

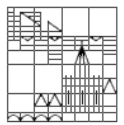


Commensurability-dependent transport of a
Wigner crystal in a nanoconstriction



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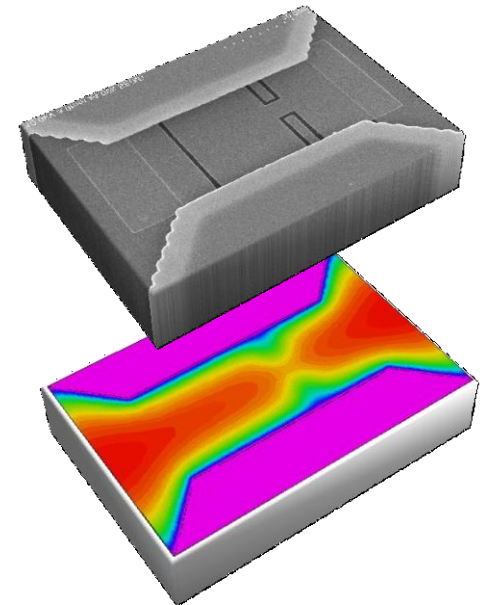


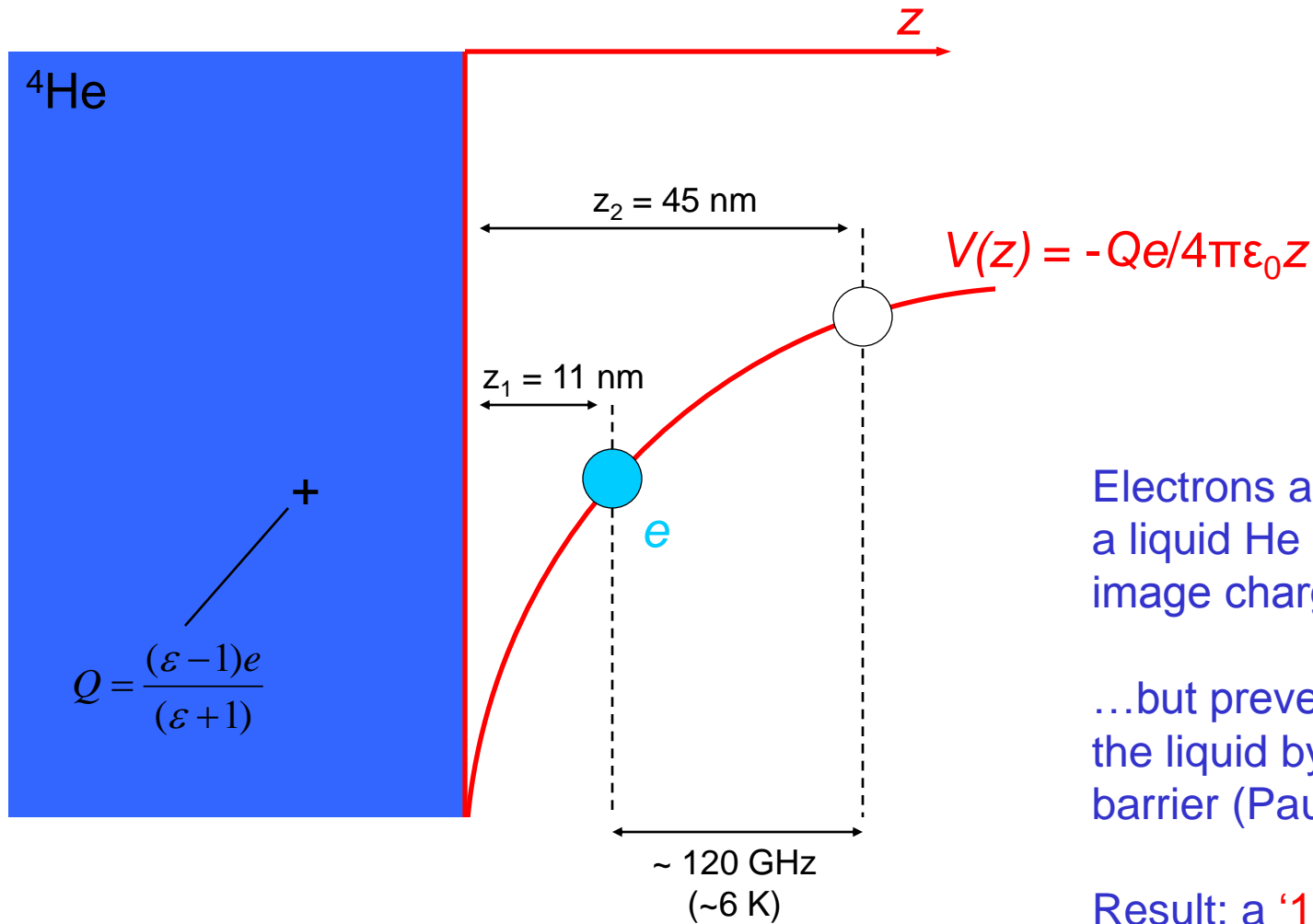
Paul Leiderer (University of Konstanz)
Hiroo Totsuji (Okayama University)



OKAYAMA UNIVERSITY

- Introduction - Electrons on helium
- Microchannel samples for mesoscopic experiments
- Point-contact transport properties of classical electron liquids
- Point-contact transport properties of Wigner crystals
- Conclusions



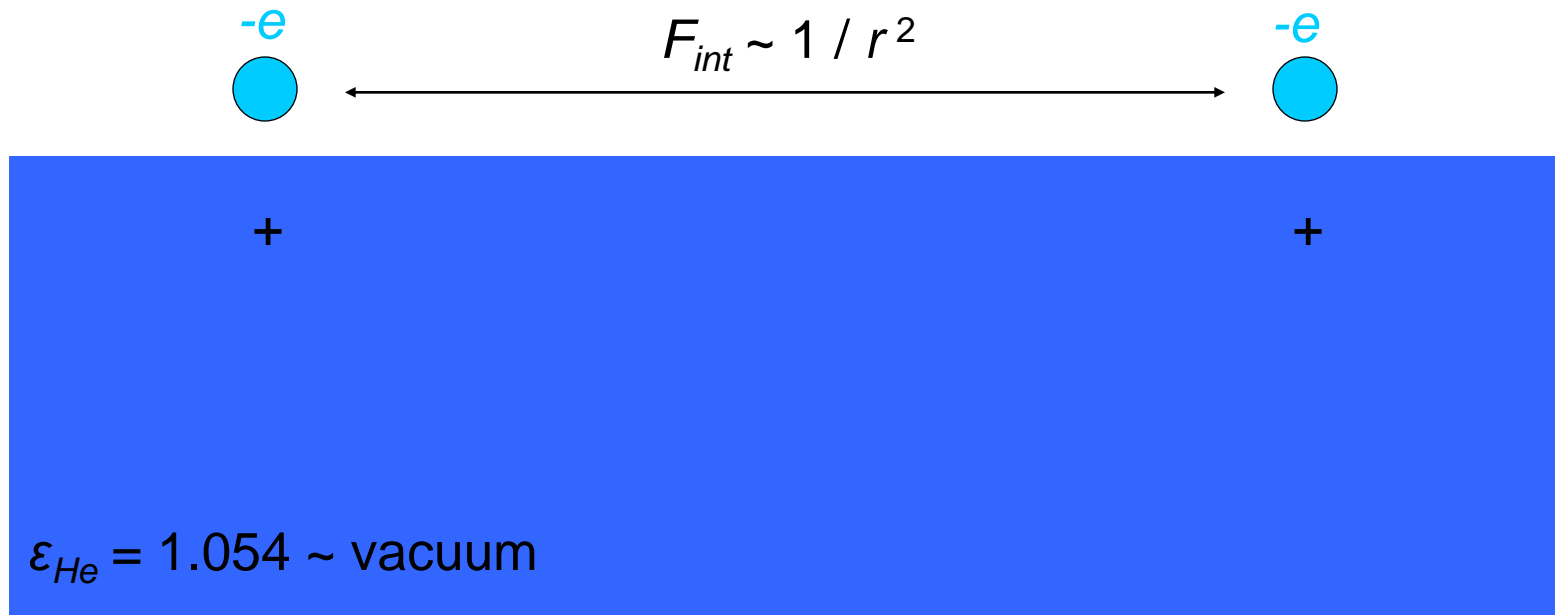


Electrons are attracted to a liquid He surface by an image charge...

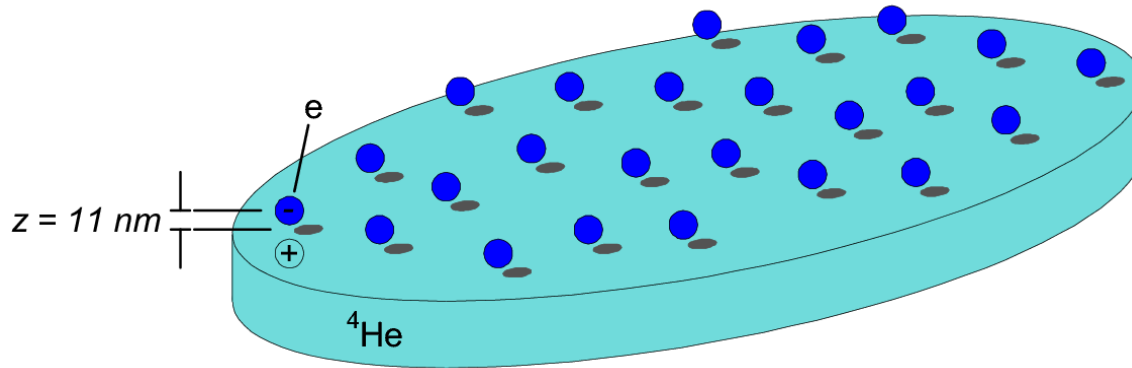
...but prevented from entering the liquid by a $\sim 1\text{eV}$ potential barrier (Pauli).

Result: a '1D Hydrogen atom' with Rydberg series of states.

The Coulomb interaction between electrons is essentially unscreened:



We can (almost) consider electrons floating in free space...



'Low' surface density: $n_s \sim 10^6 - 10^9 \text{ cm}^{-2}$

Liquid helium is a perfectly clean substrate: $\mu \sim 10^8 \text{ cm}^2/\text{V}\cdot\text{s}$ at 10 mK

→ A nondegenerate, high mobility, 'classical' 2D electron liquid (or solid)

	GaAs-2DEG	electrons on helium
n_s	$10^{10} - 10^{12} \text{ cm}^{-2}$	$10^6 - 10^9 \text{ cm}^{-2}$
Mass	$m_e^* \sim 0.067 m_e$	m_e
E_F	$\sim 10 \text{ K}$	$\sim 1 \text{ mK}$
Velocity	$\hbar k_F / m_e^* \sim 10^7 \text{ cm/s}$	$(2k_B T / m_e)^{1/2} \sim 10^5 \text{ cm/s}$
Mobility	$\sim 10^6 \text{ cm}^2/\text{Vs}$	$\sim 10^8 \text{ cm}^2/\text{Vs}$
Mean free path	$\sim 10 \mu\text{m}$	$\sim 1 \mu\text{m}$ (at 1 K)
System characteristics	Fermi degenerate electron gas	Nondegenerate Coulomb liquid / crystal

Classical many-body physics in strongly-correlated systems:

- Wigner crystallisation
- 2D melting in confined geometry
- Transport of interacting particles: Jamming, pinning etc...

What can we do with electrons on helium?

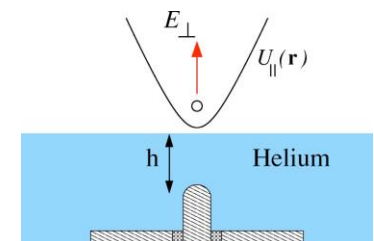
Quantum electron dynamics in a low-decoherence environment:

- Quantum transport (D. Konstantinov *et al.*, Phys. Rev. Lett., **105** (2010))
- Qubits* with long coherence times?

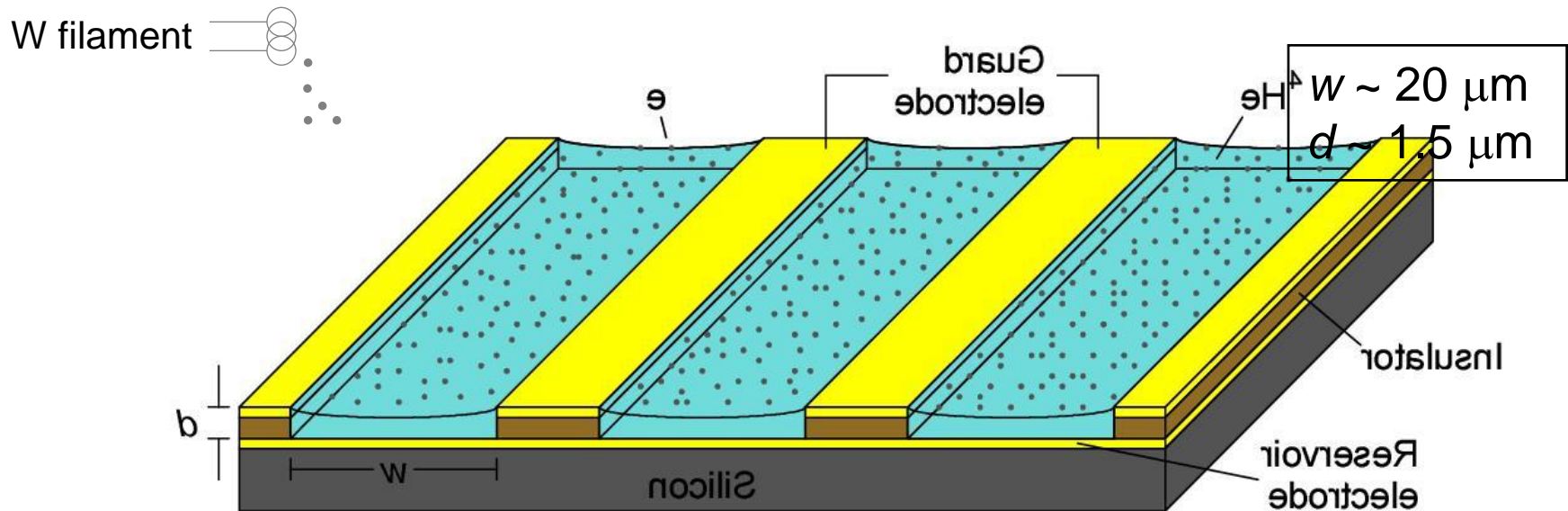
*Rydberg states: P.M. Platzman and M.I. Dykman., Science **284** (1999)

*Spin states: S.A. Lyon, Phys. Rev. A **74** (2006)

*Orbital states: D. Schuster *et al.*, Phys. Rev. Lett. **105** (2010)



Mesoscopics? Use **microchannels** filled by **capillary action** of superfluid ^4He :

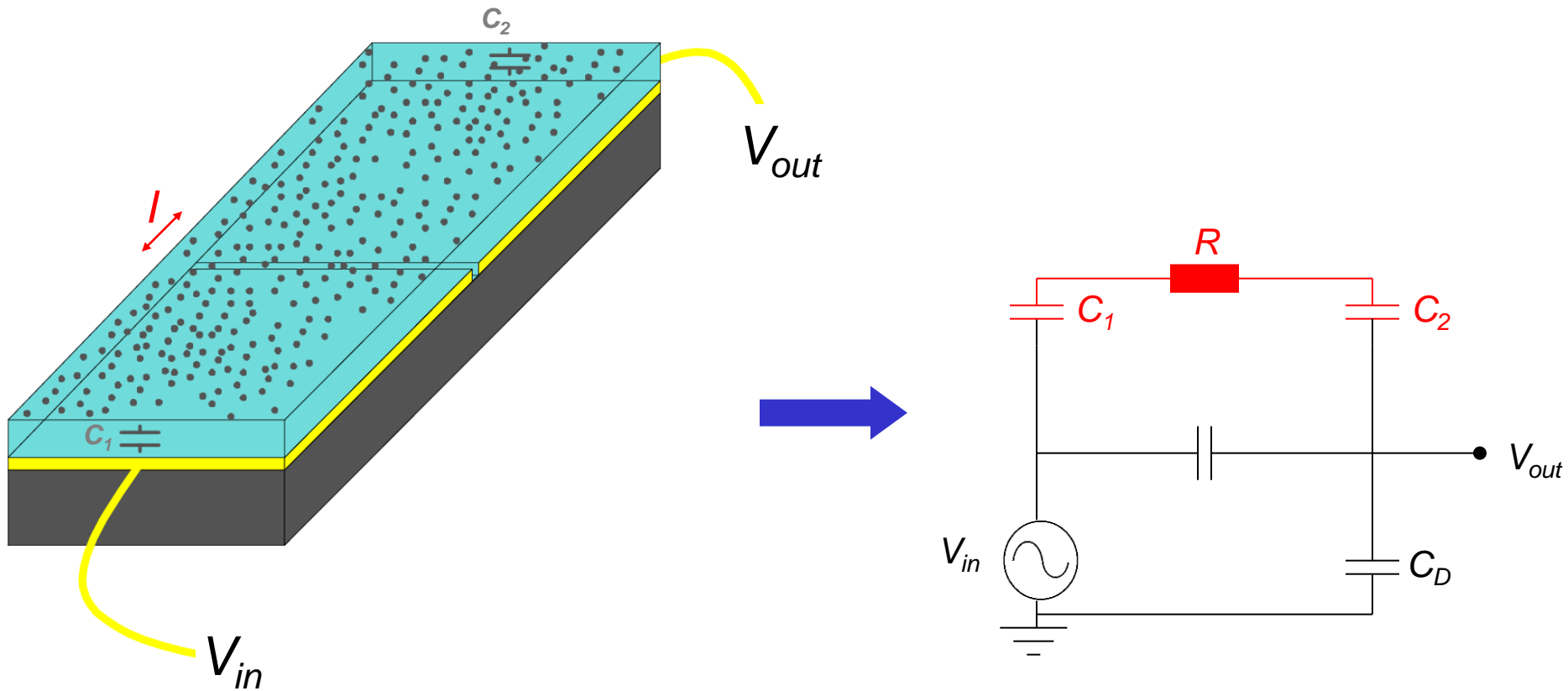


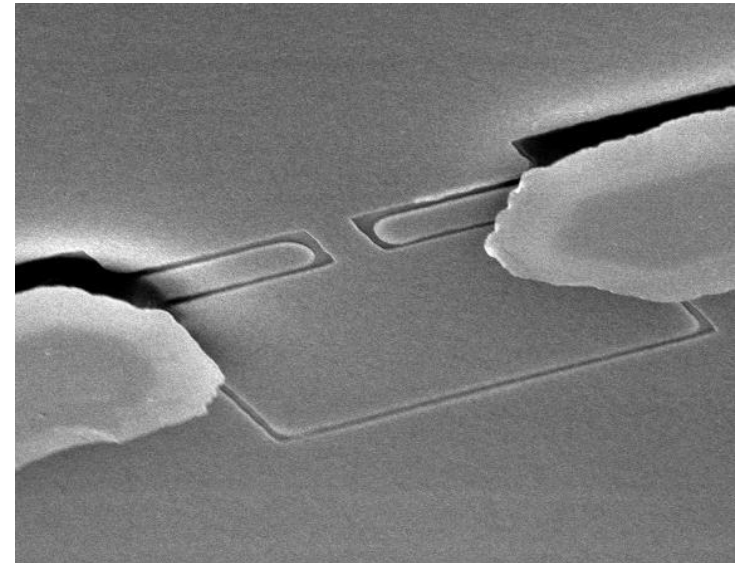
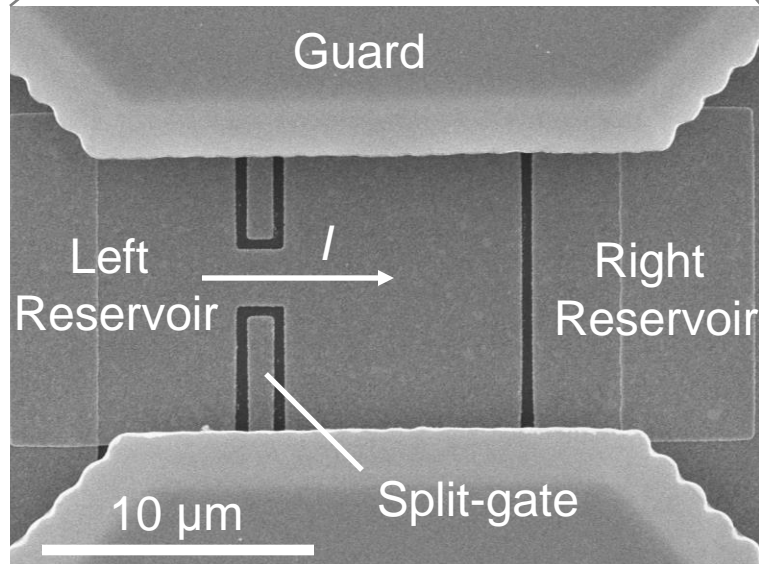
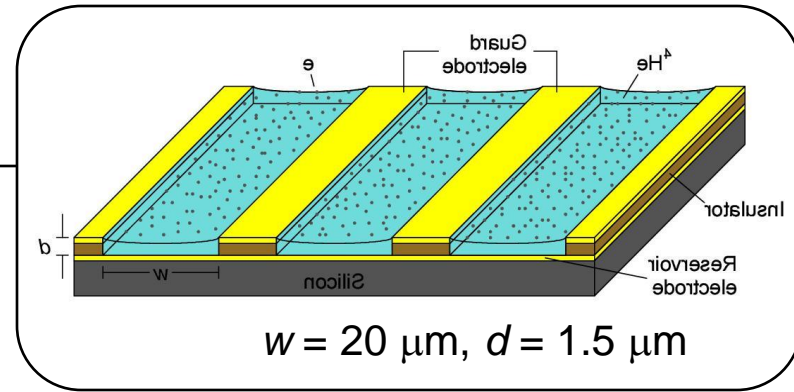
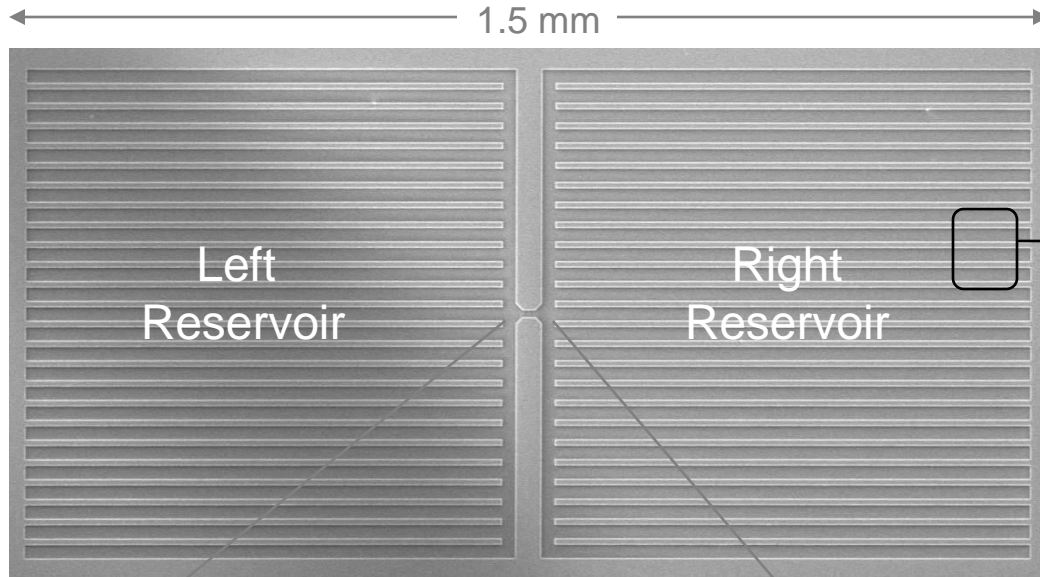
D. G. Rees *et al.*, J. Low Temp. Phys. (2011)

Fabrication techniques:

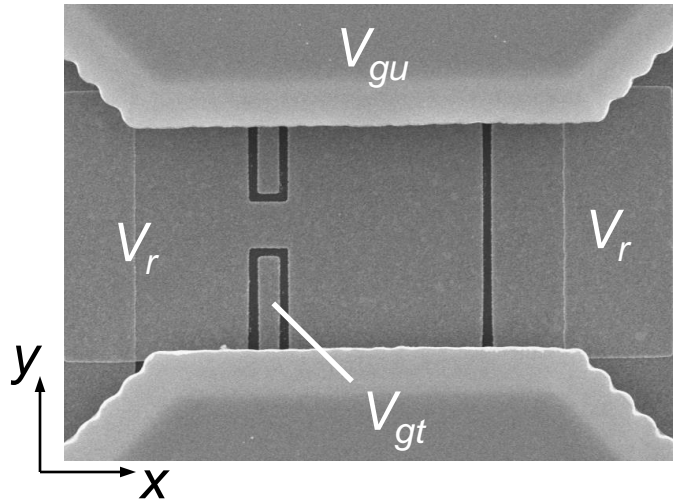
- UV / e-beam lithography (2 or 3 layers)
- Thermal / e-beam evaporation of metals
- Etching of hard-baked photoresist to create insulating layer

We can measure the transport properties of the electron system using a lumped-circuit model:

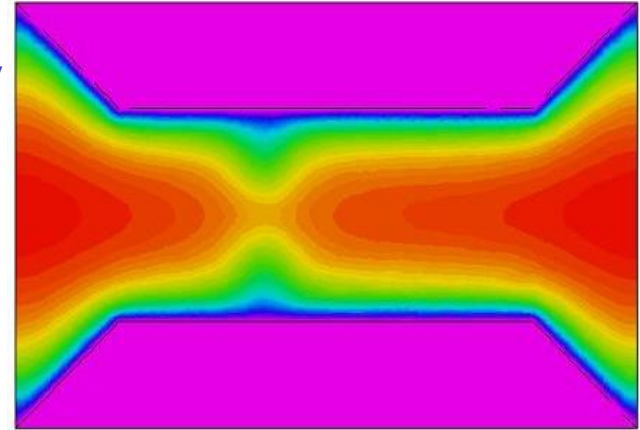




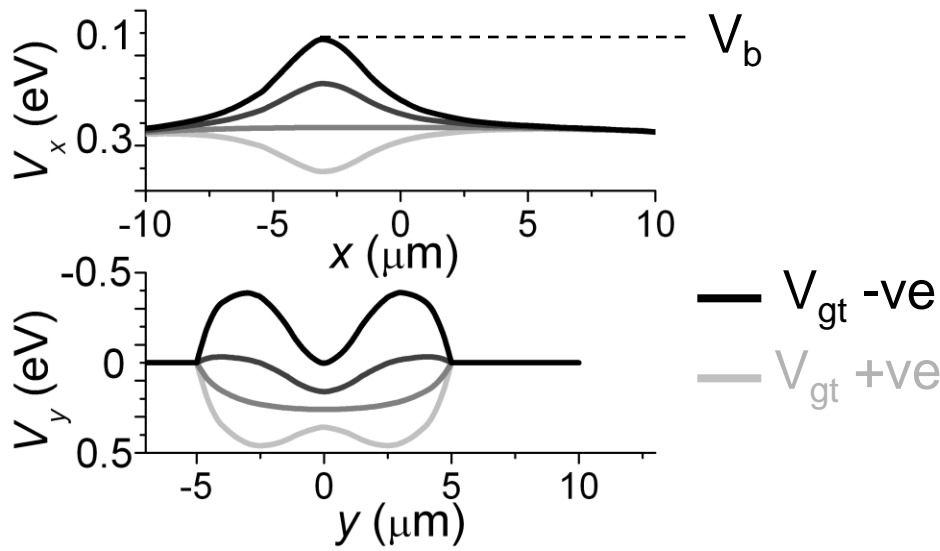
Finite-element modelling shows that a *saddle-point potential* is created at the constriction:



$$\begin{aligned} V_{gu} &= 0 \text{ V} \\ V_{gt} &= +0.5 \text{ V} \\ V_r &= +1 \text{ V:} \end{aligned}$$



At negative gate voltage we may form a potential barrier between reservoirs:



From the model we find:

$$V_b = \alpha V_r + \beta V_{gt} + \gamma V_{gu}$$

$$\alpha = 0.75, \beta = 0.10, \gamma = 0.15$$

$$T_{Well} \sim 20 \text{ GHz} \sim 1 \text{ K} \sim 0.1 \text{ meV}$$

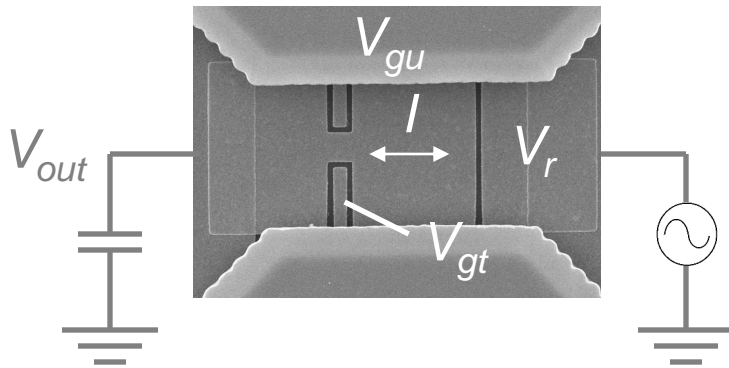
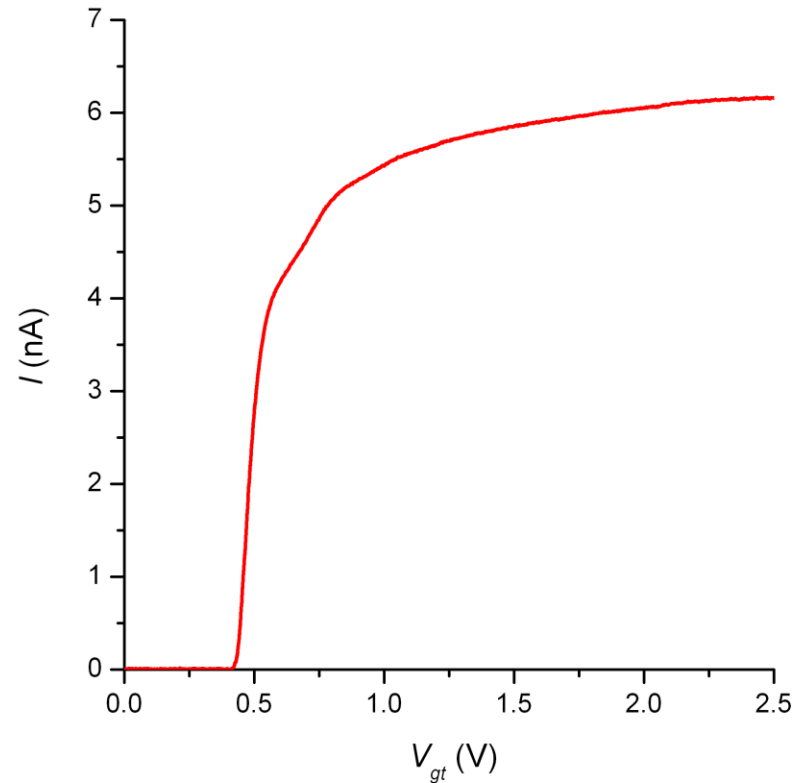
Experimental parameters:

$$T = 1.2 \text{ K}$$

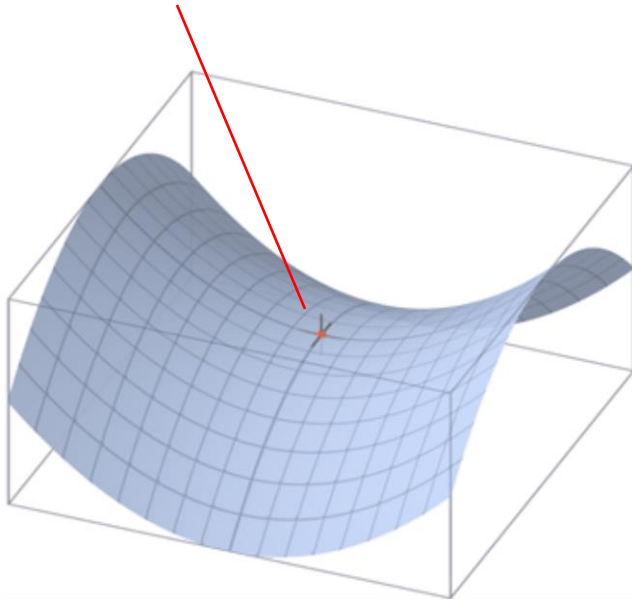
$$V_r = +1 \text{ V}, V_{gu} = 0 \text{ V}$$

$$n_s = 2 \times 10^9 \text{ cm}^{-2}$$

$$\text{Ⓢ} V_{in} \sim 5 \text{ mV}_{pp}$$

Sweep V_{gt} :

$$V_b = \alpha V_r + \beta V_{gt} + \gamma V_{gu}$$

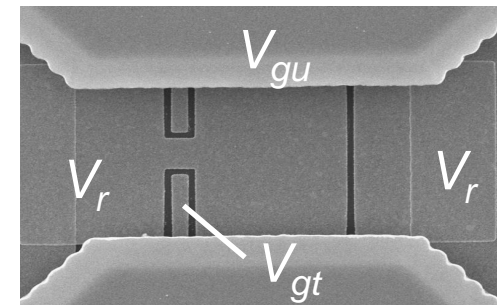


From V_{gt} threshold measurements:

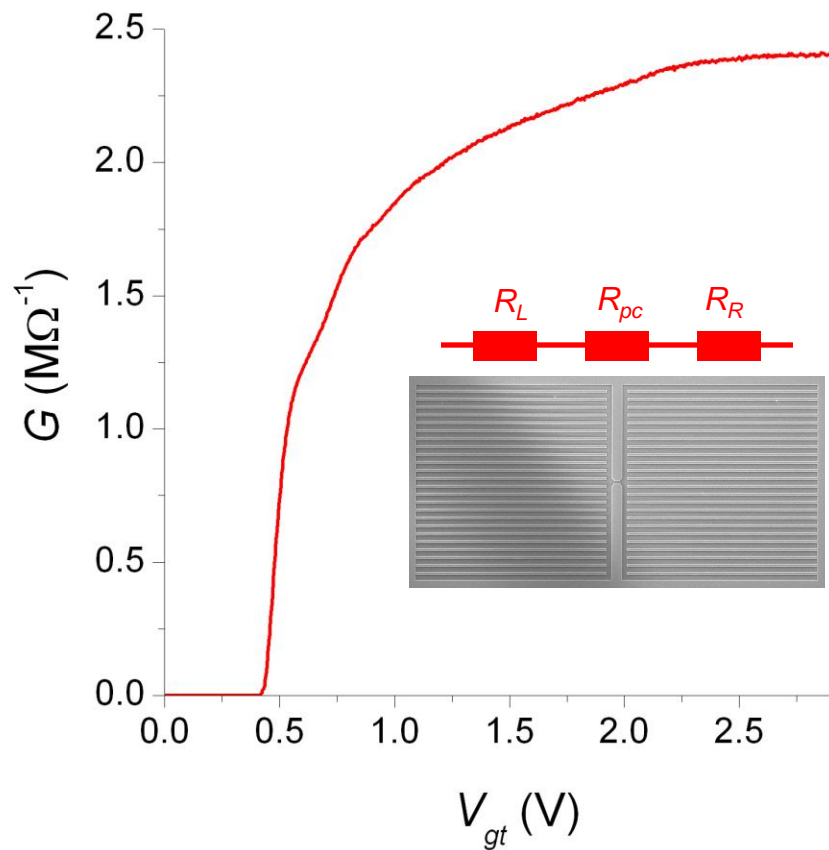
Coupling Constant	Model	Measured
α	0.75	0.77
β	0.10	0.16
γ	0.15	0.07

Good agreement...

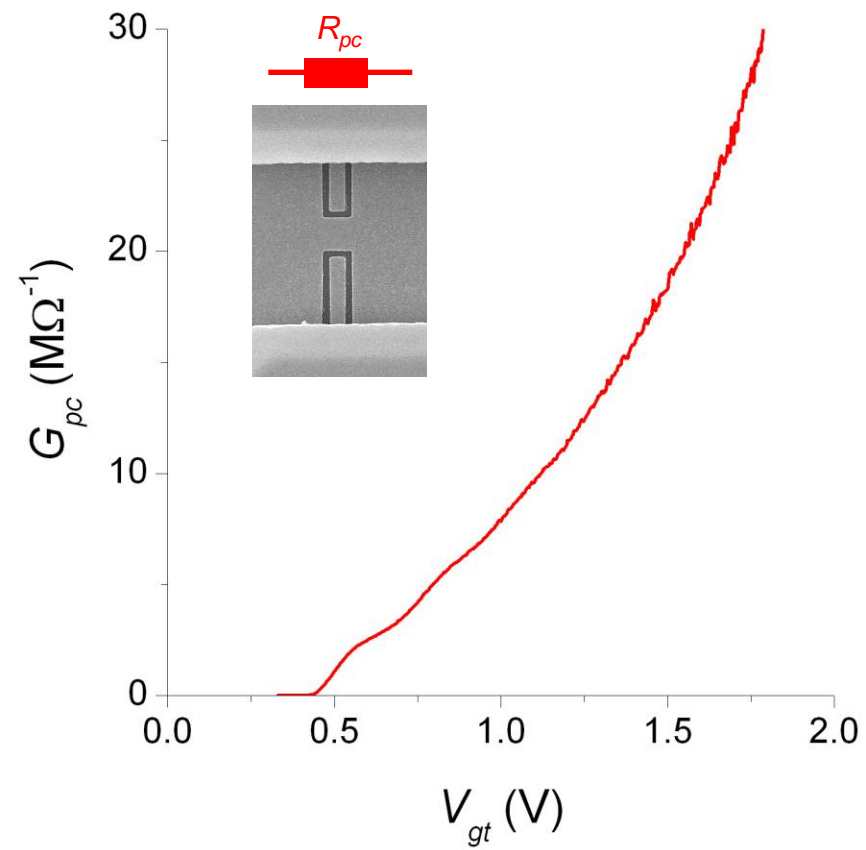
Electrons are indeed above the reservoir electrode, between the split-gate:

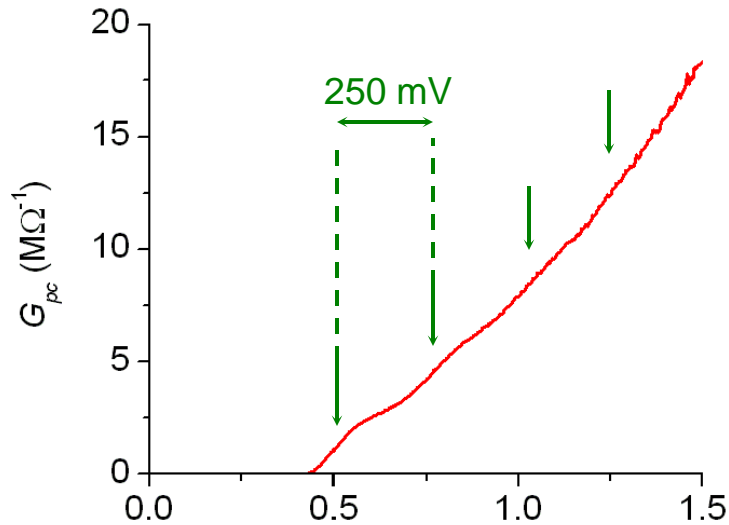


Total conductance:



Point-contact conductance:

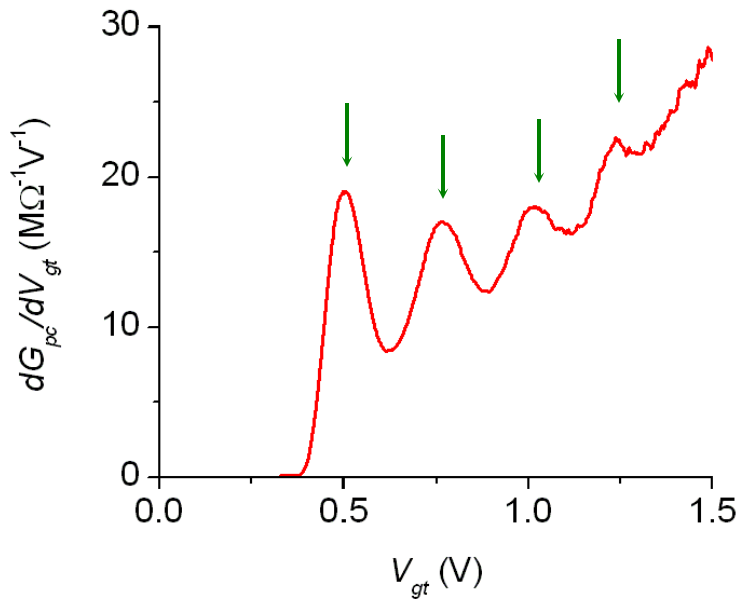
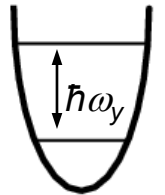




Here $k_B T \gg E_F$

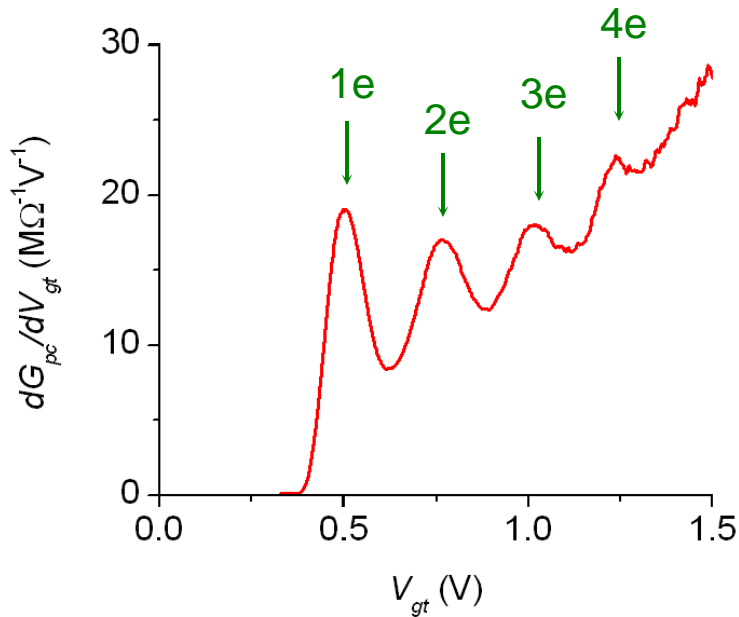
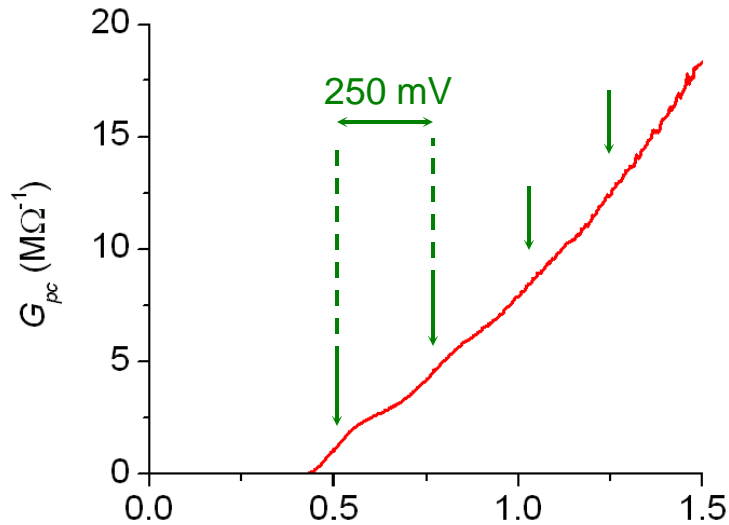
also: $V_{in} \sim 5 \text{ mV}_{pp}$

whilst: $\hbar\omega_y \sim 0.1 \text{ meV}$

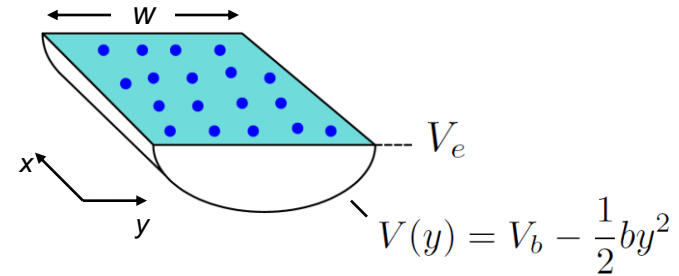


The steps are unlikely to be related to lateral subbands:

This is not a 'quantum' point contact



Consider the number of electrons
across the constriction:

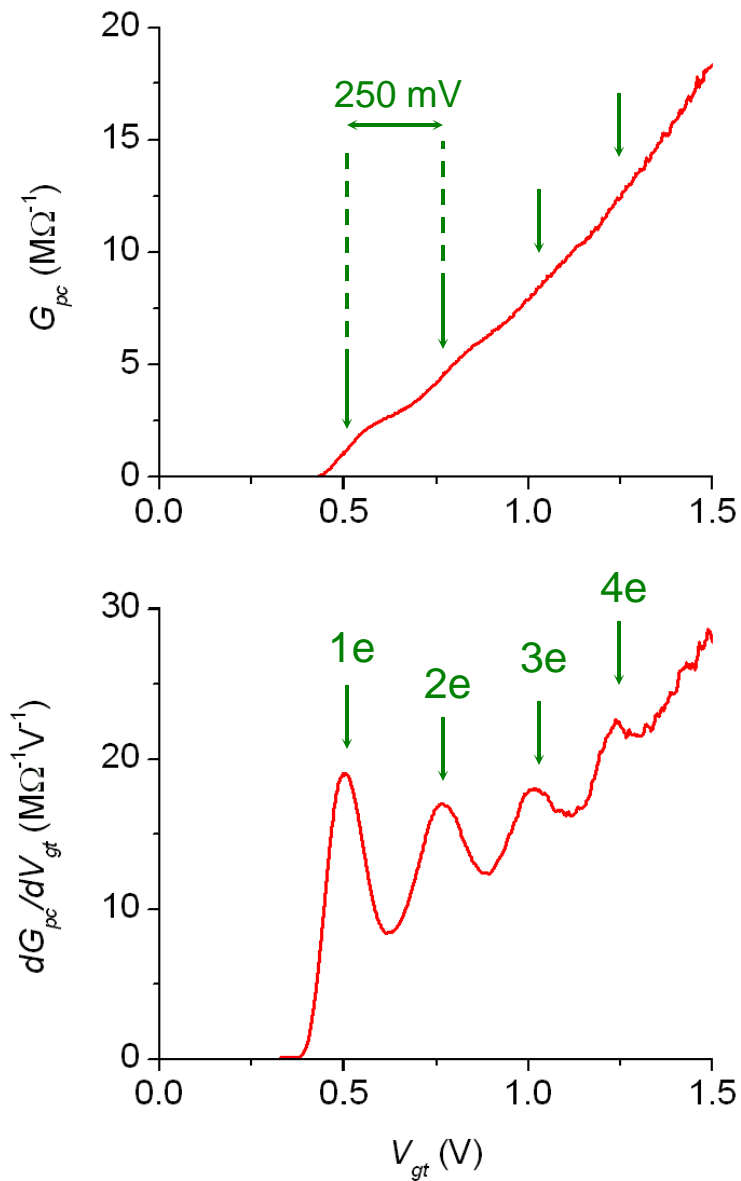


$$N_y = \left(\int_{-\frac{w}{2}}^{\frac{w}{2}} \int_{-\frac{w}{2}}^{\frac{w}{2}} \frac{\epsilon\epsilon_0}{ed} (V(y) - V_e) dx dy \right)^{\frac{1}{2}}$$

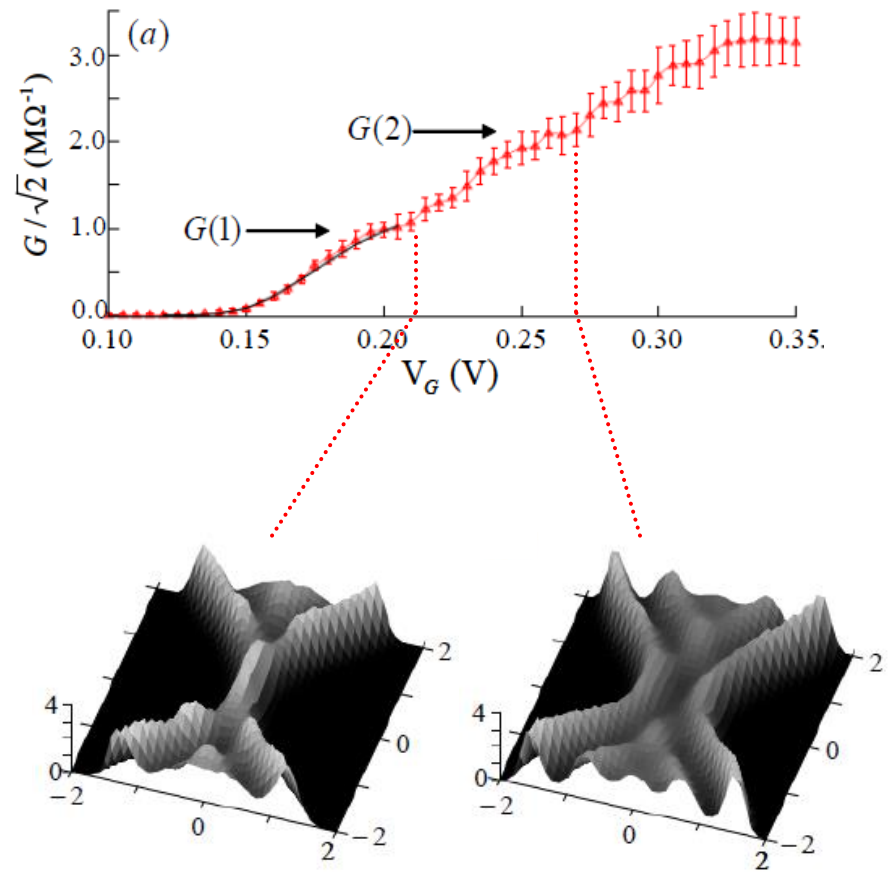
$$= \left(\frac{1}{b} \cdot \frac{16\epsilon\epsilon_0}{3ed} \right)^{\frac{1}{2}} \beta (V_{gt} - V_{gt}^{th})$$

ΔV_{gt} required to add 1 electron 'row':

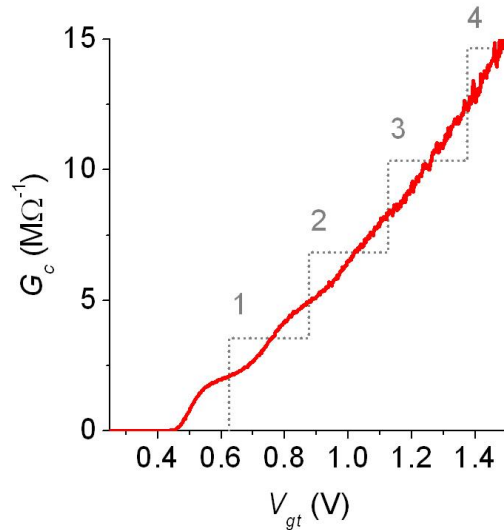
$$\underline{\underline{\Delta V_{gt} = 225 \text{ mV}}}$$



Molecular dynamics simulations by
M. Araki and H. Hayakawa, Kyoto University:



Why are the steps smoothed?



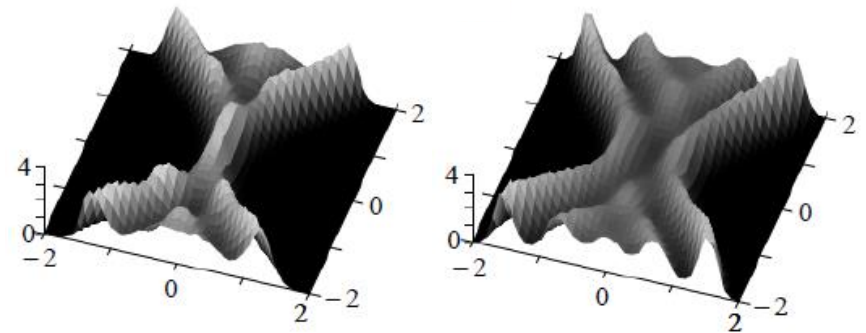
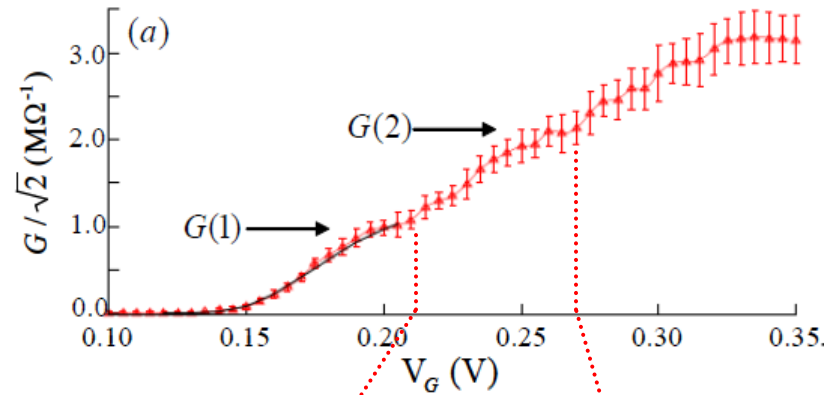
In the strongly-correlated system, electrons 'see' a strongly fluctuating electric field:

$$E_{fl} \sim T^{1/2} n^{3/4} \quad (\text{bulk 2D system})$$

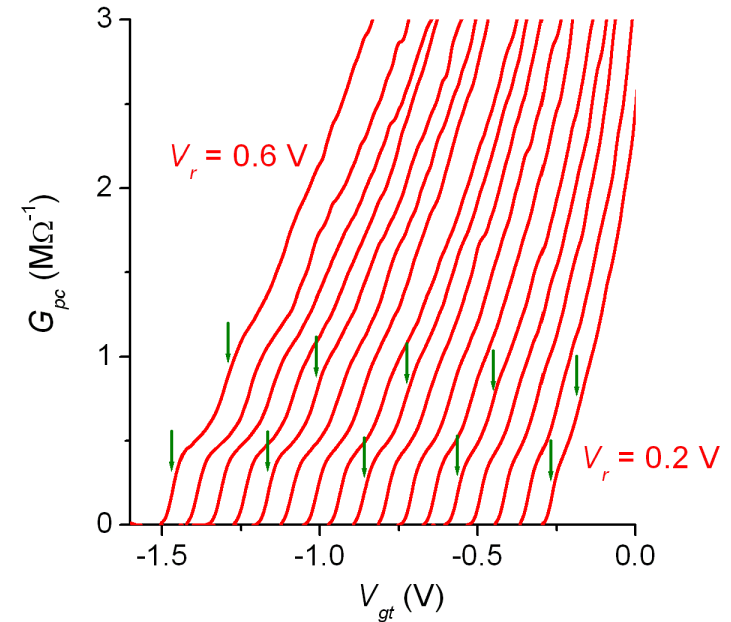
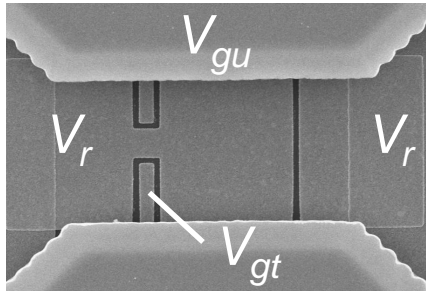
From the simulation, for electrons entering the constriction:

$$\sigma_{\varphi} \sim 1 \text{ meV} \sim V_{in}$$

Molecular dynamics simulations by
M. Araki and H. Hayakawa, Kyoto University:



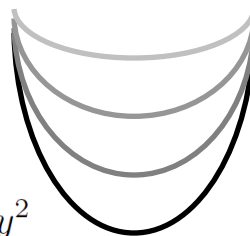
Measure the conductance for different V_r :



For less positive V_r :

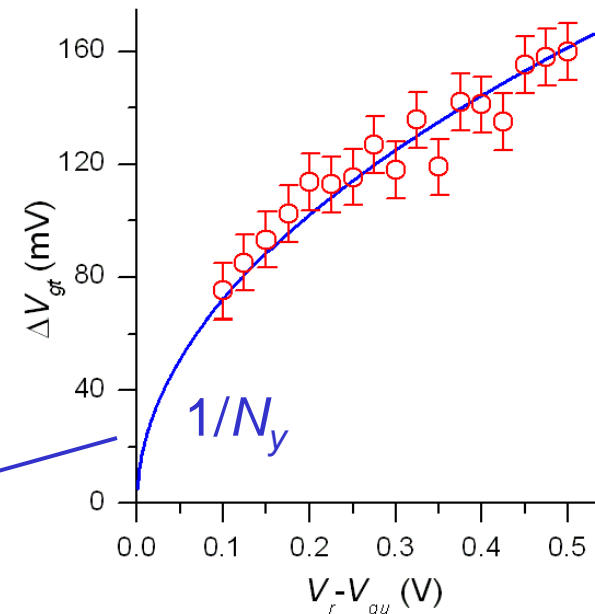
- 1) V_{gt} threshold is less negative
- 2) Step width is smaller

because the parabolic confinement becomes shallower:

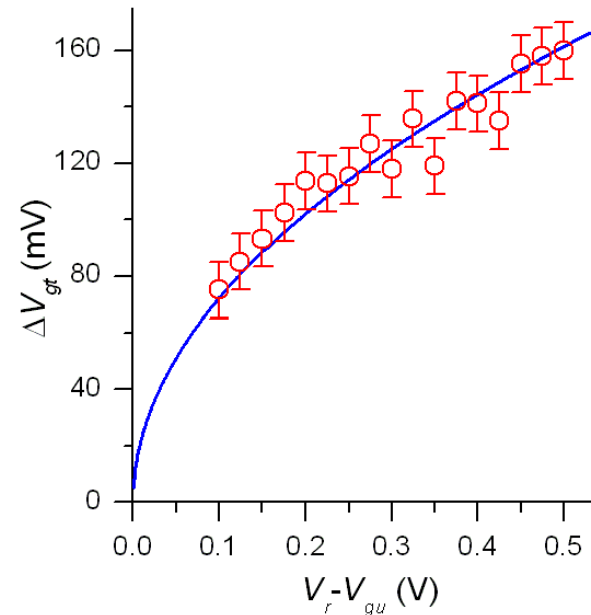
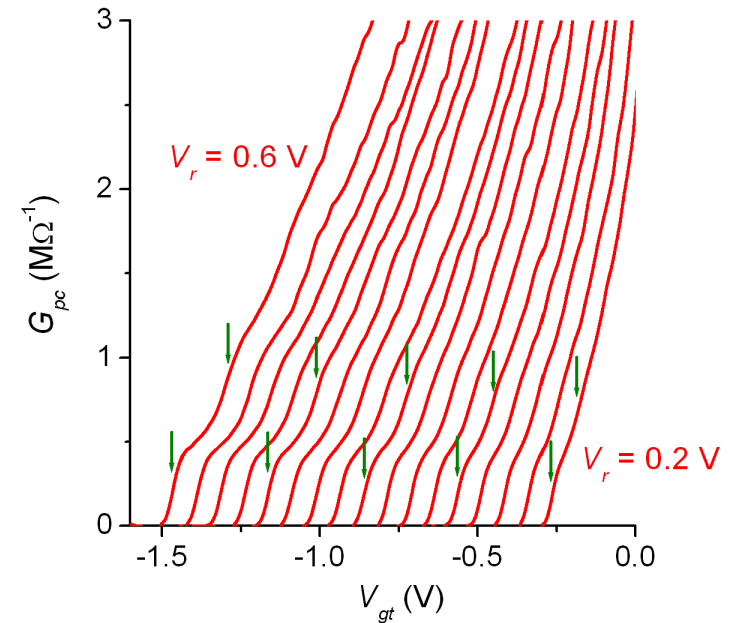


$$V(y) = V_b - \frac{1}{2}by^2$$

$$N_y = \left(\frac{1}{b} \cdot \frac{16\epsilon\epsilon_0}{3ed} \right)^{\frac{1}{2}} \beta(V_{gt} - V_{gt}^{th})$$



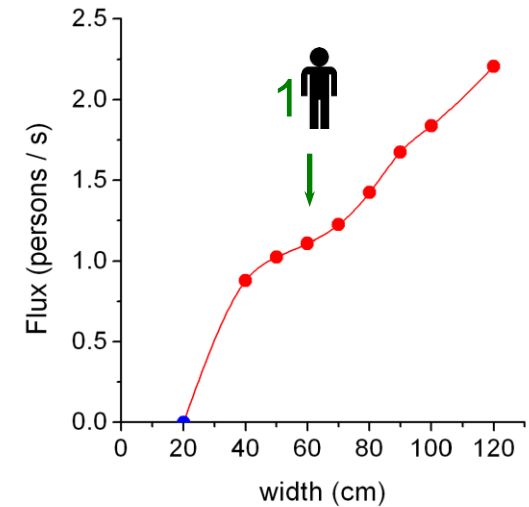
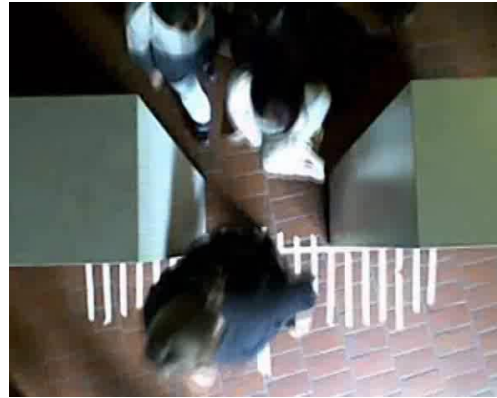
- We have observed a steplike increase in current in the PC device.
- This is due to the increase of the number of electrons able to pass side-by-side through the constriction.
- This can be considered as an effect of Coulomb blockade, at a single constriction.
- Result: A classical analogue of the QPC.
- The same dynamics should be observed in a variety of other systems...



Humans also exhibit
long-range interactions:

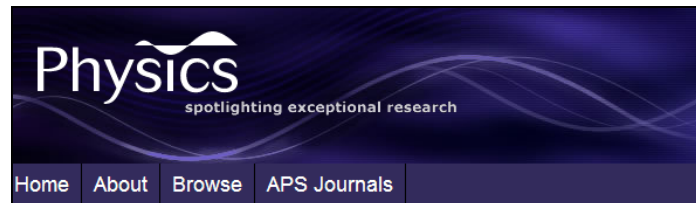
$$\underline{F_{int} \sim e^{-r}}$$

Kretz *et al*, J. Stat. Mech. (2006):



Coulomb systems:

$$\underline{F_{int} \sim 1 / r^2}$$



Focus: Electrons Take Turns Like Pedestrians

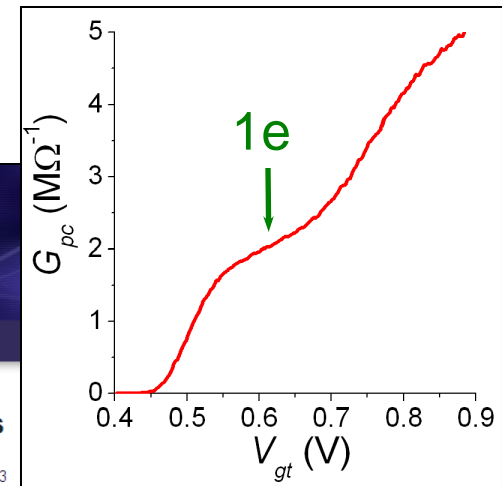
Published January 21, 2011 | *Phys. Rev. Focus* 27, 3 (2011) | DOI: 10.1103/PhysRevFocus.27.3

Electrons confined to a layer floating above liquid helium move in an orderly way through a constriction because their repulsion forces them to keep their distance from one another.

When electrons are put onto liquid helium, they skate like air-hockey pucks above the surface. In the 14 January *Physical Review Letters*, experimentalists report that, when they force a sheet of such electrons through a narrow constriction, the particles' mutual repulsion causes them to take turns passing through, like a crowd of commuters going through a turnstile. The results show how a two-dimensional layer of electrons acts when their quantum nature is not important.

Point-Contact Transport Properties of Strongly Correlated Electrons on Liquid Helium

D. G. Rees, I. Kuroda, C. A. Marrache-Kikuchi, M. Hofer, P. Leiderer, and K. Kono
Phys. Rev. Lett. **106**, 026803 (2011)
Published January 14, 2011

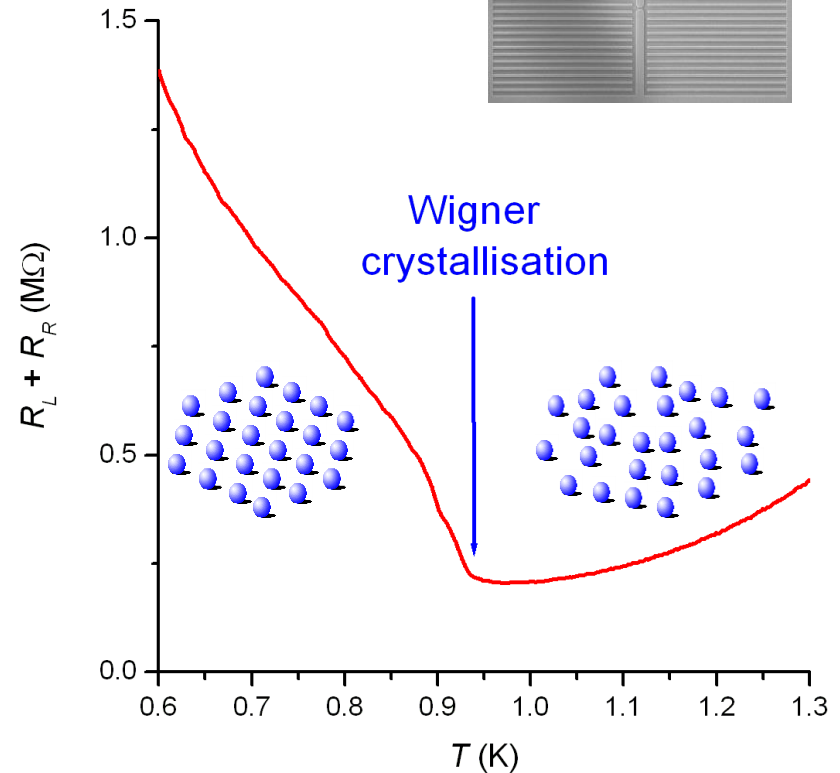
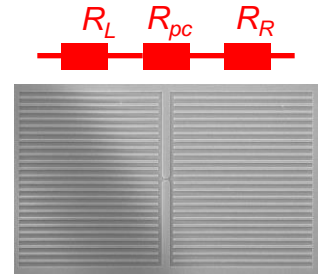
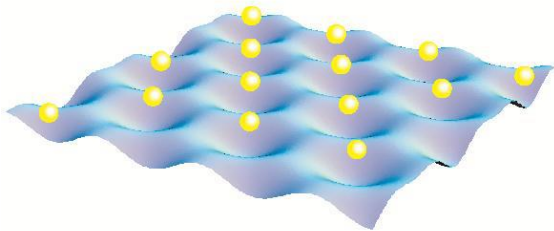


The electron system 'freezes' for $\Gamma > 130$:

$$\Gamma = \frac{E_{\text{Coulomb}}}{E_{\text{kinetic}}} \sim \frac{n_s^{1/2}}{k_B T}$$

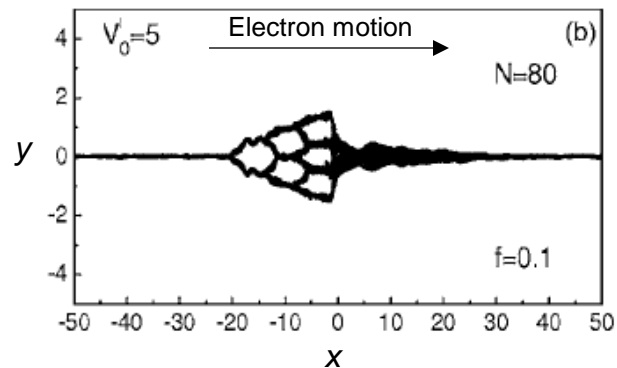
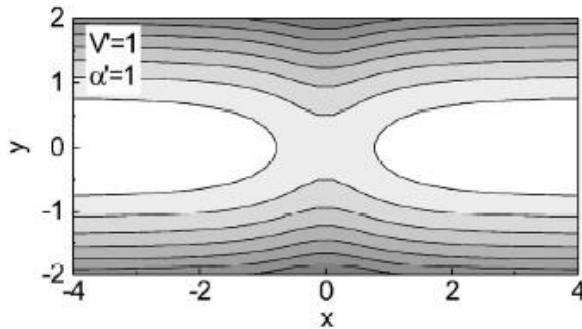
For $n_s \sim 10^9 \text{ cm}^{-2}$, $T_m \sim 1 \text{ K}$

'Dimples' formed beneath each electron increase resistivity:



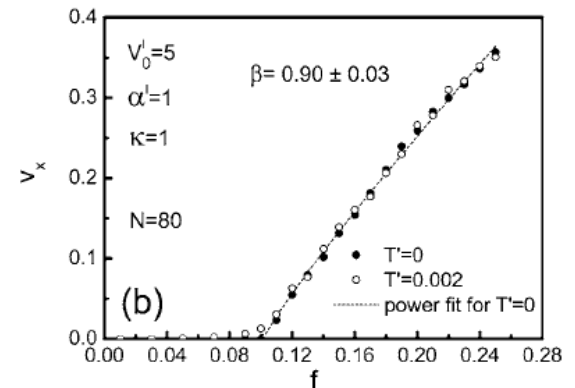
Simulations of Wigner crystal transport through constrictions:

- Piacente and Peeters, PRB **72** (2005):

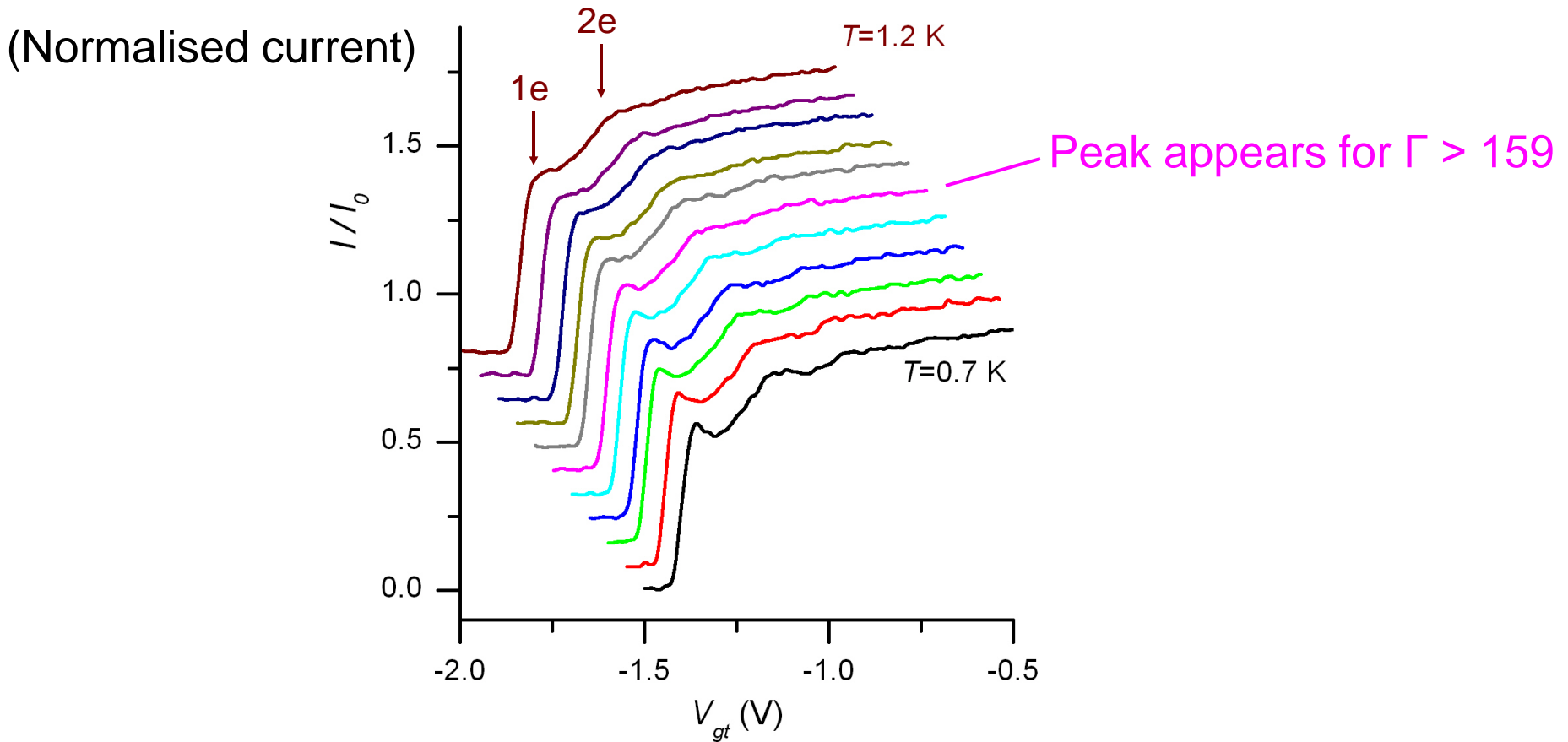


At low temperatures we expect the system to become **pinned** at the constriction.

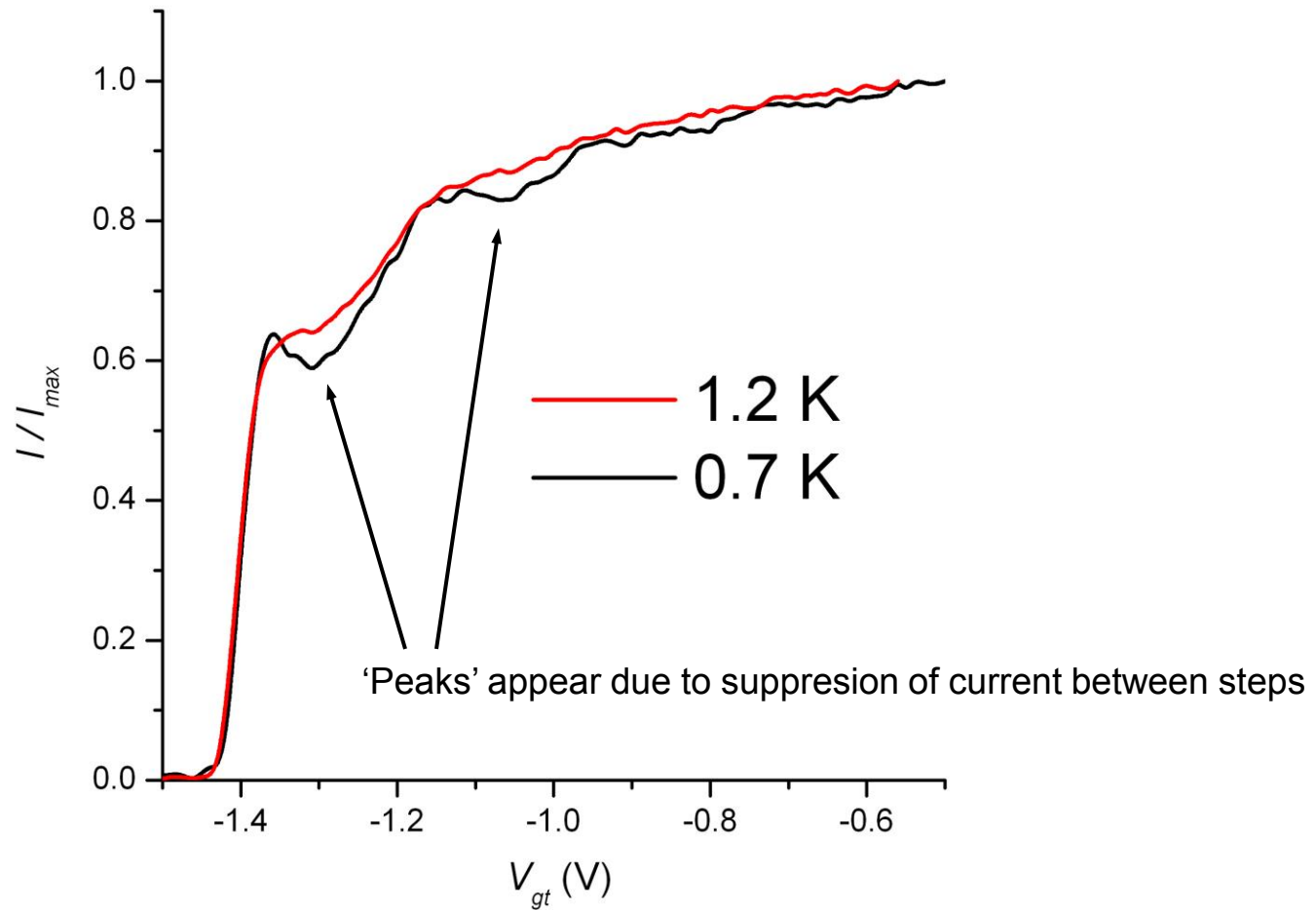
Motion can be induced by increasing the **force** applied to the system (depinning):



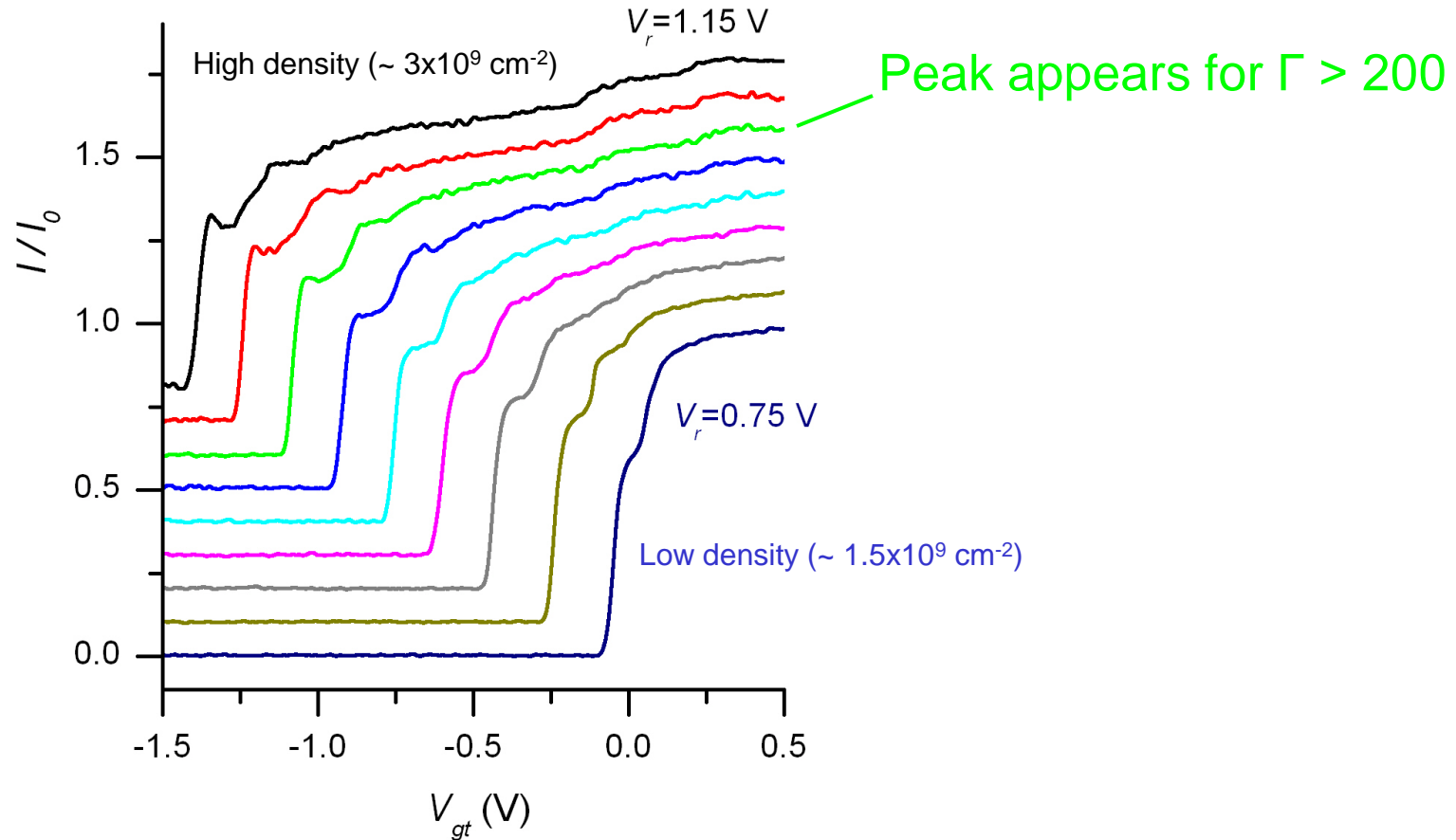
Change temperature (here $T_m = 1.19$ K):



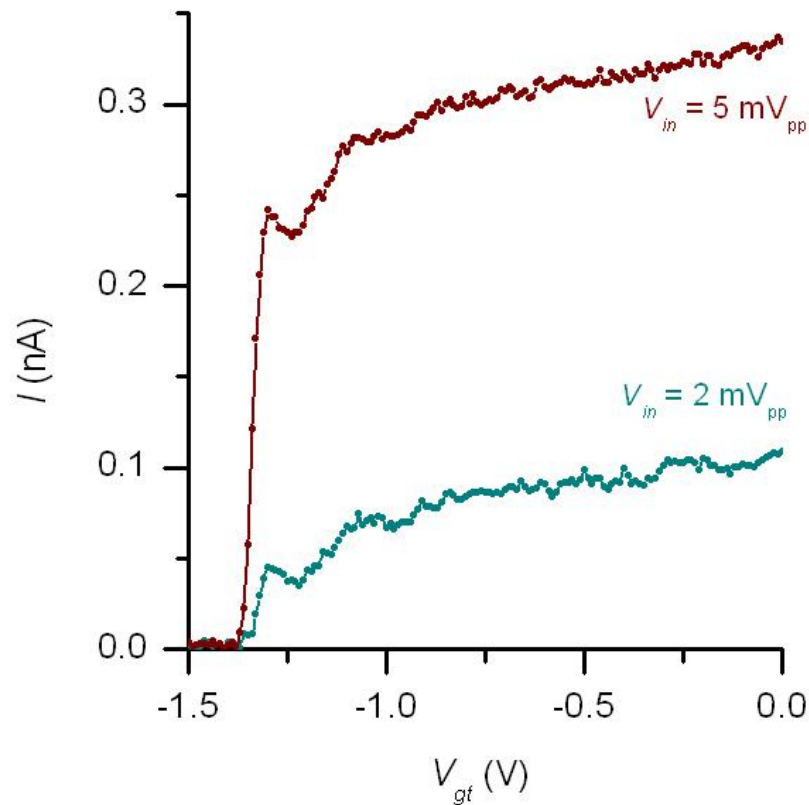
Compare high and low T sweeps directly:



Change density ($T = 0.7$ K):



Change driving voltage ($T = 0.5$ K):



$I_0 \sim 325$ pA

For 5 mV_{pp}, I_0 is similar to that at 1.2 K, 2 mV_{pp}... but the peak is still visible:

The peaks do not appear simply by changing the current.

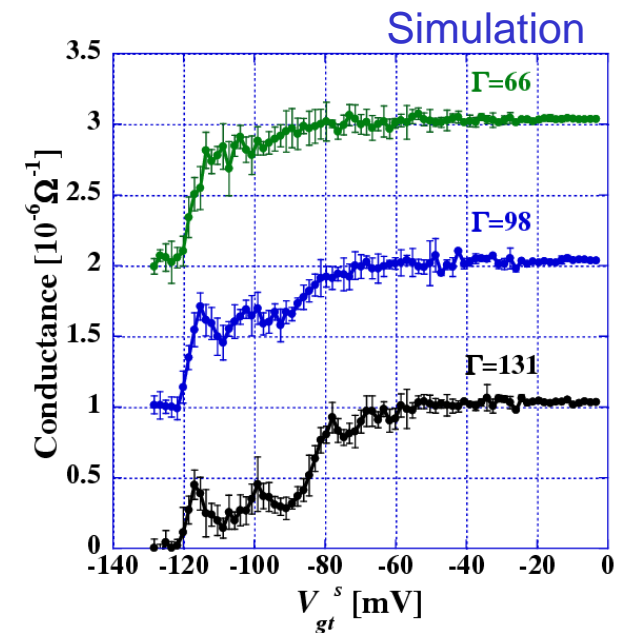
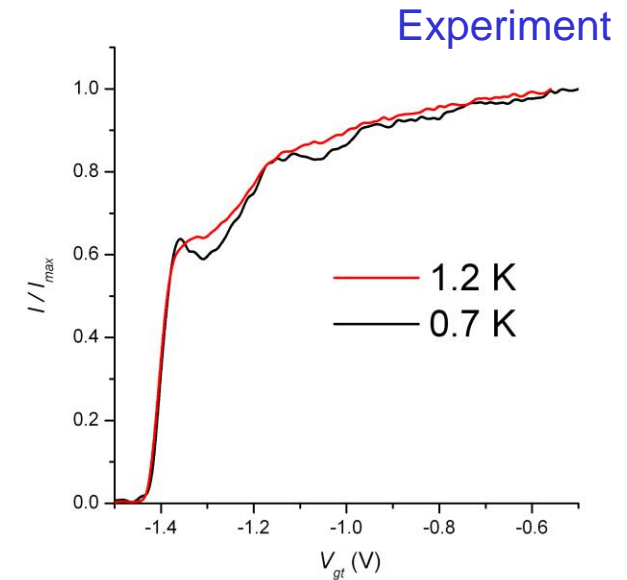
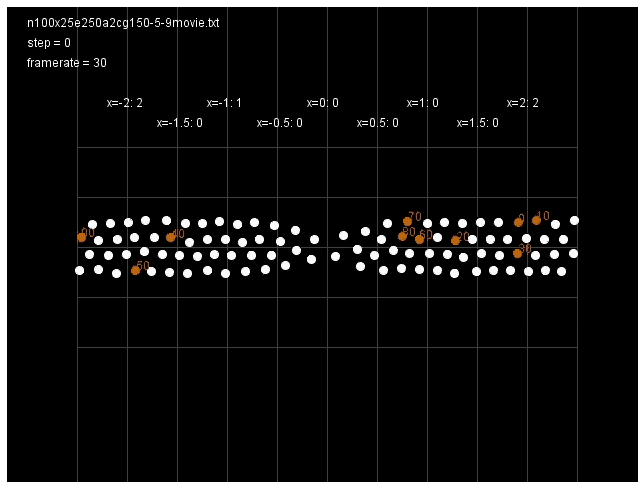
Molecular dynamics simulations (H. Totsuji):

$$H = \sum_i \frac{1}{2} m \left(\frac{dR_i}{dt} \right)^2 + \sum_{i>j} \frac{e^2}{|R_i - R_j|} + \sum_i V_{ext}(R_i)$$

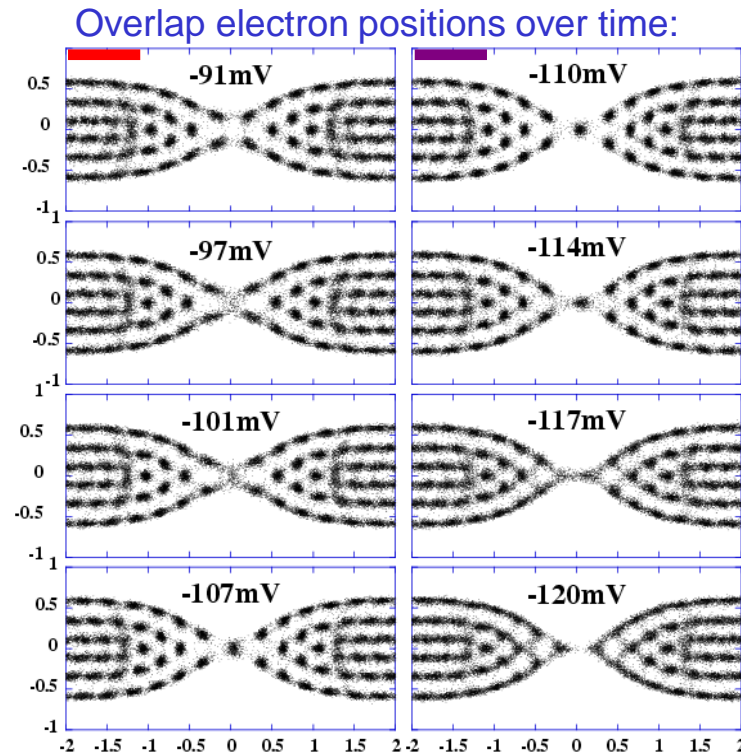
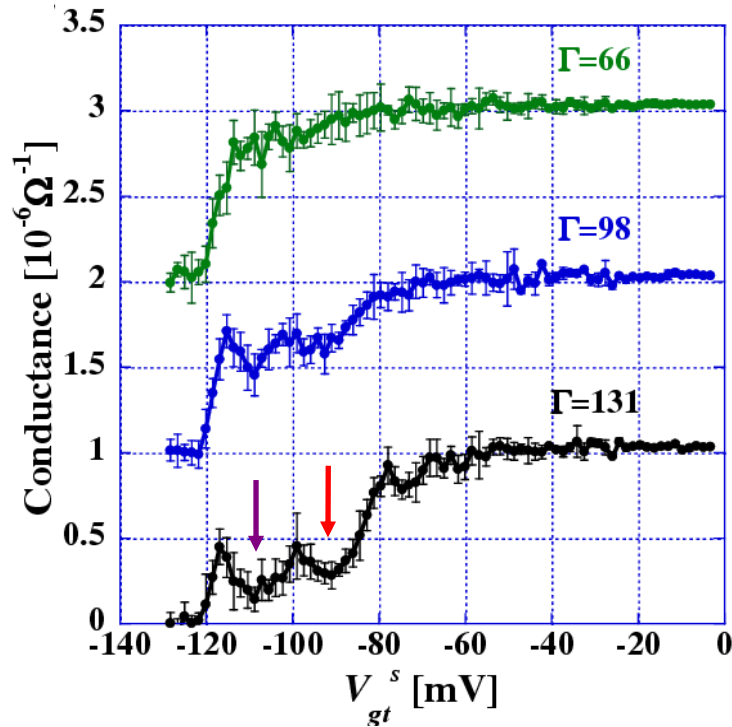
where

$$V_{ext} = V_{gu} \tanh\left(\frac{y^2}{l_0^2}\right) + V_{gt} \frac{1}{1 + (\alpha x/l_0)^2}$$

$$n_s = 3 \times 10^9 \text{ cm}^{-2} :$$

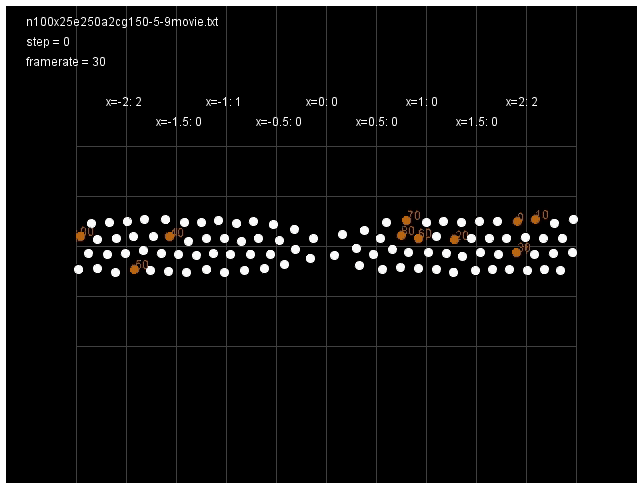


Current is suppressed for symmetric, stable configurations:

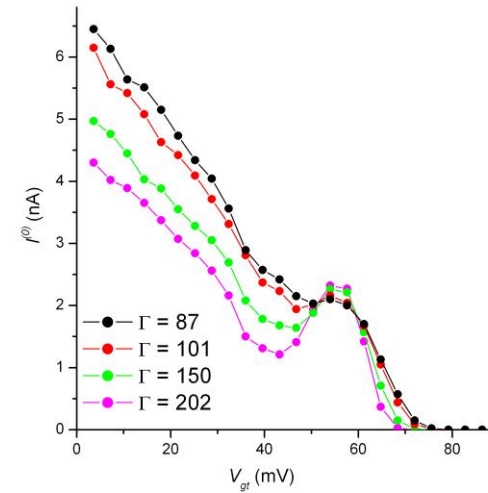


Current suppression
↓
Current grows
↓
Current peak
↓
Current suppression

Note: These pictures are also valid without the applied driving voltage...

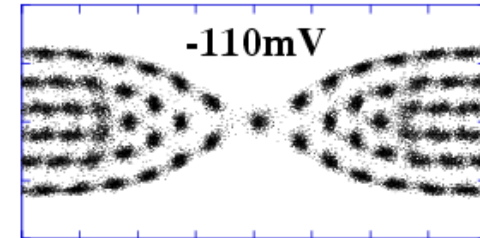


Fluctuation current $I^{(0)}$:



There is a link between the thermal fluctuations in electron positions and the conductance through the constriction...

So: When particles are arranged in a commensurate way at the constriction we observe a suppression of electron thermal motion:



For this case, the fluctuation current is suppressed.

Fluctuation dissipation theorem:

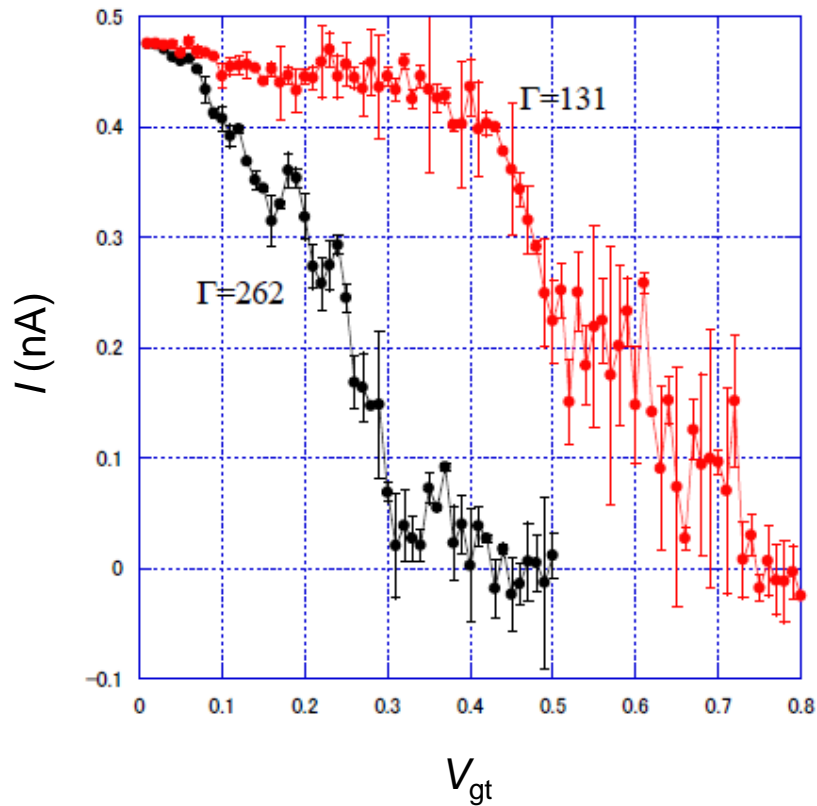
‘The response of a system in thermodynamic equilibrium to a small applied force is the same as its response to a spontaneous fluctuation.’

eg R. Kubo, *Rep. Prog. Phys.* **29** (1966)

So our current is suppressed due to Coulomb interactions...

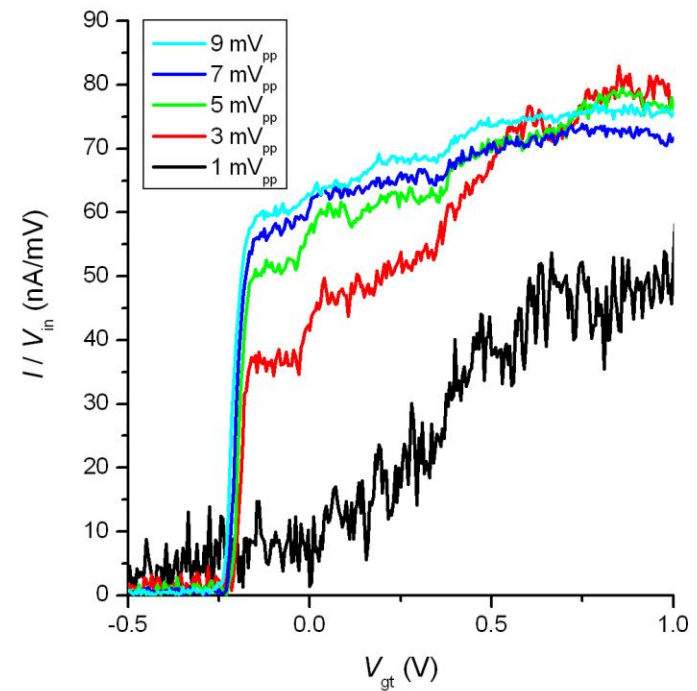
The suppression of current can be regarded as the onset of **pinning**, which depends on the **commensurability** of the electron lattice.

Preliminary simulation data:



Preliminary experimental data:

$T = 440$ mK:



Signs of strong suppression at low T , but further measurements required...

- We have measured the transport properties of classical electron liquids and solids in a point-contact device.
- In the liquid phase:
 - We observe **conductance steps** due to lane formation.
- In the solid phase:
 - We observe **conductance peaks** due to the onset of pinning for commensurate electron lattice arrangements.
- In the next talk we will see related conductance oscillations in a long microchannel, but due to **ripplon scattering**.
- The dynamics revealed here could be observable in many other **classical many-body systems** (colloids, grains, pedestrians etc...)
- Good agreement with simulations shows that e on He are a useful **model system** for the study of many-body systems in confined geometry.

