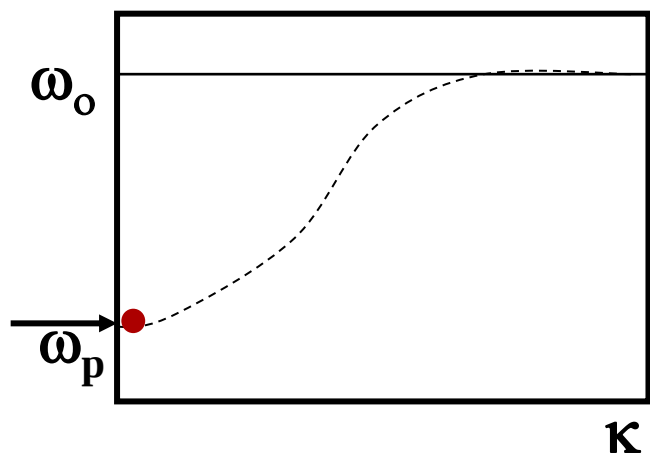


$CsMnF_3$

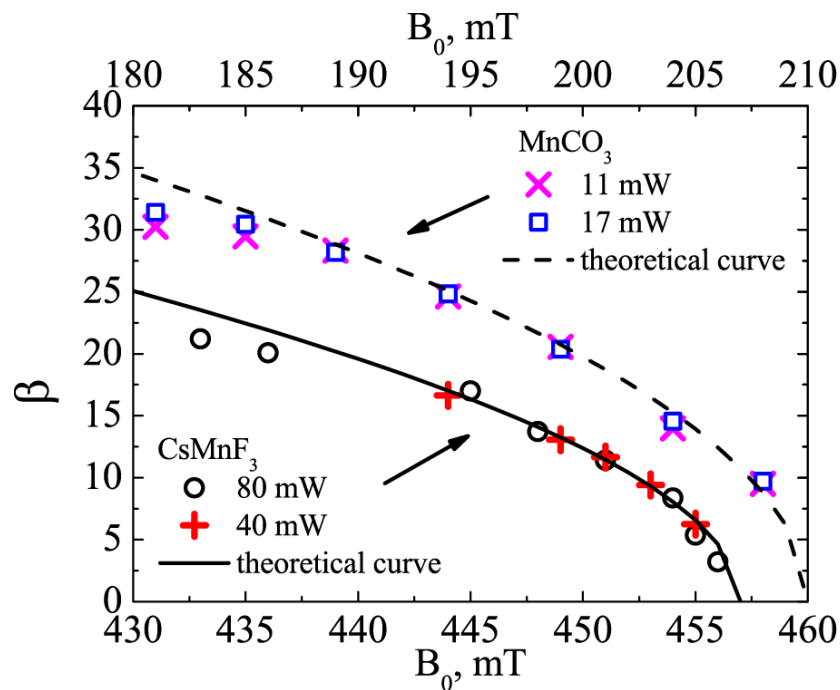


$^3\text{He-A}$ in aerogel

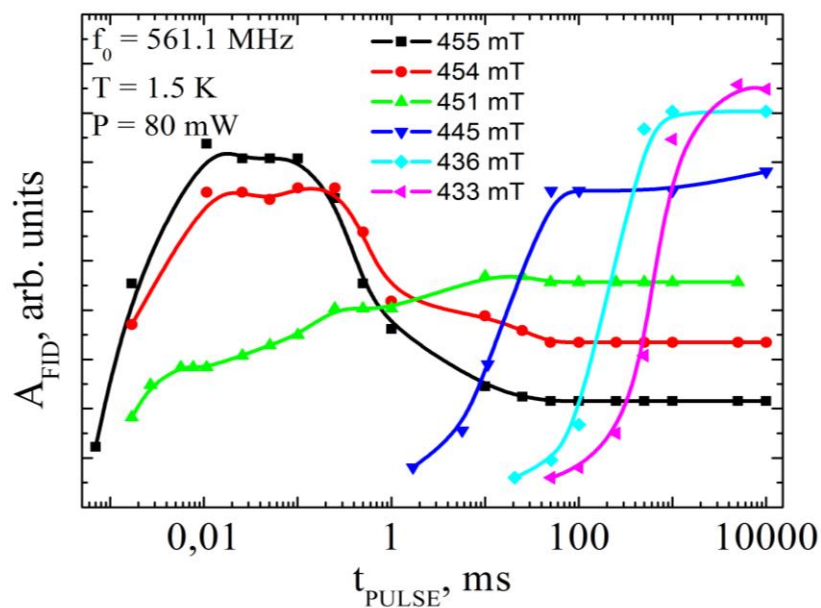
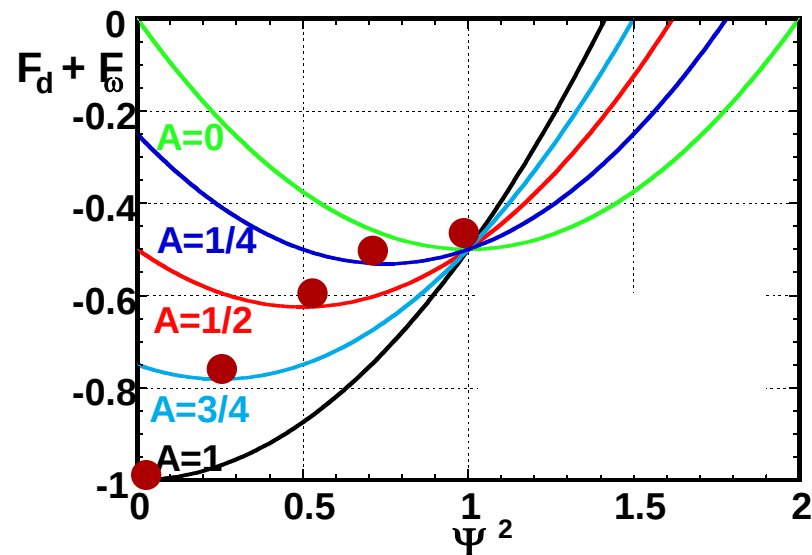
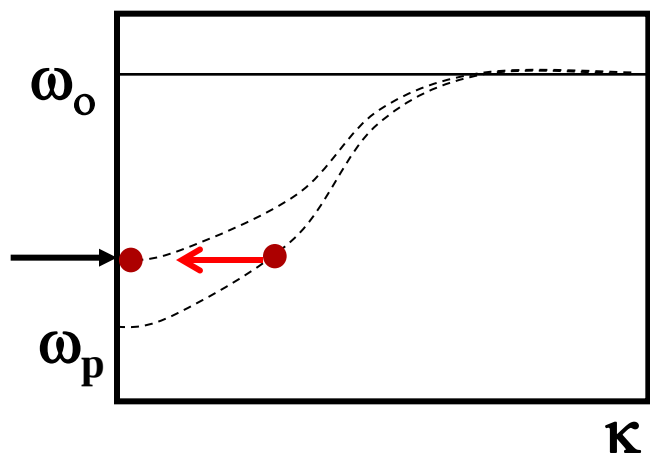




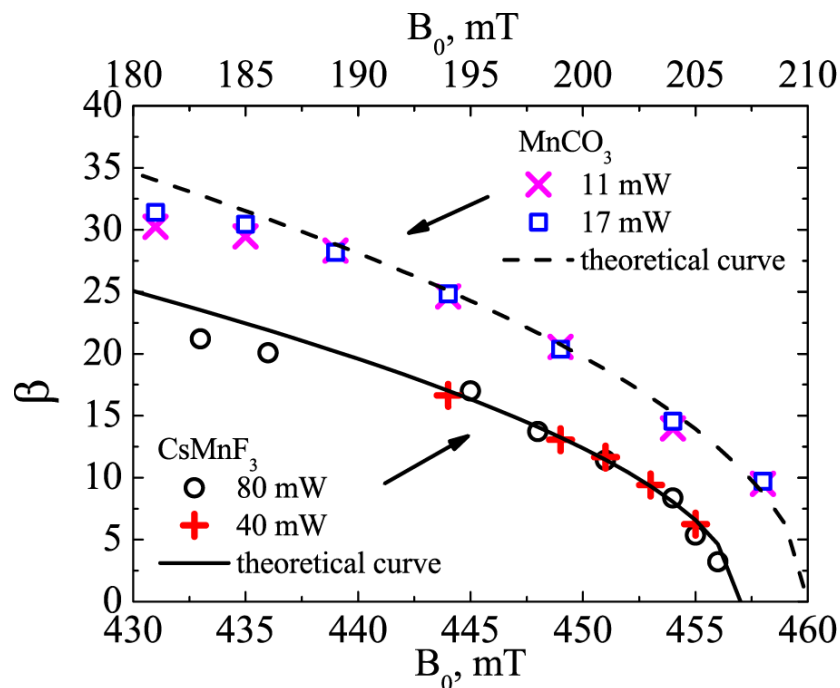
**FID amplitude vs. RF pulse length
at different magnetic fields**



Signal intensity vs. magnetic field

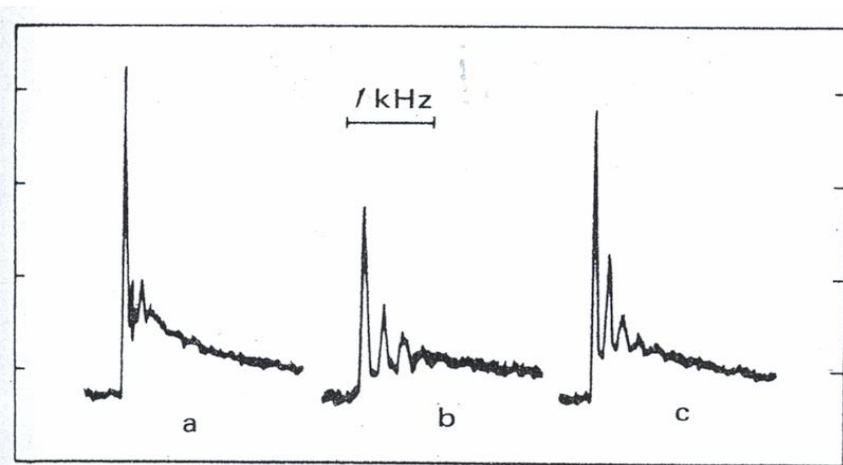


**FID amplitude vs. RF pulse length
at different magnetic fields**



Signal intensity vs. magnetic field

Non-linear Stationary Spin Waves in Flared out texture



Before rotation

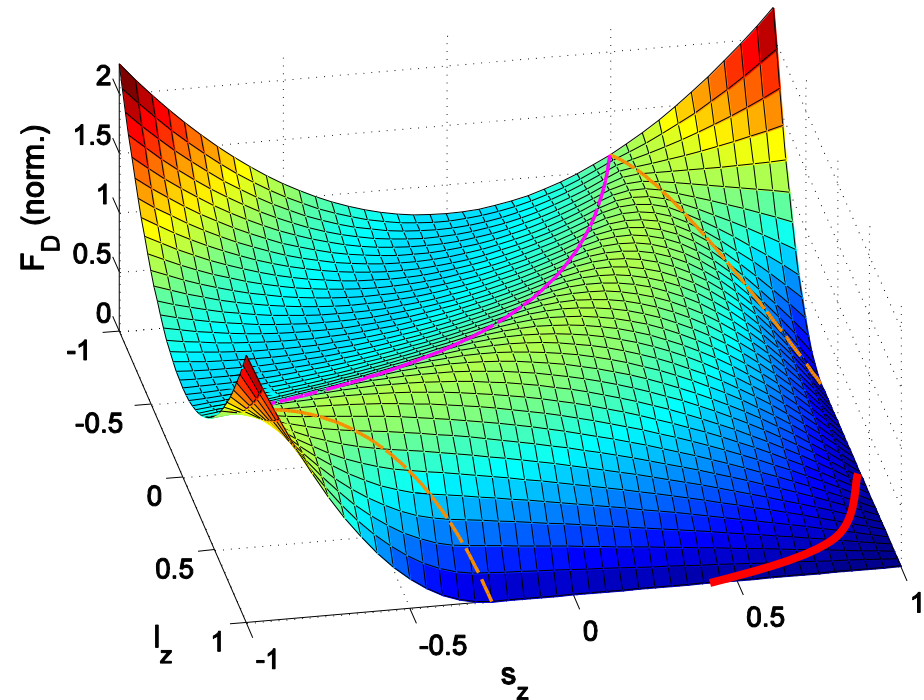
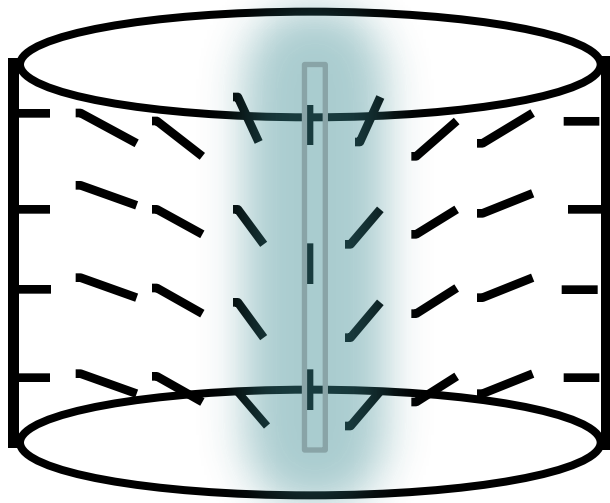
During rotation

After rotation

NMR of Rotated superfluid 3He-B
 O.T.Ikkala, G.E.Volovik, P.Y.Hakonen,
 Yu.M.Bunkov, S.T.Islander, G.A.Haradze,
 JETP Letters v.35, p.416 (1982).

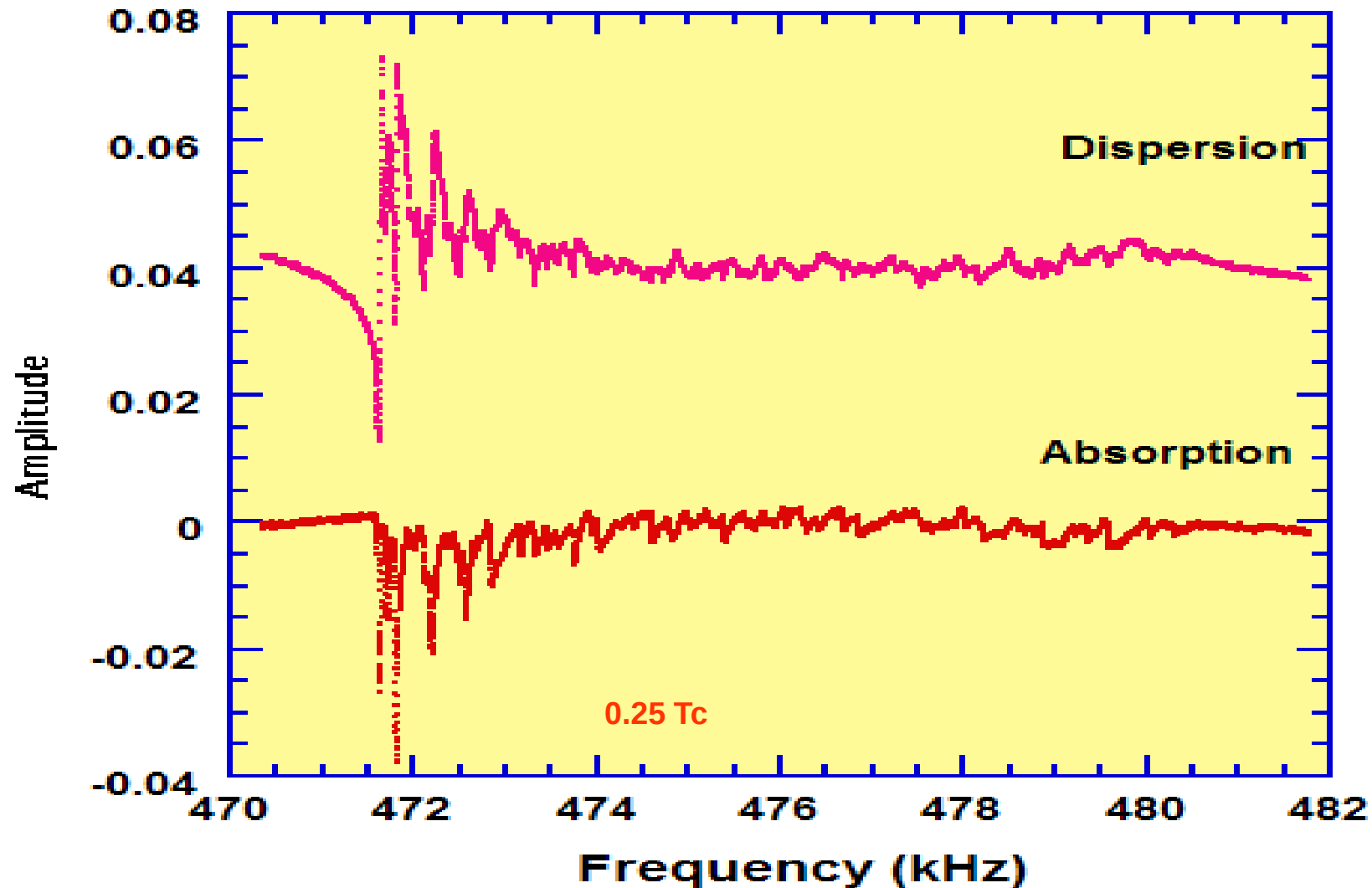
$$\omega^2 = (\gamma H)^2 + n_{\perp}^2 \Omega_D^2$$

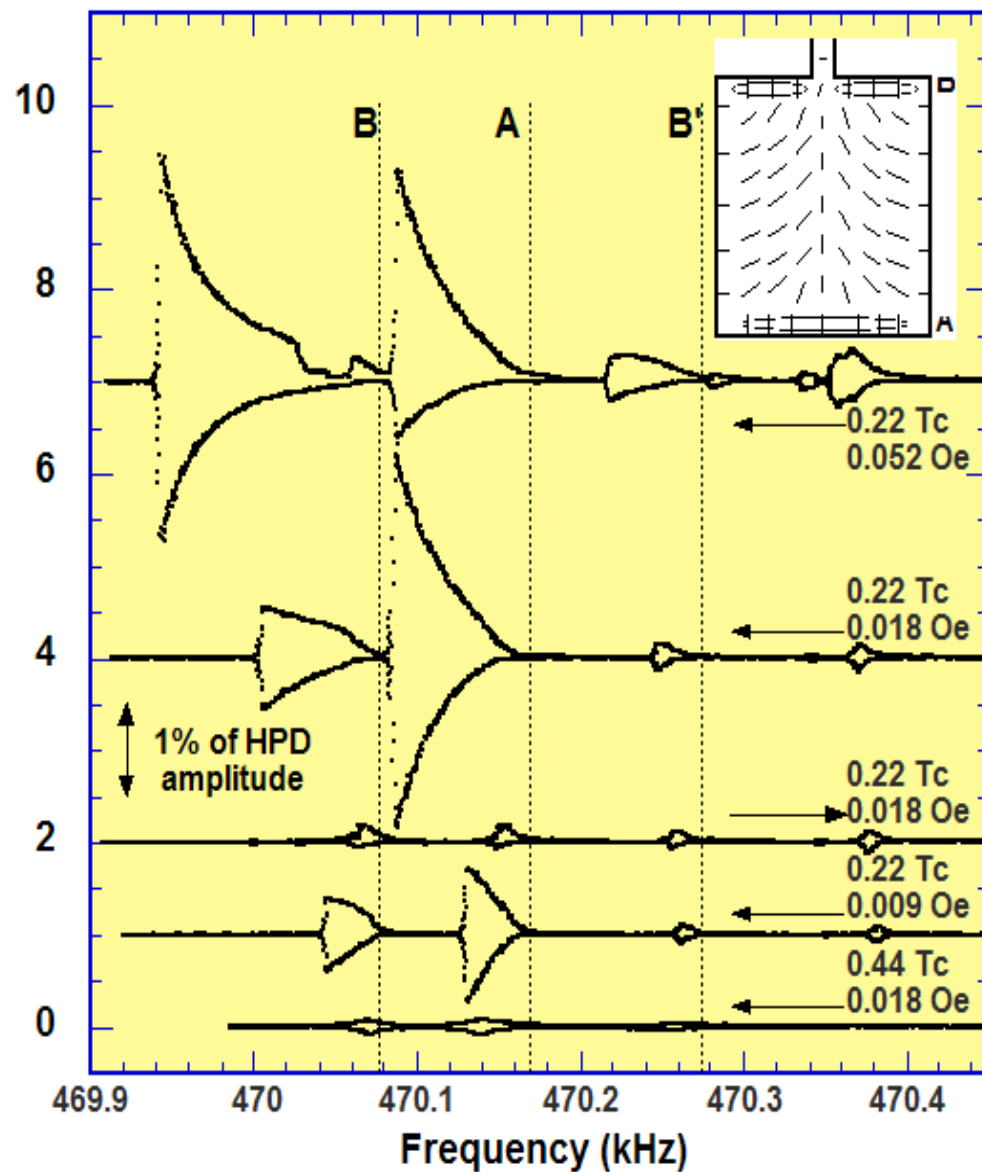
$$(\omega - \omega(z)) M^+ = \frac{\Omega_D^2}{2\omega(z)} \left(\frac{2}{5} \sin^2 \beta_L(r) - \frac{24}{65} \xi_d^2 \nabla^2 \right) M^+$$

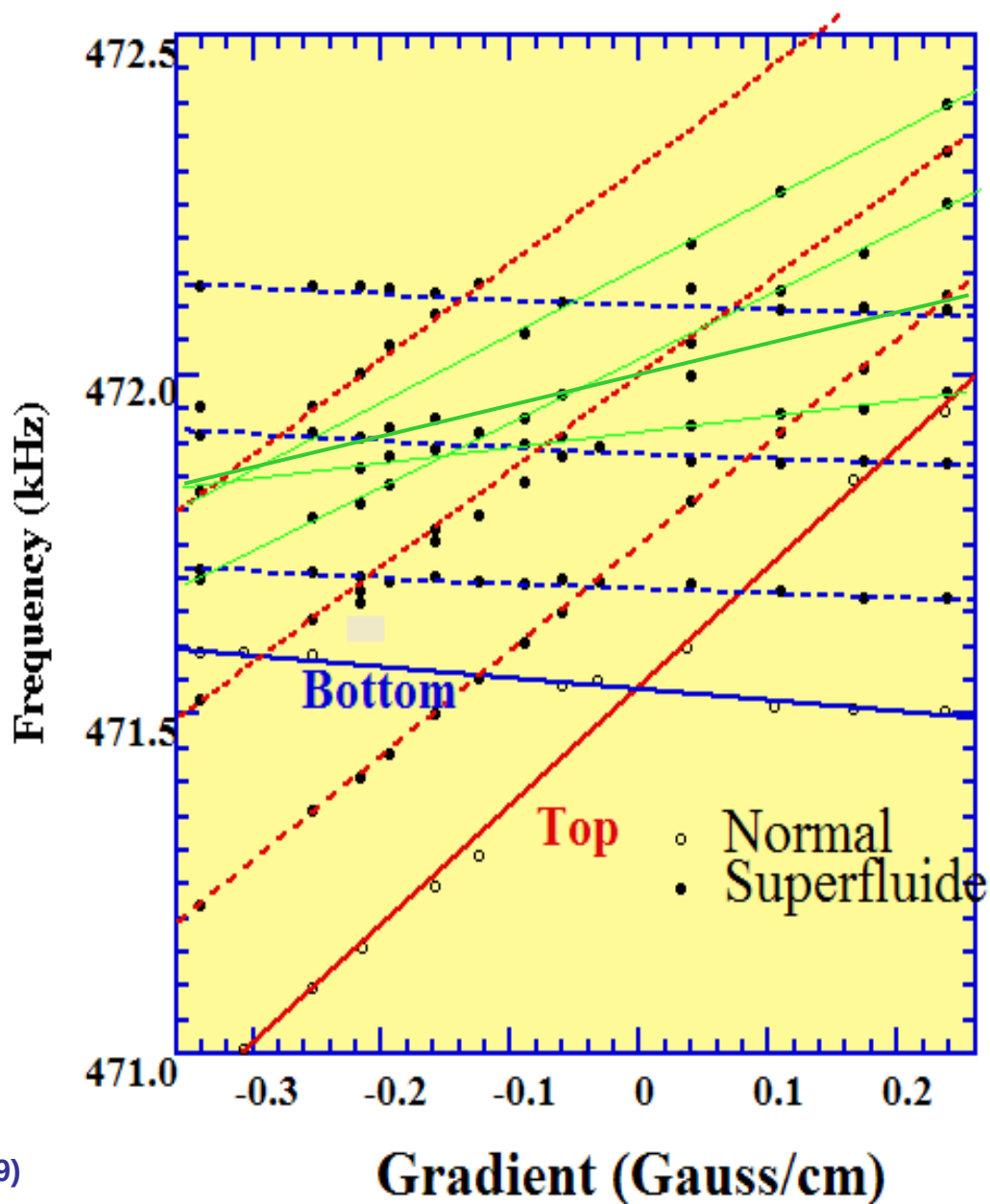
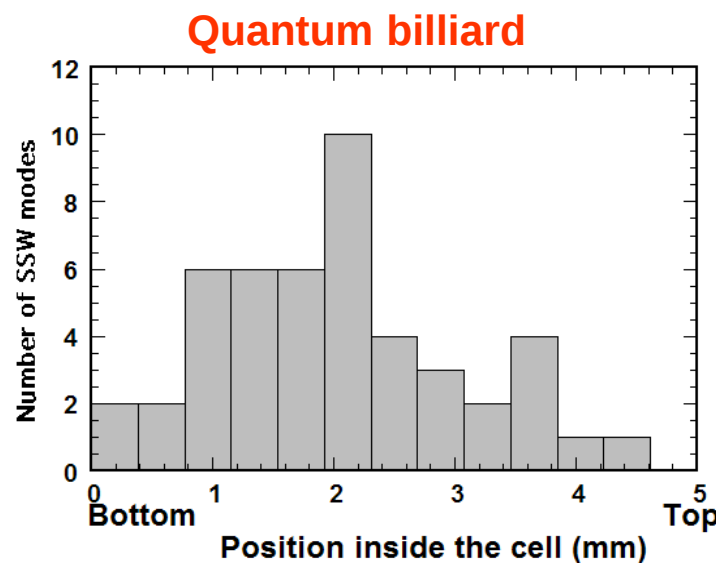
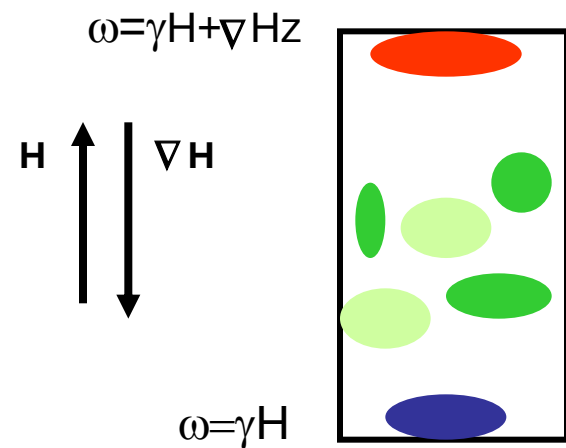


Grenoble experiments with Non-linear Stationary Spin Waves

A.-S. Chen, Yu.M. Bunkov, H. Godfrin, R. Schanen, F. Scheffer.
J. Low Temp. Phys, 110, p. 51, (1998).

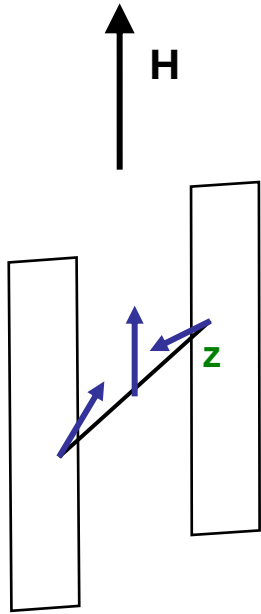




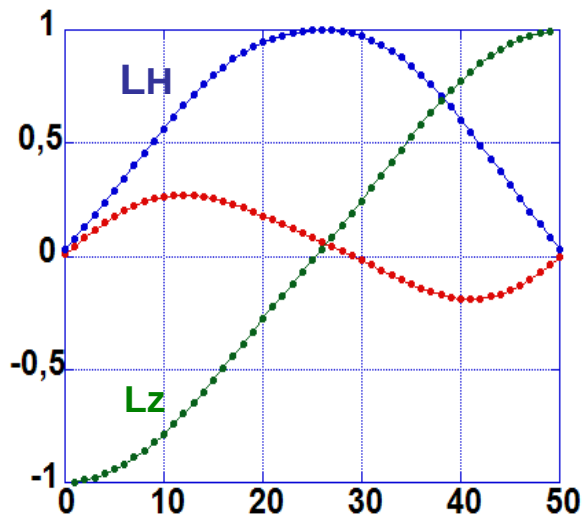
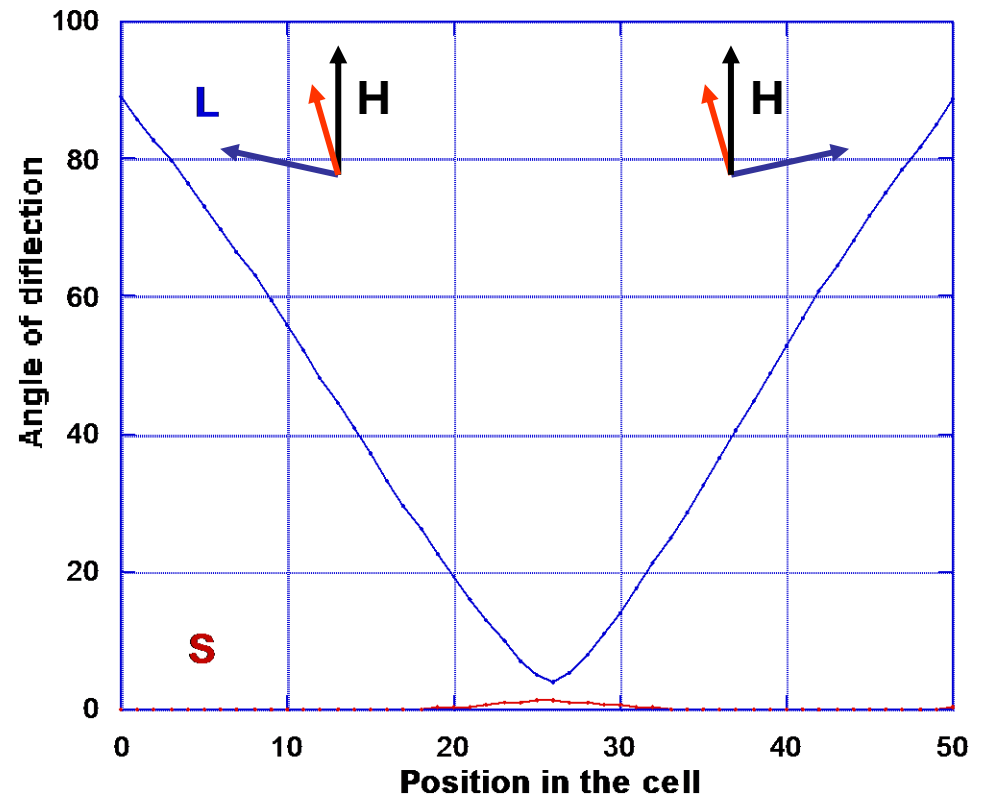


Computer simulation Grenoble 2004

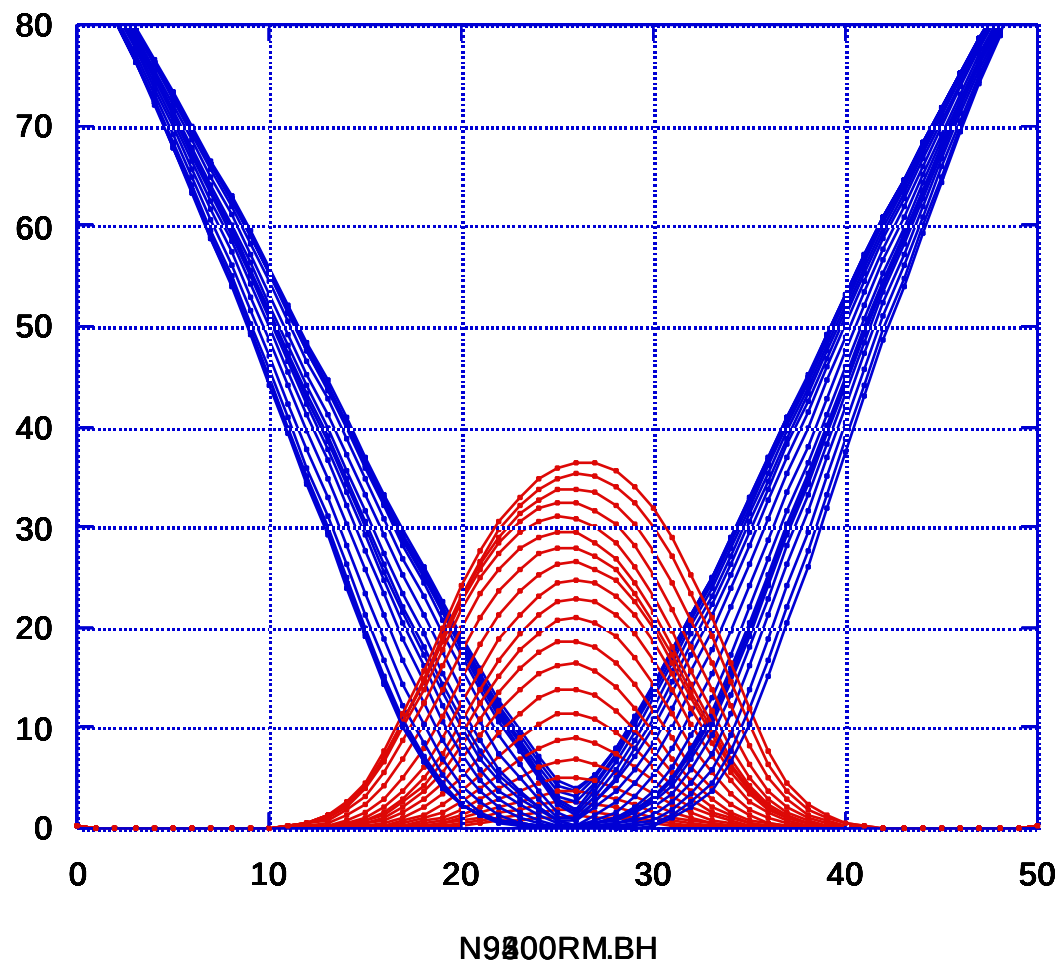
Follow Voislav Golo algorithm



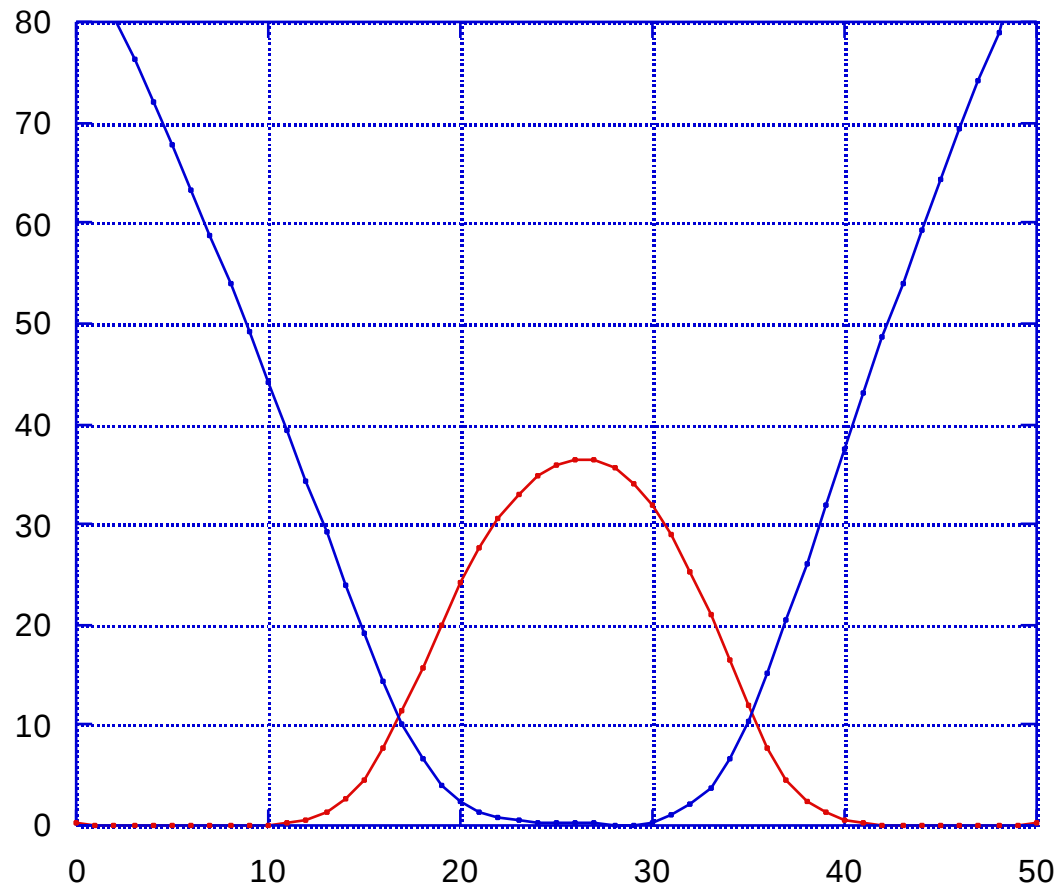
Calculations of a spatial deflection of spin and orbit on
basis of Poisson brackets and Takagi relaxation



Grenoble, 2004



Grenoble, 2004

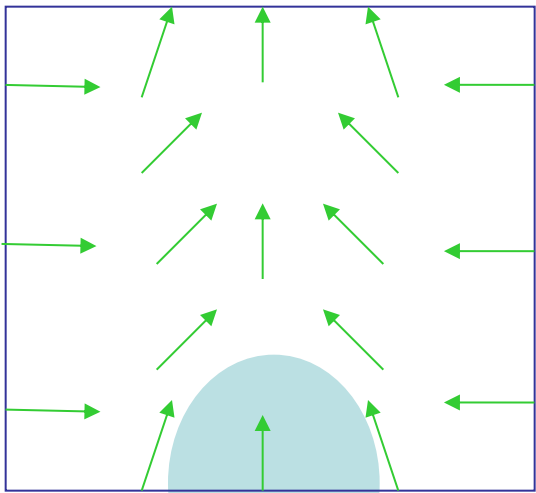


Magnons condensation in Q-balls In the orbital texture trap

CW NMR A.-S. Chen, Yu.M. Bunkov, H. Godfrin, R. Schanen, F. Scheffer.
 J. Low Temp. Phys, 110, 51, (1998), 113, 693 (1998).

Yu.M. Bunkov “Persistent Signal; Coherent NMR state Trapped by Orbital Texture”
 J. Low Temp. Phys, 138, 753 (2005)

Yu.M. Bunkov, G.E. Volovik, *Phys. Rev. Lett.*, 98, 265302 (2007).



3D axisymmetric trap.

$$\omega_{xy}^2 r^2 + \omega_z^2 z^2$$

$$F_D = \chi \Omega_L^2 \left[\frac{4 \sin^2(\beta_L/2)}{5S} |\Psi|^2 - \frac{\sin^4(\beta_L/2)}{S^2} |\Psi|^4 \right]$$

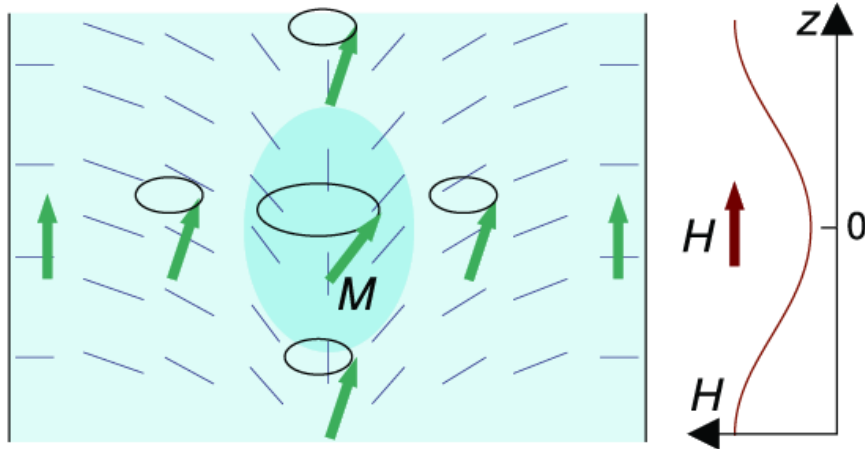
$$Q \sim |\Psi|^2 r_Q^2 \vec{l}_Q,$$

$$U(r, z) \propto \kappa^2 r^2 z^2 / (r^2 + z^2).$$

$$(\omega - \omega_L(z)) \Psi = \frac{\delta F}{\delta \Psi^*},$$

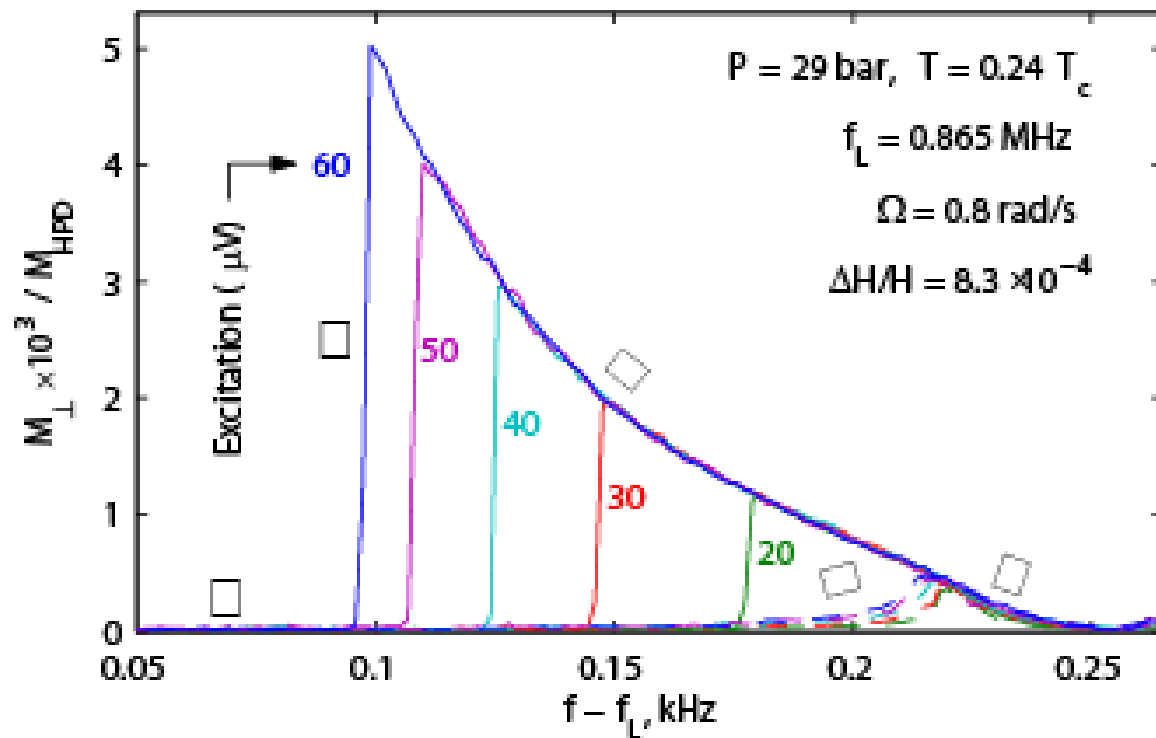
$$F = \int d^3 r \left(\frac{|\nabla \Psi|^2}{2m_M} + F_D \right),$$

Non-ground-state Bose-Einstein condensates of magnons in superfluid 3He-B



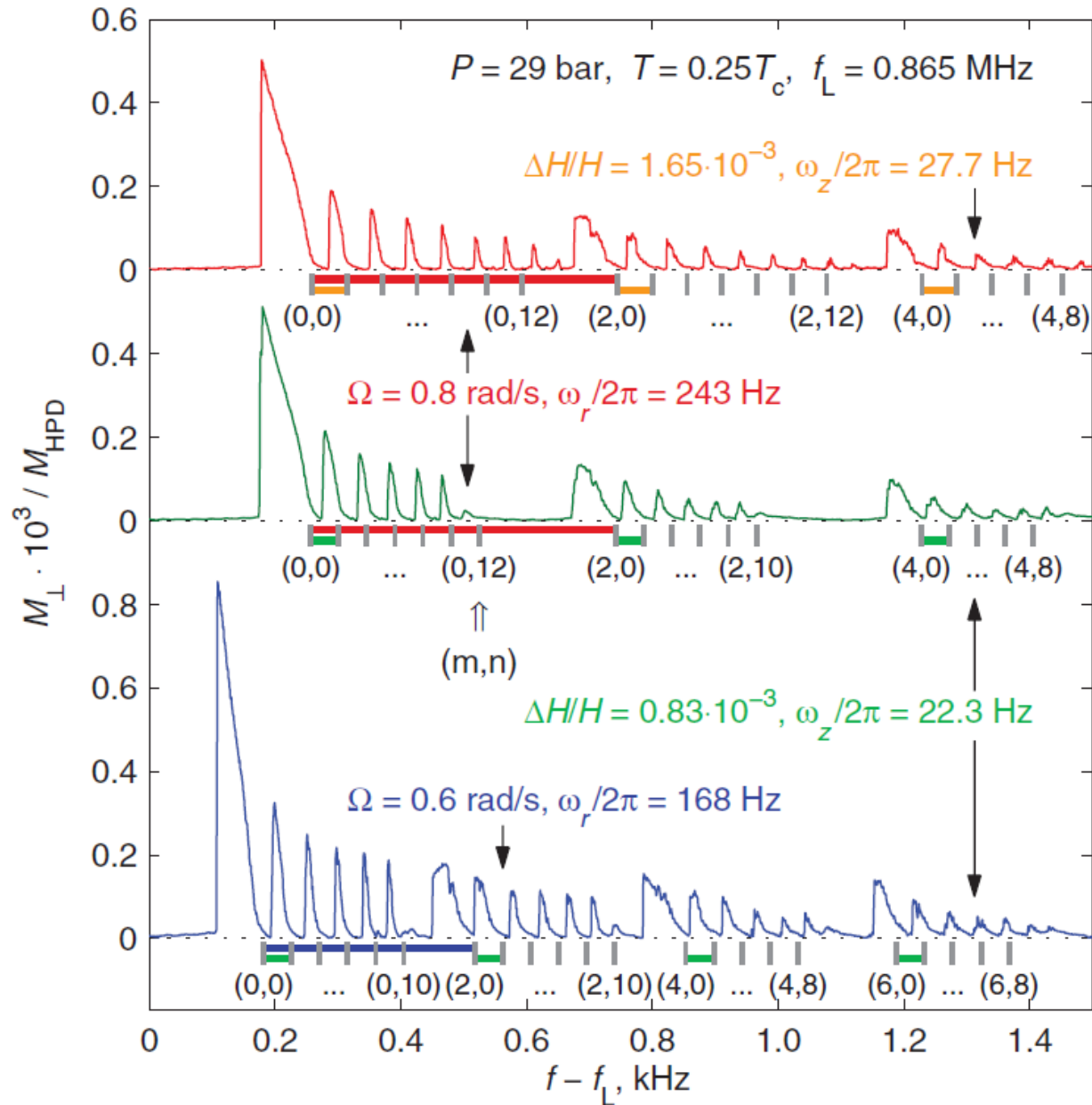
3D axisymmetric trap.

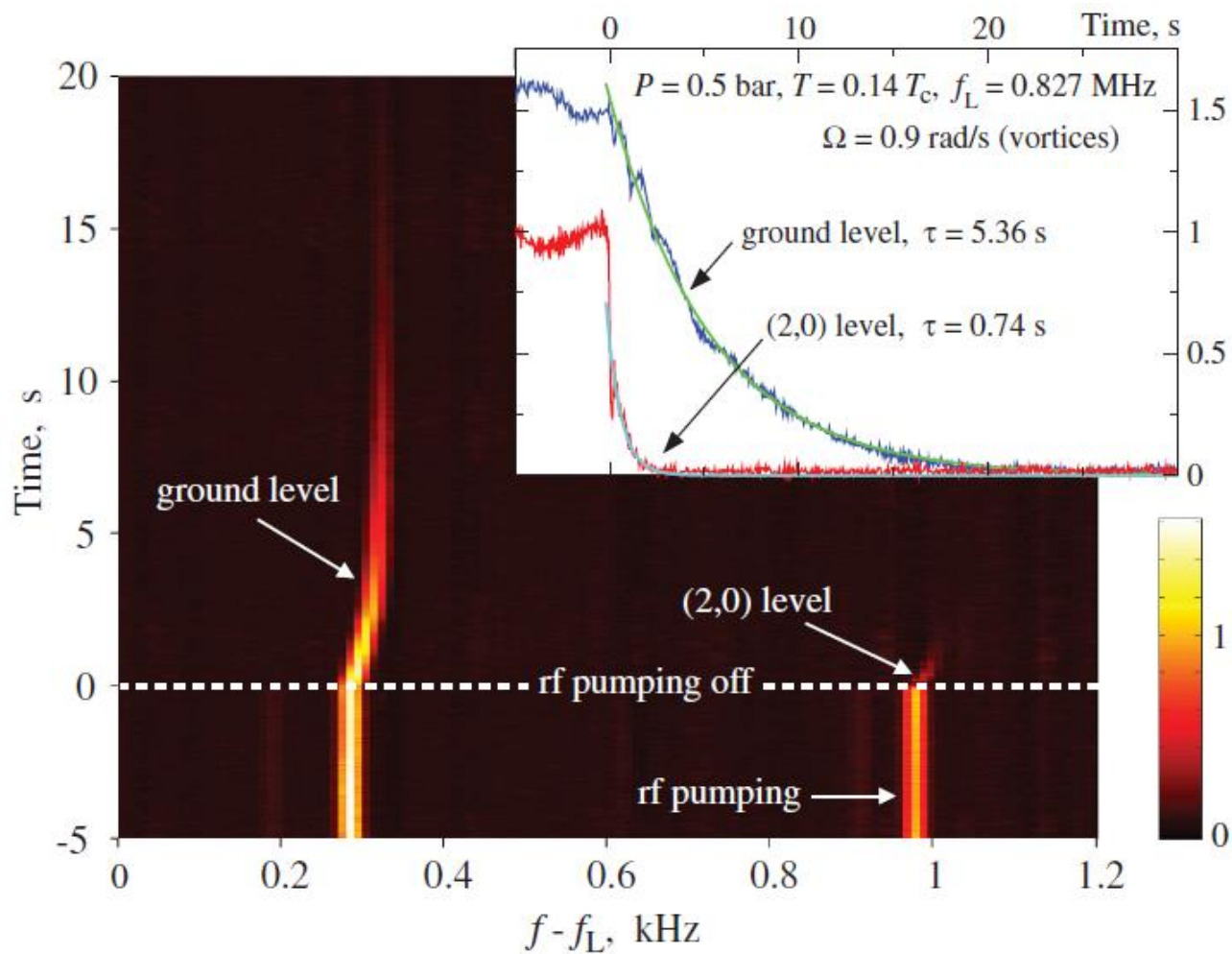
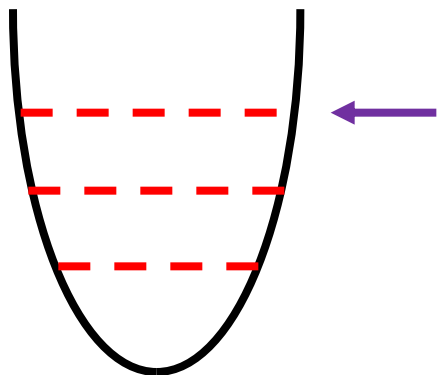
$$\omega_{xy}^2 r^2 + \omega_z^2 z^2$$



Non-ground-state Bose-Einstein condensates of magnons in superfluid $^3\text{He-B}$

$$f - f_0 = a_r(\Omega)(2n_r + 1) + a_z(2n_z + 1/2),$$





Conclusions

The Spin Superfluidity, the magnetic counterpart of mass superfluidity and electric superconductivity was discovered and widely studied in Moscow, Grenoble, Lancaster, Ithaca, Helsinki, Kosice, Kyoto, Tokio, Los-Alamos and by many theoreticians.

There was discovered and observed:

1. The coherent transport of magnetization in superfluid $^3\text{He-B}$.
2. Its based only on an antiferromagnetic properties of ^3He and can be found in other magnetically ordered materials.
3. The formation of domain with coherent precession of magnetization.
4. This excited state correspond to a Bose-Einstein Condensation of spin waves.
5. Josephson phenomena, critical current and phase slippage in a channel.
5. Different modes of HPD oscillations.
6. Horizontal and vertical Spin vortex.
7. HPD techniques was applied for studies of counterflow and mass vortices in ^3He , new types of vortex - spin-mass vortex was observed
8. 6 different states with coherent precession in A and B phases of ^3He
9. Magon BEC was found recently in JYG. (Demokritov) *Nature* 443, 430 (2006).

The end

