

# ***Non equilibrium transport In ultra clean systems***

**A.D. Chepelianskii**

**Experiments on surface electrons :**

**D. Konstantinov, K. Kono**

**Experiments in Orsay :**

**J.Laidet, H. Bouchiat**

**groupe de physique mesoscopique**

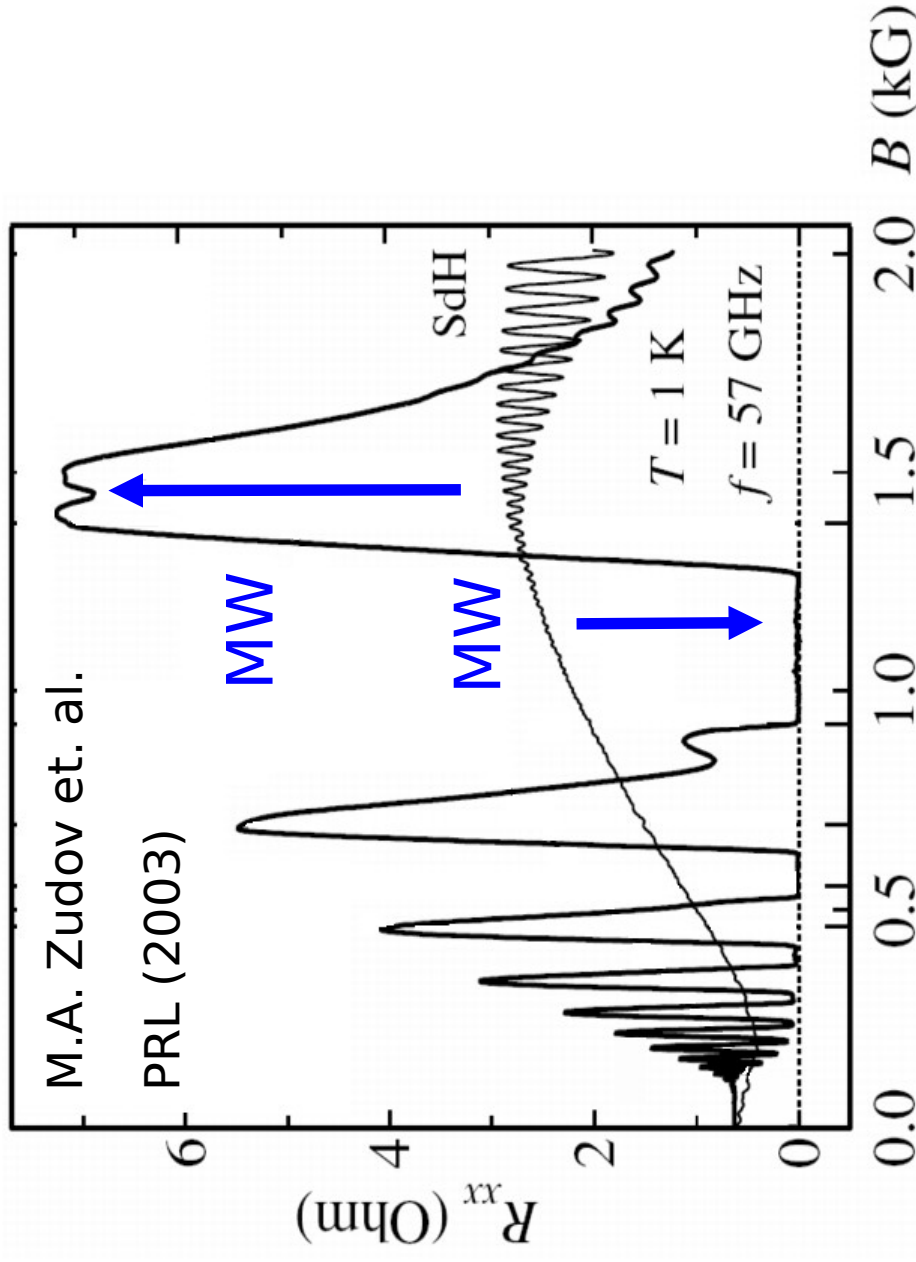
**Theory: D.L. Shepelyansky**

**Experiments in Cambridge :**

**A. Brewer, I. Farrer, H.E Beere, D.A. Ritchie  
R.H Friend**

# Microwave induced zero-resistance states

- R.G. Mani et al. (2002) and M.A. Zudov et. al. (2003)
- Complete suppression of  $R_{xx}$  under irradiation at 1 kGauss



Position of zeros determined by  $\omega / \omega_c$  ;  $\omega_c$  cyclotron frequency

## Existing theories :

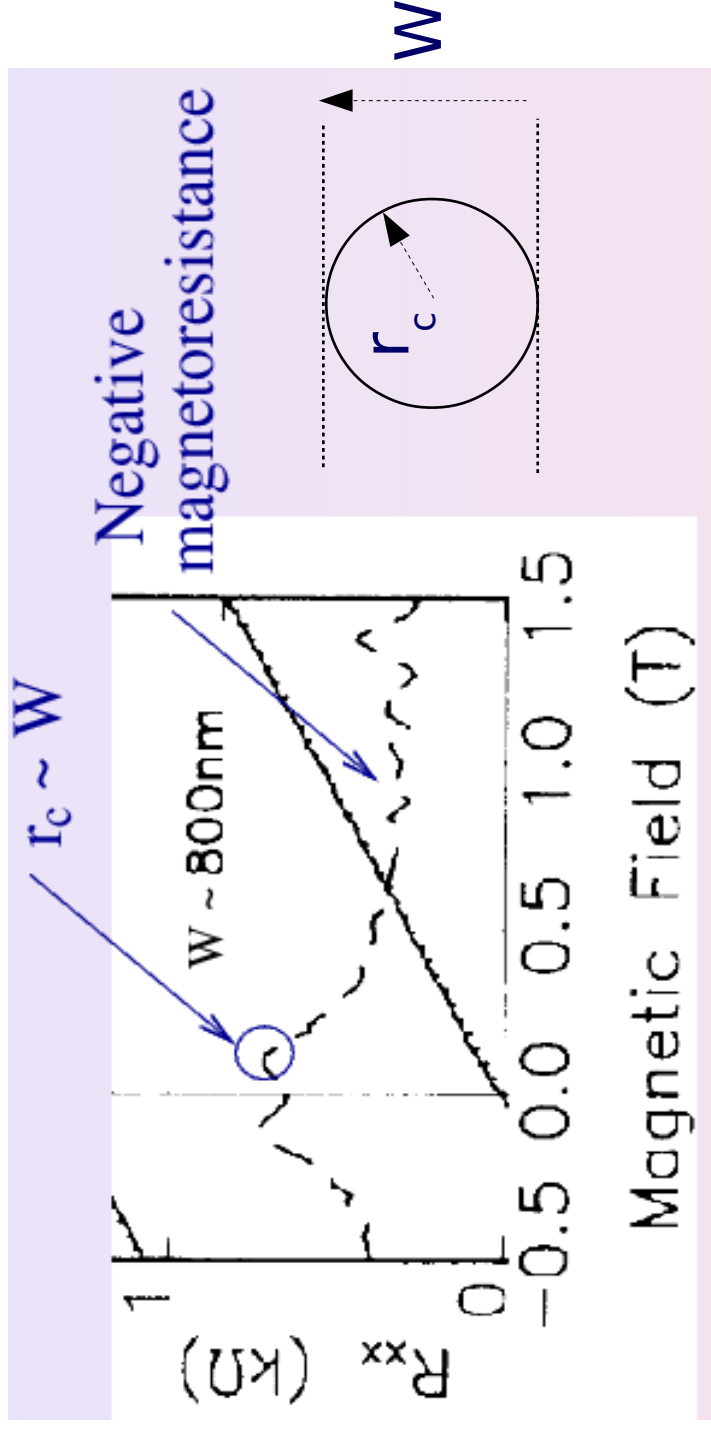
- Most developed theory (elastic/inelastic) :  
negative resistance & domains theory  
outstanding contributors in the audience
- J. Inarrea theory (a bulk theory as well)
- Microwave effect on edge channels (“home” theory)
- Microwave effect on contact regions ! S.A. Mikhailov (2011)

**Bulk transport/edges/contacts ...**

**All possibilities offered by Solid State physics were tried !**

# Commensurably effects in transport

When the Larmor Radius  $r_c$  is commensurable with the channel width  $W$  magneto-transport changes



- Peaks when  $r_c \sim W$

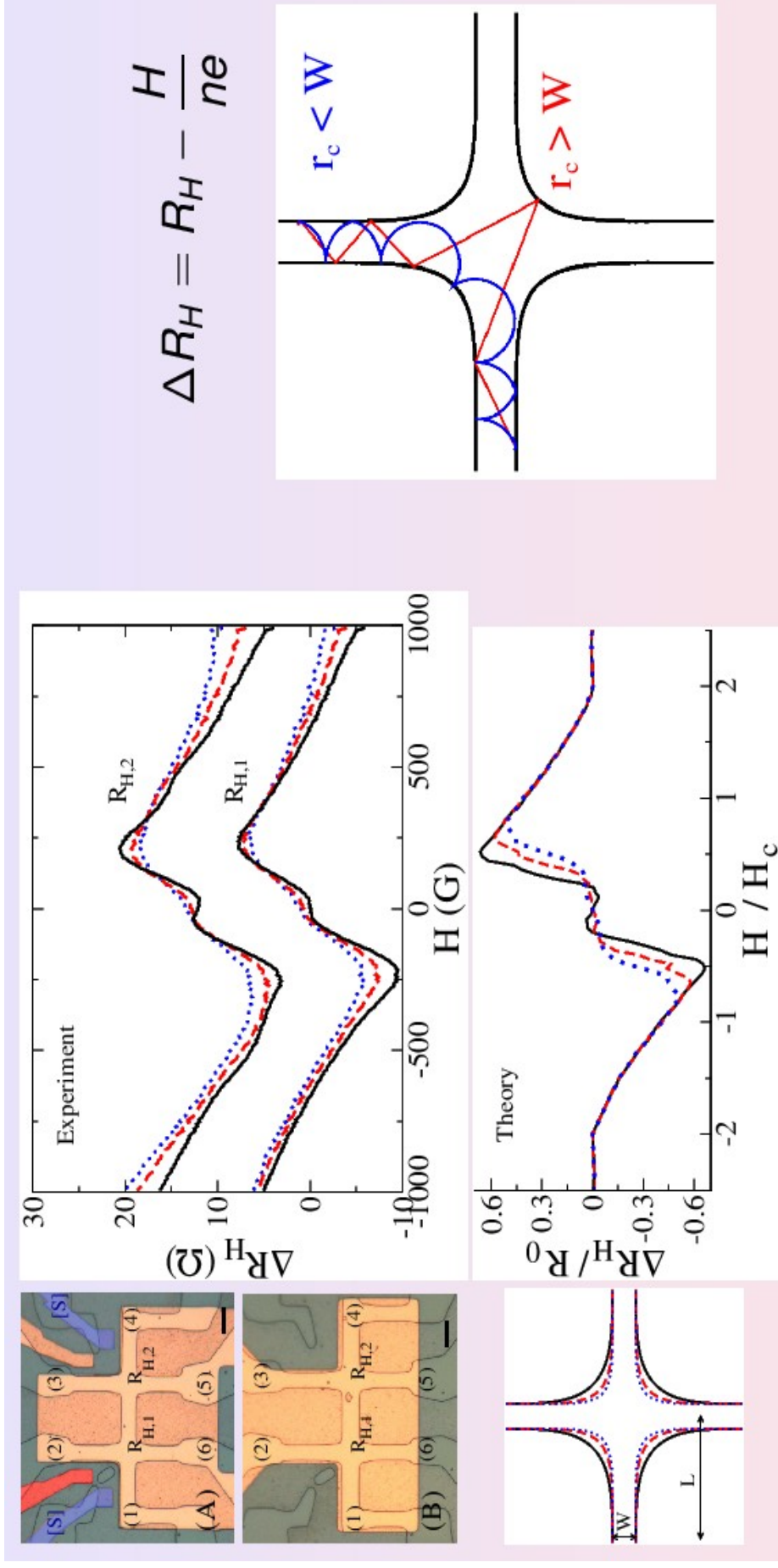
- Suppression of  $R_{xx}$  when  $r_c < W$

M.L. Roukes et. al. PRL 1987

# Understanding using a billiard model

- Determine Hall resistance  $R_H$ ,  $R_{xx}$  from the classical

Transmission probabilities from one contact to another



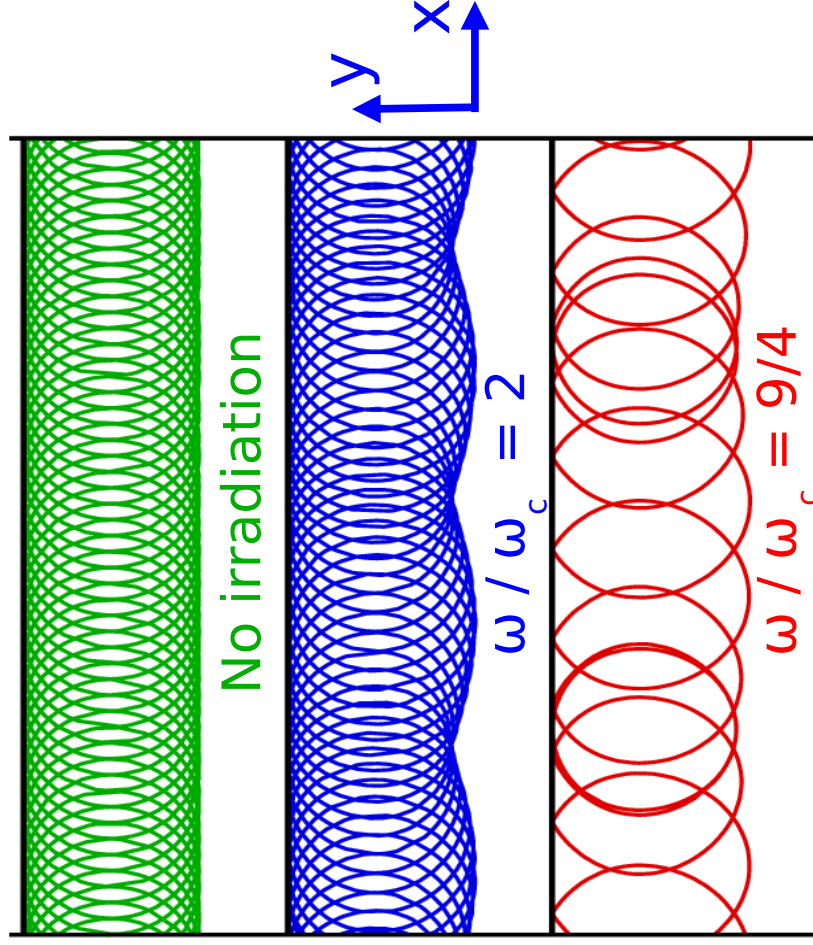
Billiard model C.W. Beenakker et. al. PRL 1989; Experiments A.C. PRL 2009

If guiding becomes perfect  $R_{xx} \rightarrow 0$  !?

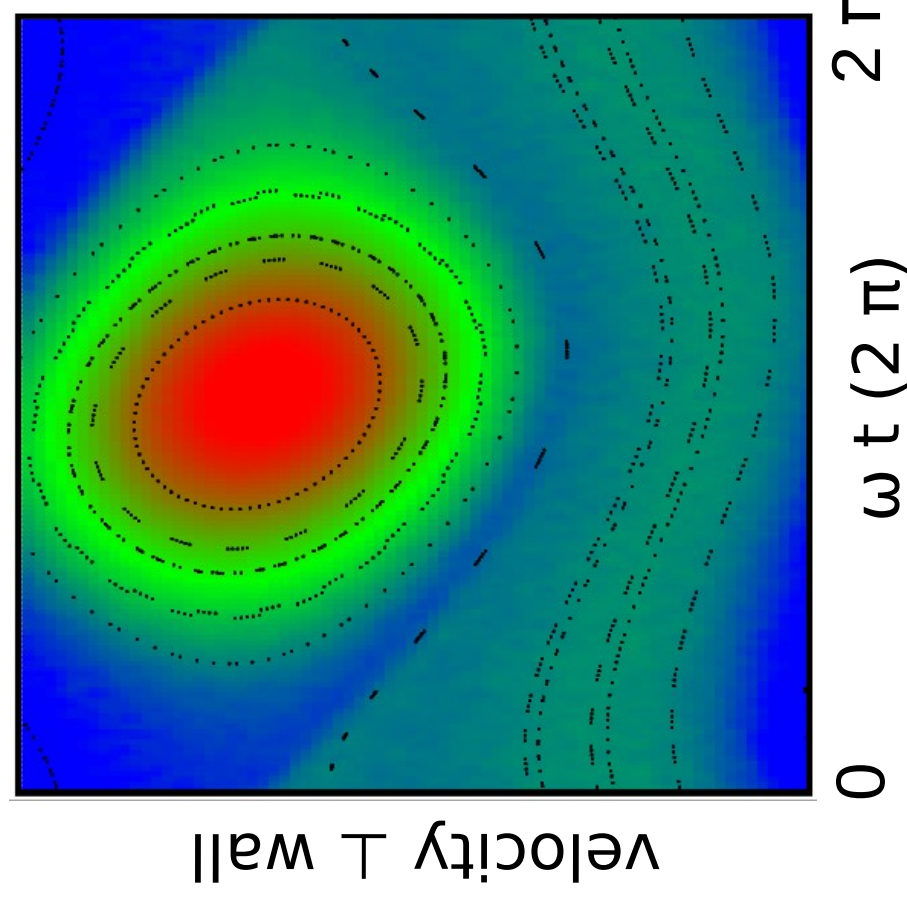
# Theory : Microwave stabilization of edge transport

- Non linear resonance under microwave irradiation
- With dissipation  $\rightarrow$  attractor and trapping

Trajectories in (x,y) plane



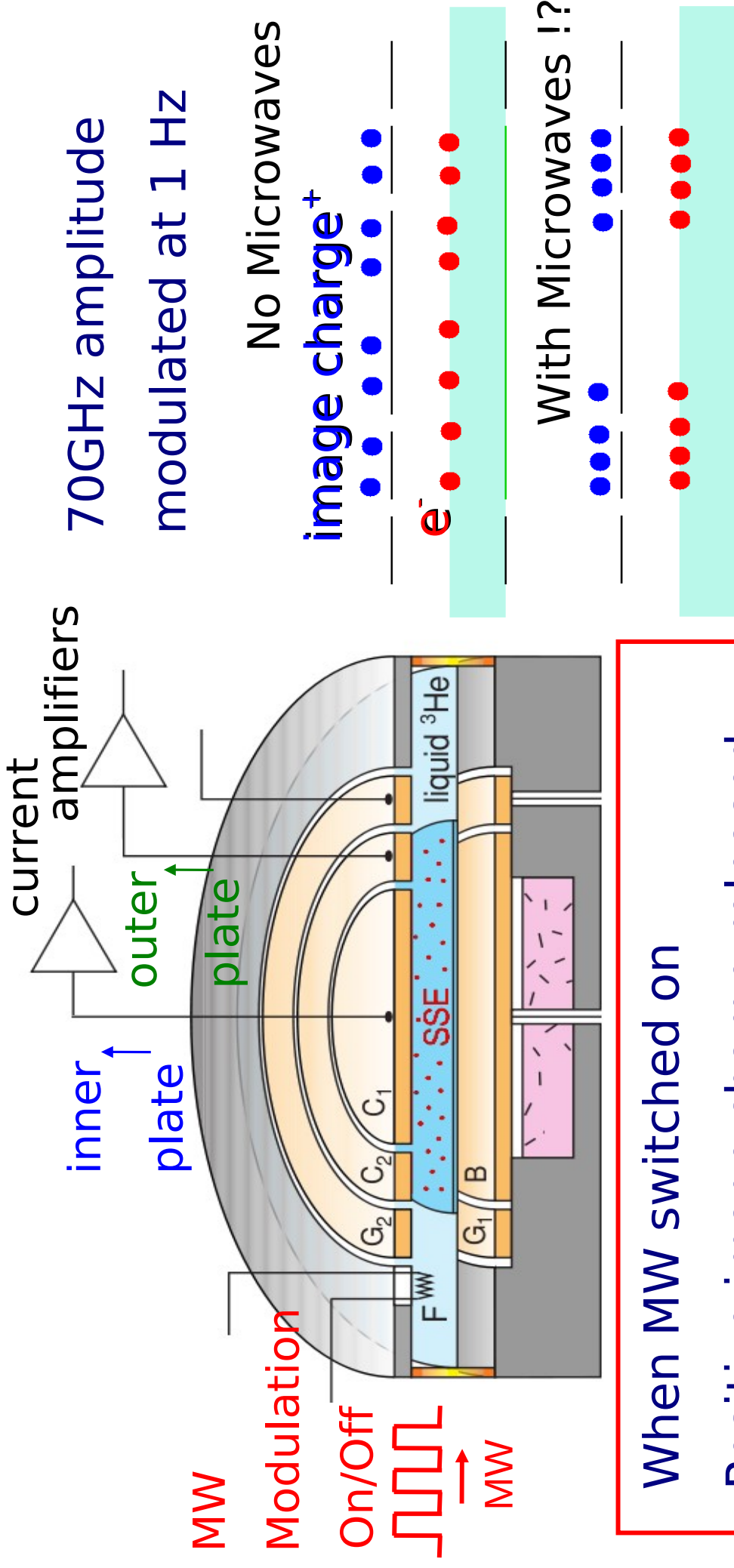
Chirikov standard map



# How to detect trapping at the edge ?

Modulate the microwave power without external bias !

Detect transient currents due to motion of image charge



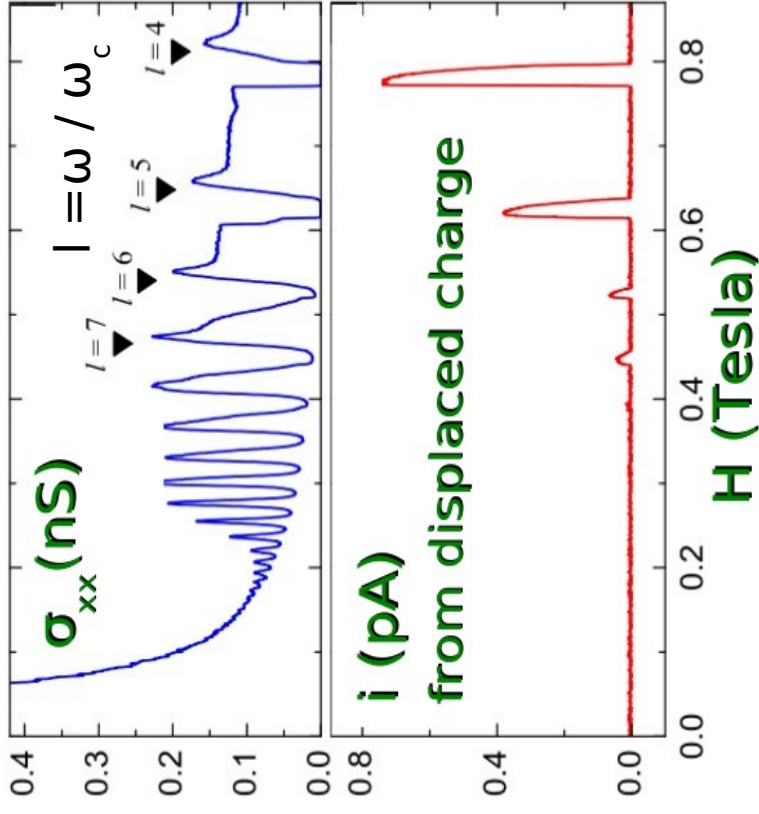
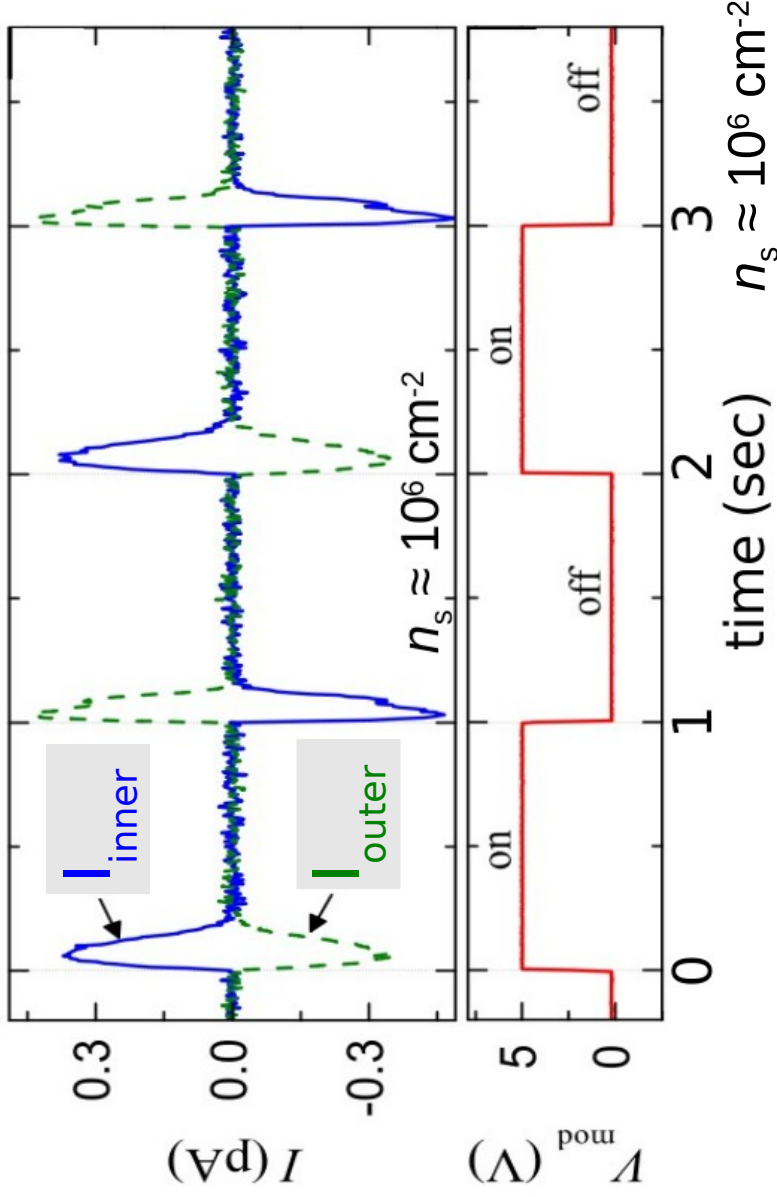
When MW switched on

Positive image charge released

Positive inner transient current

# Transient radial currents !

Under the experimental conditions for ZRS  
current from inner to outer plate when MW ON

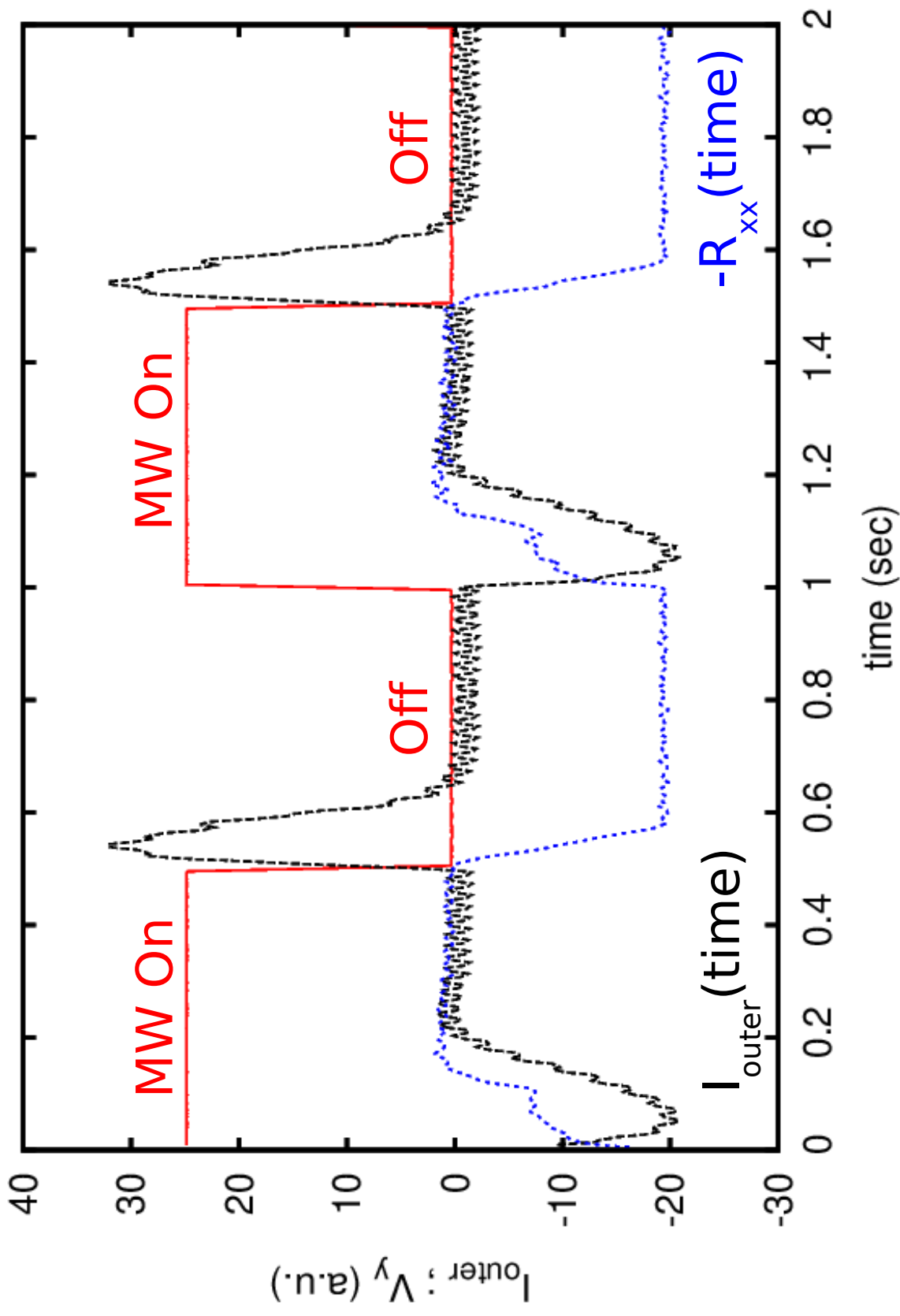


Large fraction of electrons (20 to 100%) move to the edge

Demonstration of trapping at the edges !

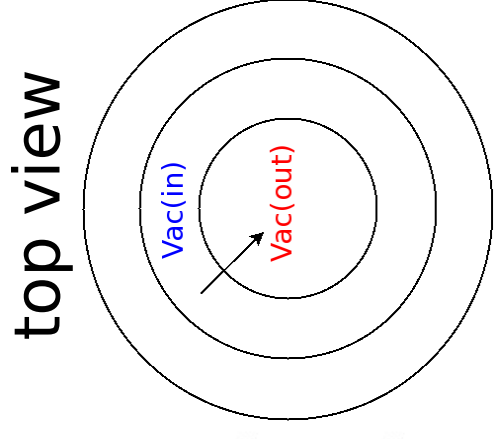
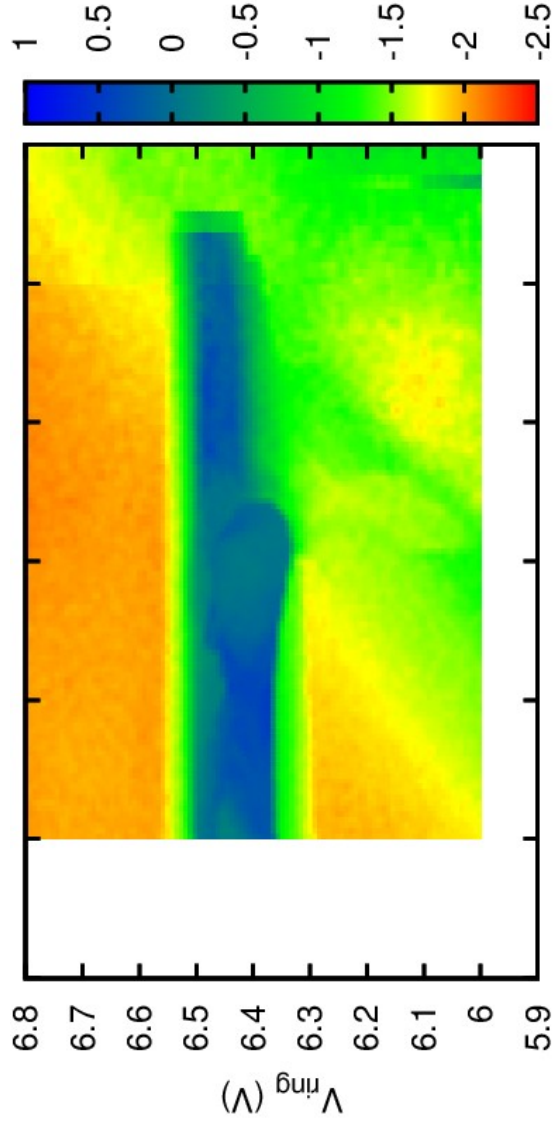


# Transient conductivity measurements

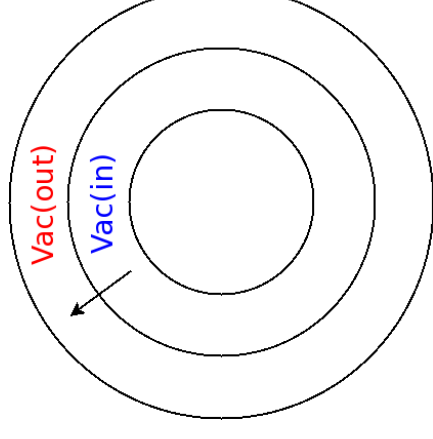
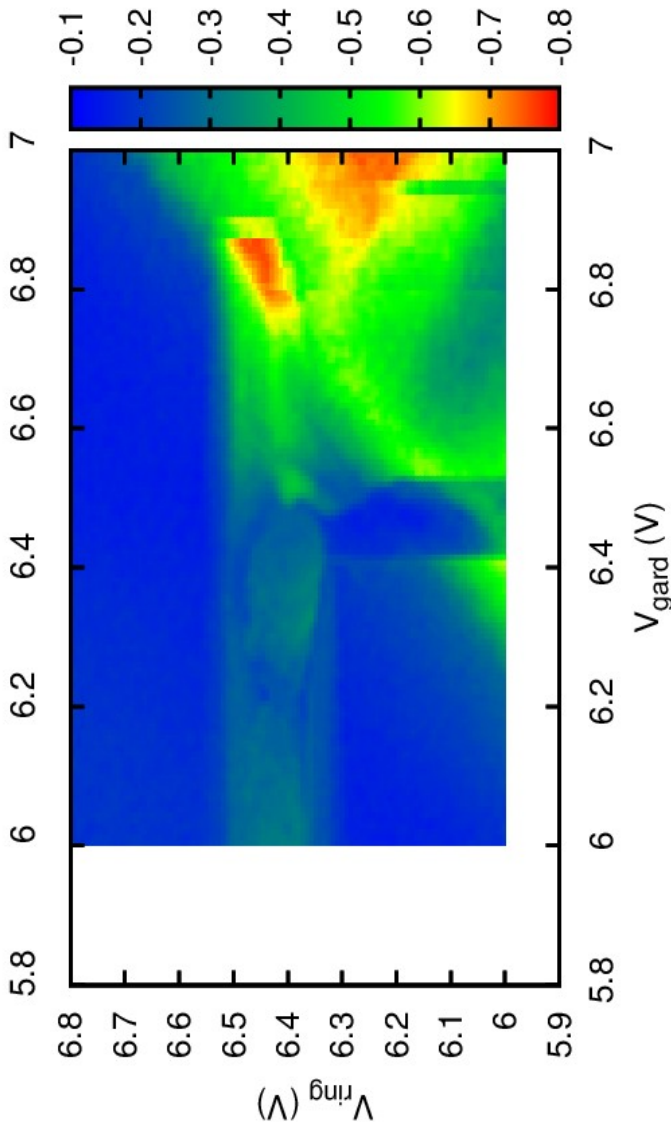
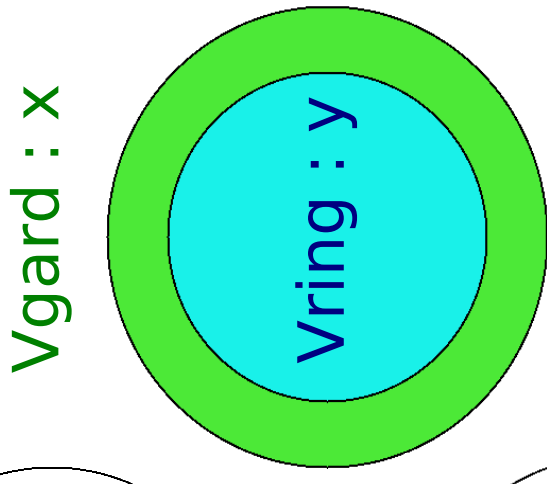


Zero resistance appears only when the charge redistribution is completed

# First indirect measurements



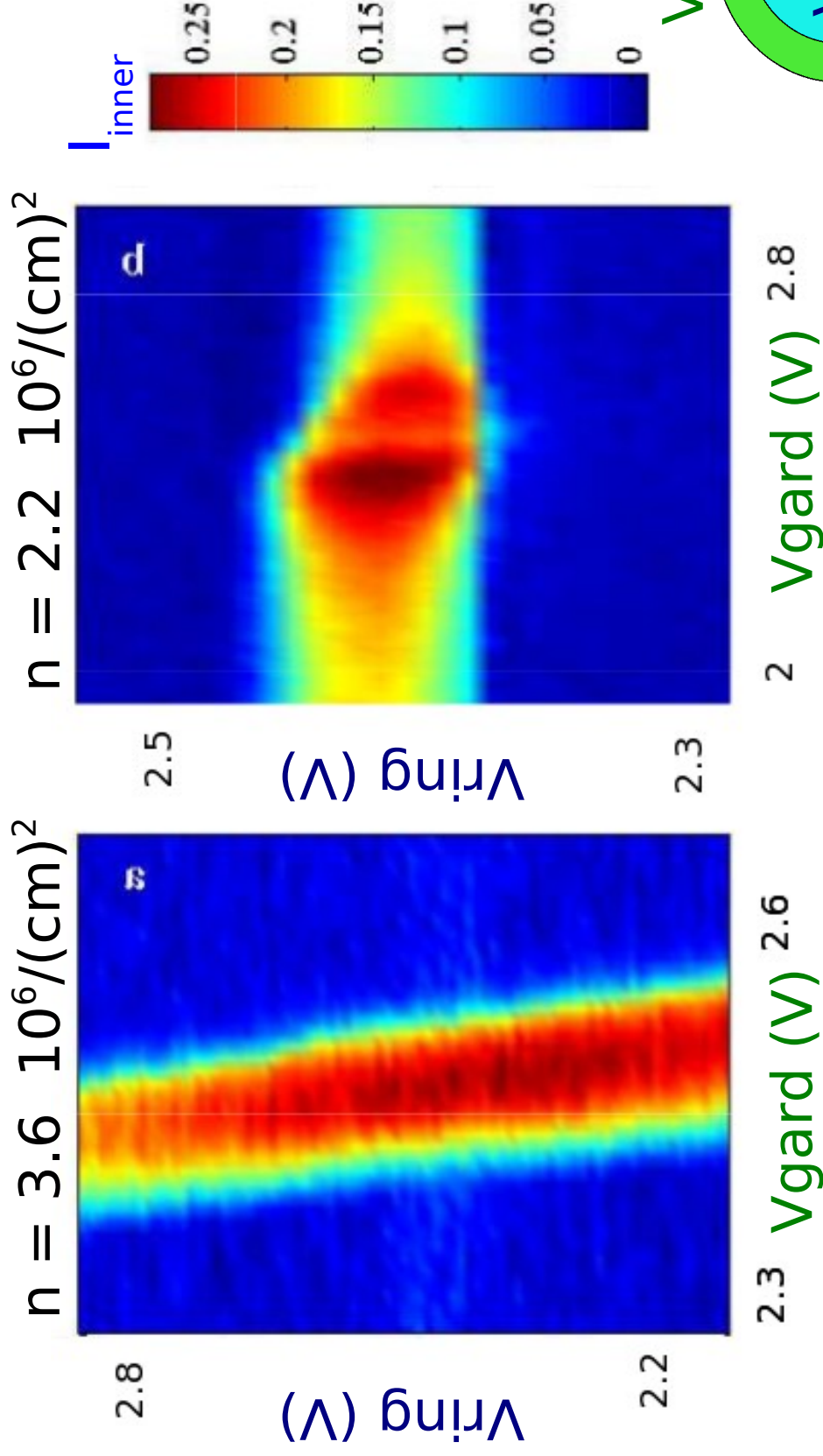
bottom  
view



Zero resistance in the center but not at the edge !

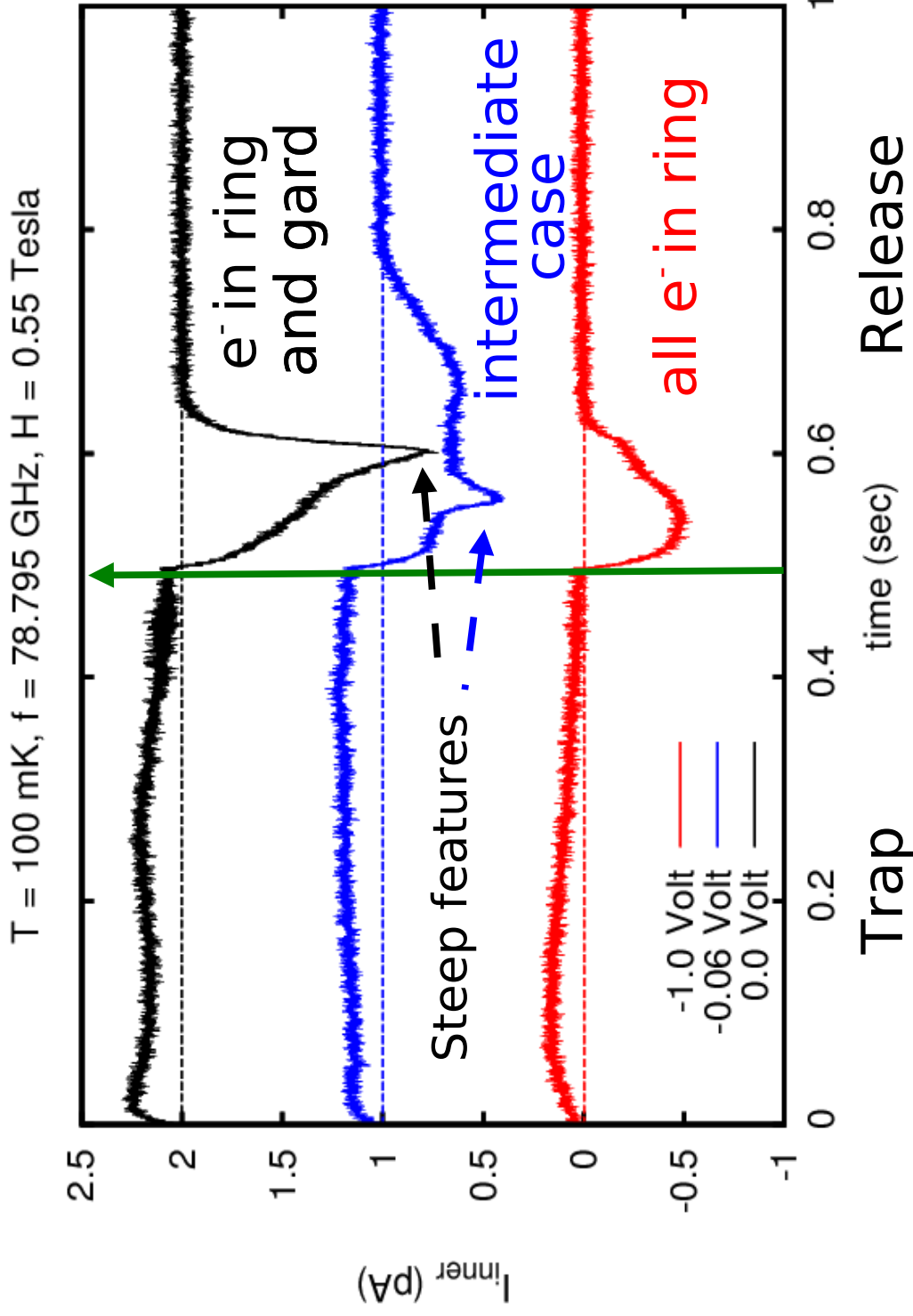
# Local resonant excitation

Since electrons are trapped at the edge, do we really need resonant excitation in the center ?



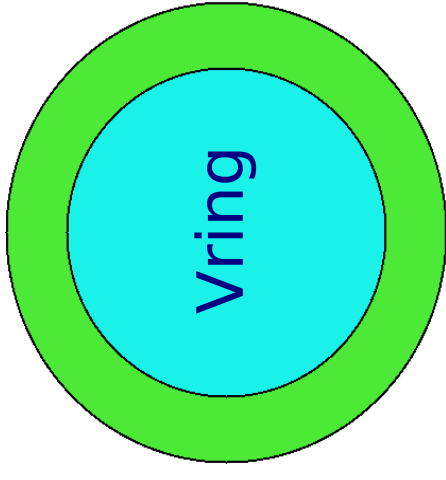
Not at "high" electron densities !

# Reconstruction of the density profile from the decay kinetics ?



Change  
 $V_{\text{gard}} - V_{\text{ring}}$

$V_{\text{gard}}$



Indications of a steep density distribution ?

# Multi-photon absorption

High repulsion energy per trapped  $e^- \sim 1\text{eV}$

Conservation of energy : many  $0.4\text{meV}$  photons per  $e^-$

Model Hamiltonian (at short times) :

$$\hat{H} = \hbar\omega_c(\hat{a}^\dagger\hat{a} + \frac{1}{2}) + \sum_k \epsilon_k |k\rangle\langle k| + \hat{H}_{angle} + \hat{W} + \hat{H}_{ac}(t)$$

Landau levels z levels

$$\hat{H}_{angle} = i\alpha\sqrt{\frac{\hbar m\omega_c^3}{2}} \sum_{k,k'} z_{kk'} (\hat{a} - \hat{a}^\dagger) |k\rangle\langle k'|$$

tilt in the magnetic field

$$\hat{W} = \sum_{l,l';k,k'} W_{l,l';k,k'} |l\rangle\langle l'| \otimes |k\rangle\langle k'|$$

Riptions

$$\hat{H}_{ac}(t) = eE_z \sum_{l,n} z_{ln} |l\rangle\langle n| \cos\omega t + eE_x \sqrt{\frac{\hbar}{2m\omega_c}} (\hat{a} + \hat{a}^\dagger) \cos\omega t$$

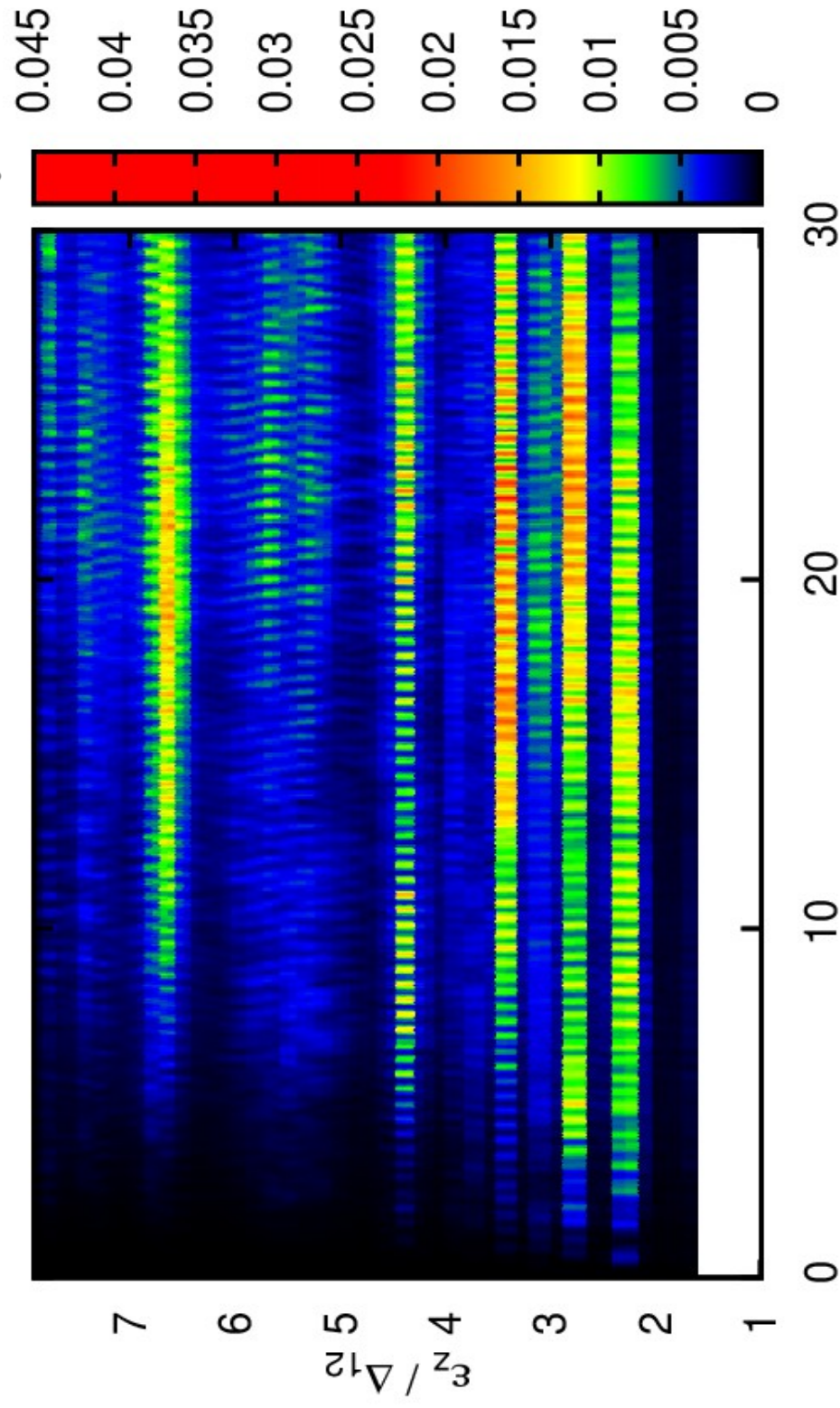
AC driving

$$a = \sqrt{\frac{m\omega_c}{2\hbar}} \left( \hat{x} + \frac{i}{m\omega_c} \hat{p} \right)$$

$z_{ln} = \langle l|z|n\rangle$  dipolar transition elements in the z direction

# Numerical integration of dynamics (1)

$$P(\epsilon_z; t) = \sum_l |\psi(l, n_z; t)|^2$$



$$J = \omega / \omega_c = 6$$

$$\omega = \Delta_{12}^2$$

$$B \sim 0.5 \text{ Tesla}$$

time (ns)

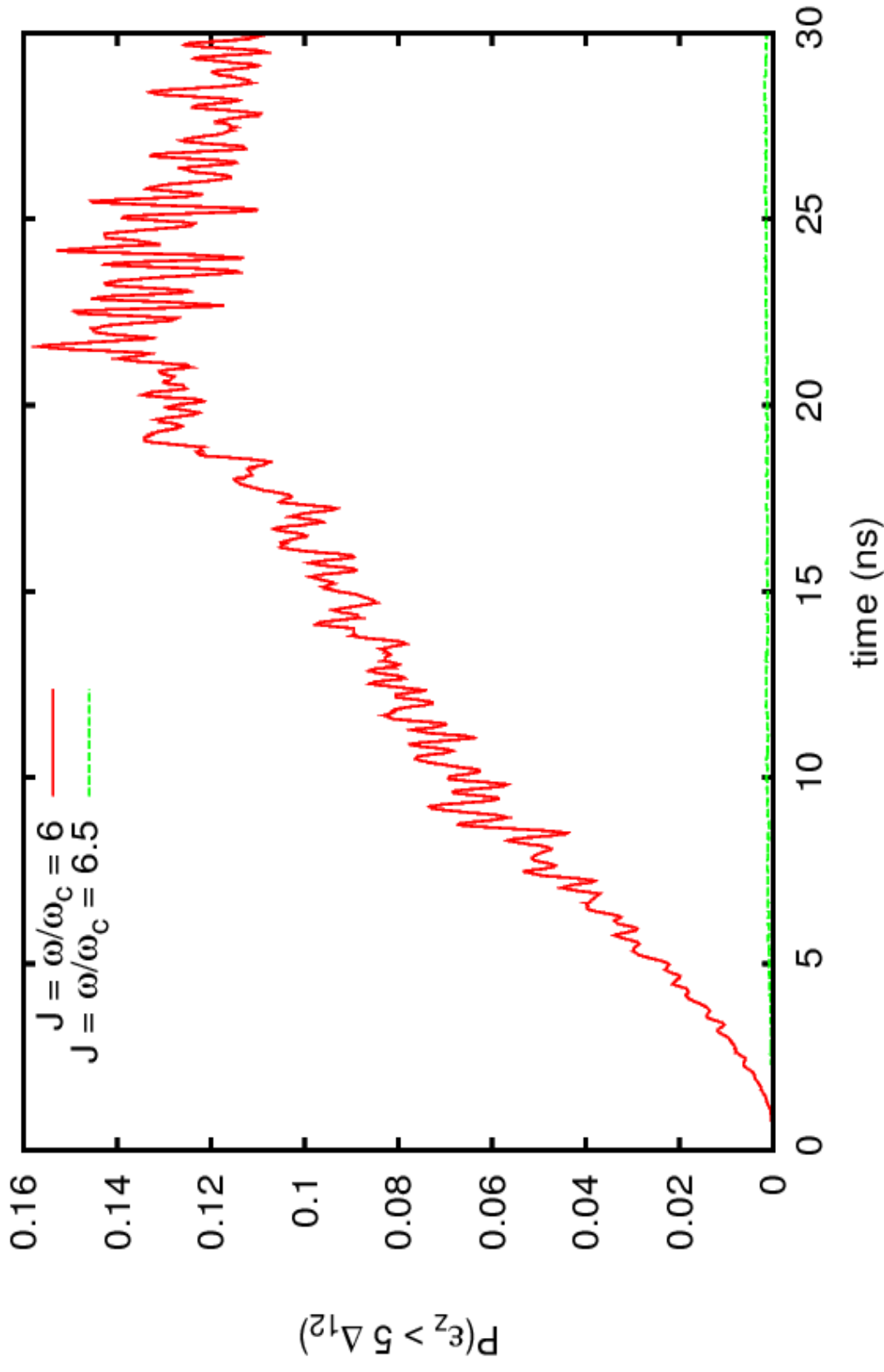
$$E_{z;dc} = 3 \text{ V/mm}$$

$$E_{x;ac} = E_{z;ac} = 1 \text{ V/mm}$$

$$\alpha = 6 \text{ deg}$$

$$W = 0.02 \hbar \omega_c$$

# Numerical integration of dynamics (2)



The highly excited z-states should be very long lived; they are far from the surface

# Summary for e<sup>-</sup> on liquid Helium

In ZRS electrons accumulate on the edge

Repulsion energy per trapped e<sup>-</sup> ~ 1eV

Photon energy ~ 0.4 meV, Temperature ~ 100 mK

Transient conductivity measurements suggest :

e<sup>-</sup> Redistribution → ZRS (and not the other way around!)

At high densities :

Resonant excitation at the edge induces redistribution

Resonant excitation in the center : no effect !

In this story I focused on the first second after turnon off MW,

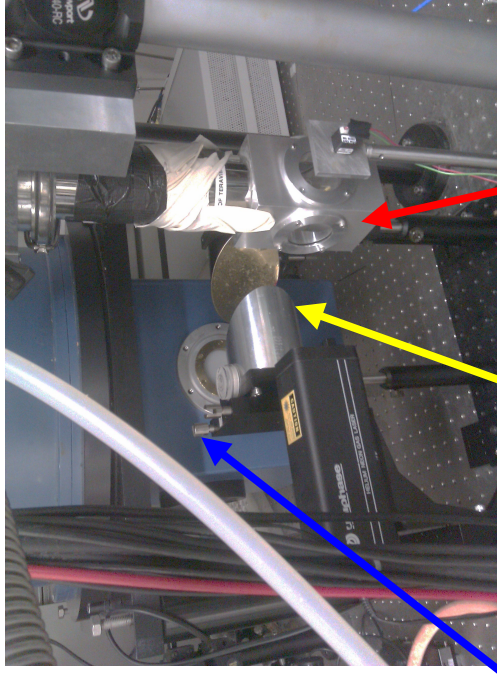
More non trivial effects at later times (but not only)



# “Photo-voltage under THz light

Photo-transport at THz frequencies :

Coupling between a mesoscopic sample  
and a Quantum cascade laser (QCL)



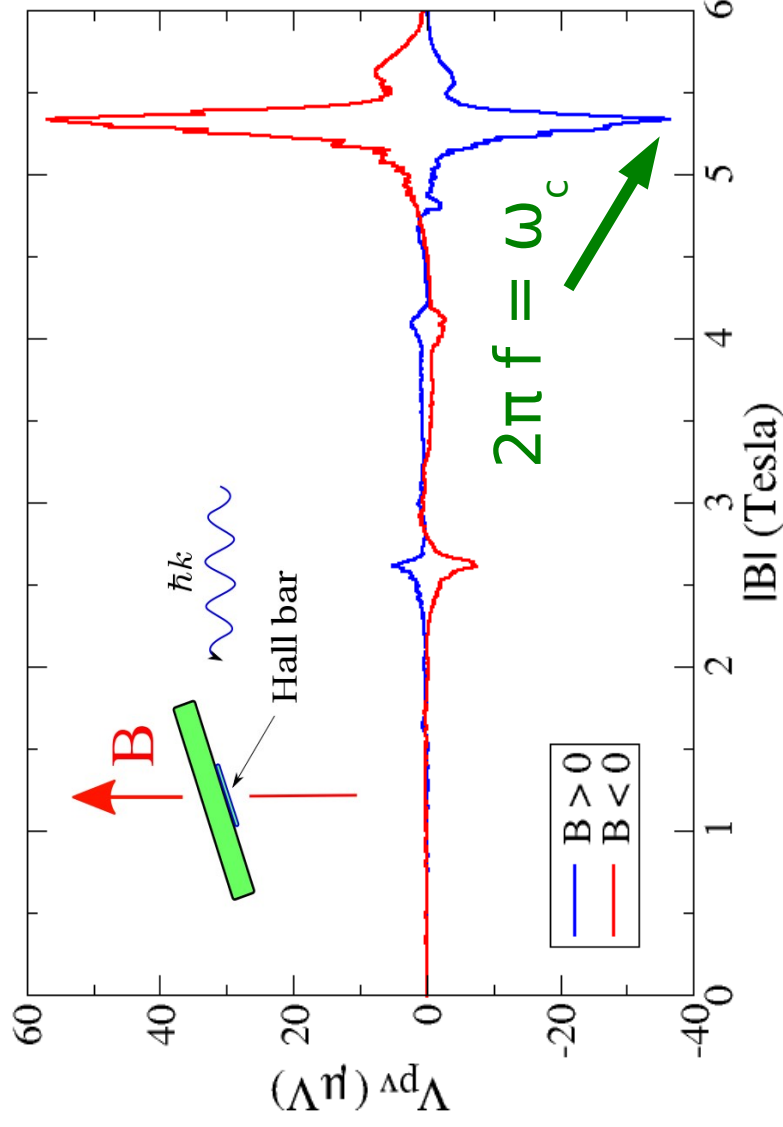
Sample (1K)  
Parabolic mirrors  
QCL (10K)

Photovoltage across  
ultra-high mobility

Hall bar under irradiation

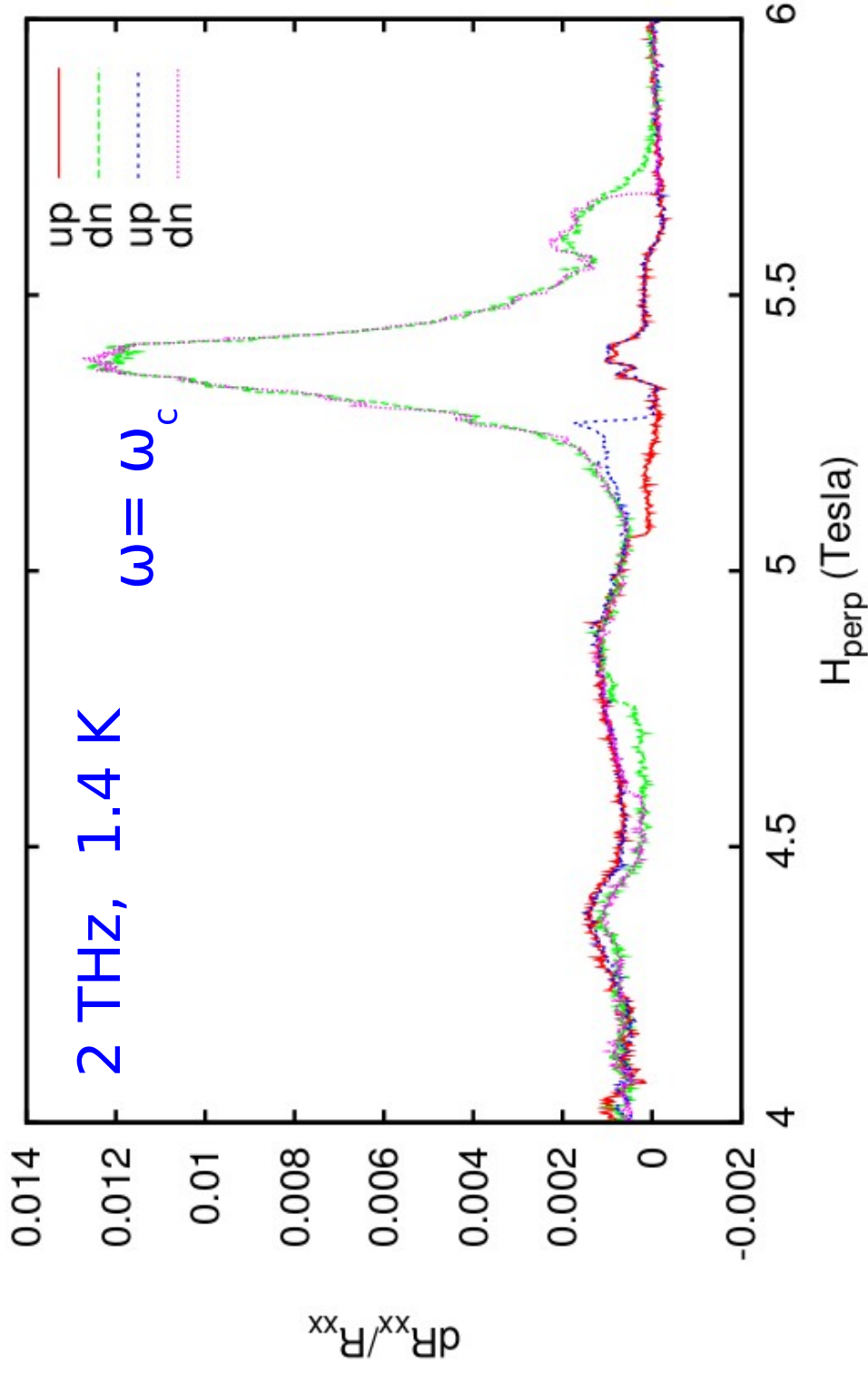
$f = 2.25 \text{ THz}$

(Cambridge 2011-2012)



Interesting B symmetry properties of photo-photovoltage

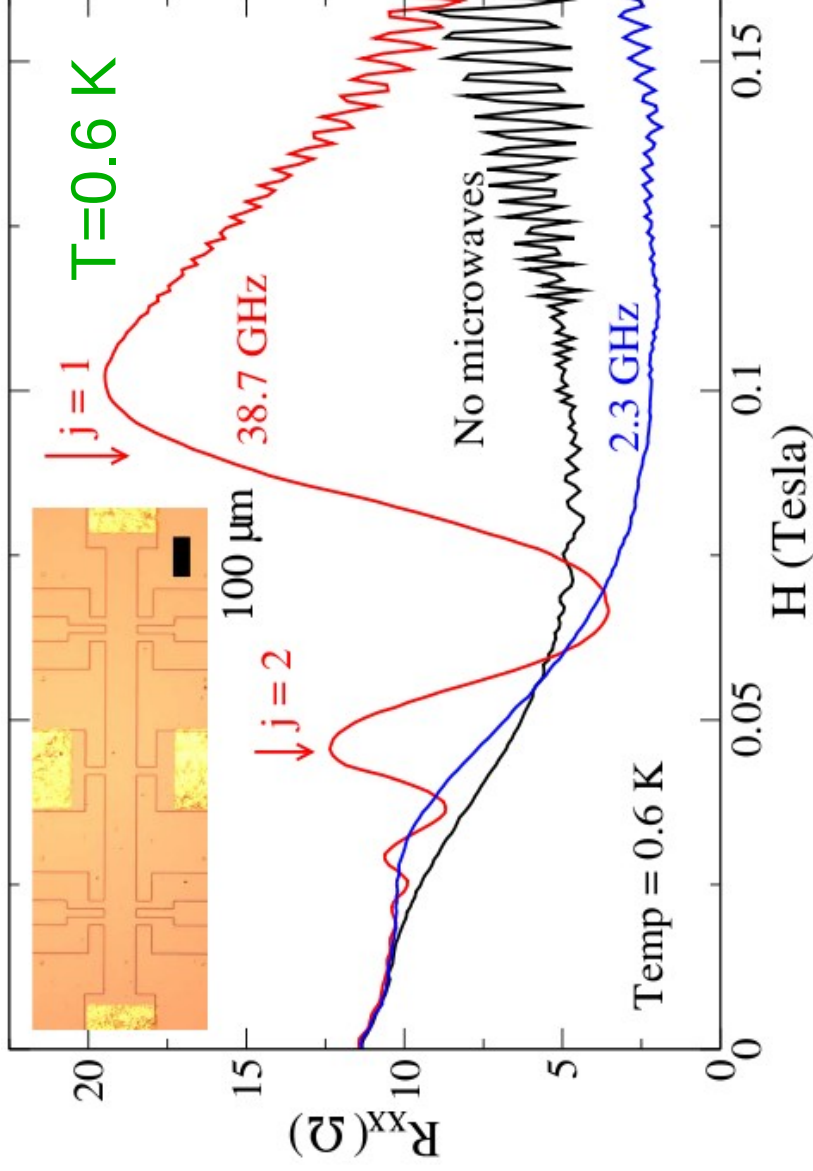
# Bi-stable photo-resistance



- bi-stability under THz illumination (“domains” if one wishes)
- but no zero-resistance ...

Even if one detects “domains” in ZRS, this is not a proof that the “domains” are the cause of ZRS

# Transport under low frequency irradiation (2DEG)



High frequency

$$\omega > \omega_c$$

Low frequency

$$\omega \ll \omega_c$$

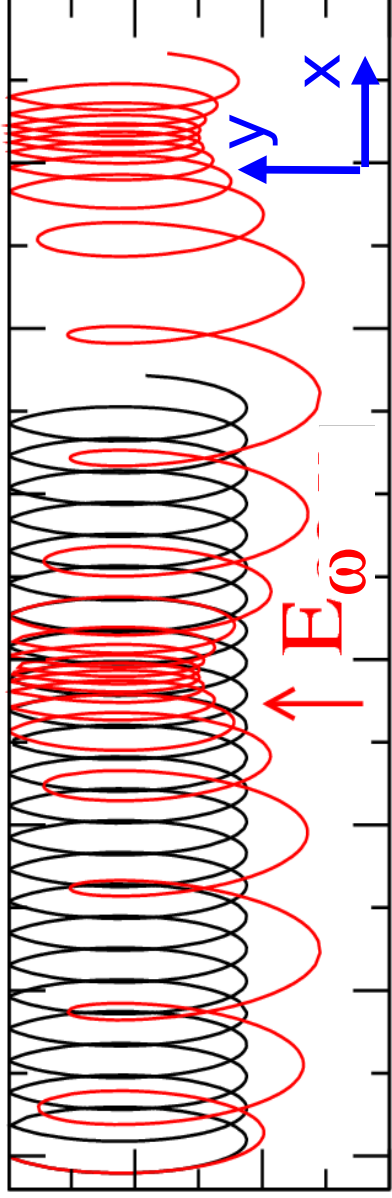
Even a low frequency irradiation can reduce  $R^{xx}$

This effect was not anticipated in bulk transport theories (?)

$\omega \ll \omega_c$  : no transitions between LL in the bulk  
plasma regime  $\omega \tau \sim 10$  : no bulk magnetoplasmons  
for  $\omega < \omega_c$  RF field should not penetrate sample bulk

# A simple edge channel explanation ?

- Low frequency accelerates drift along edges :



Better guiding

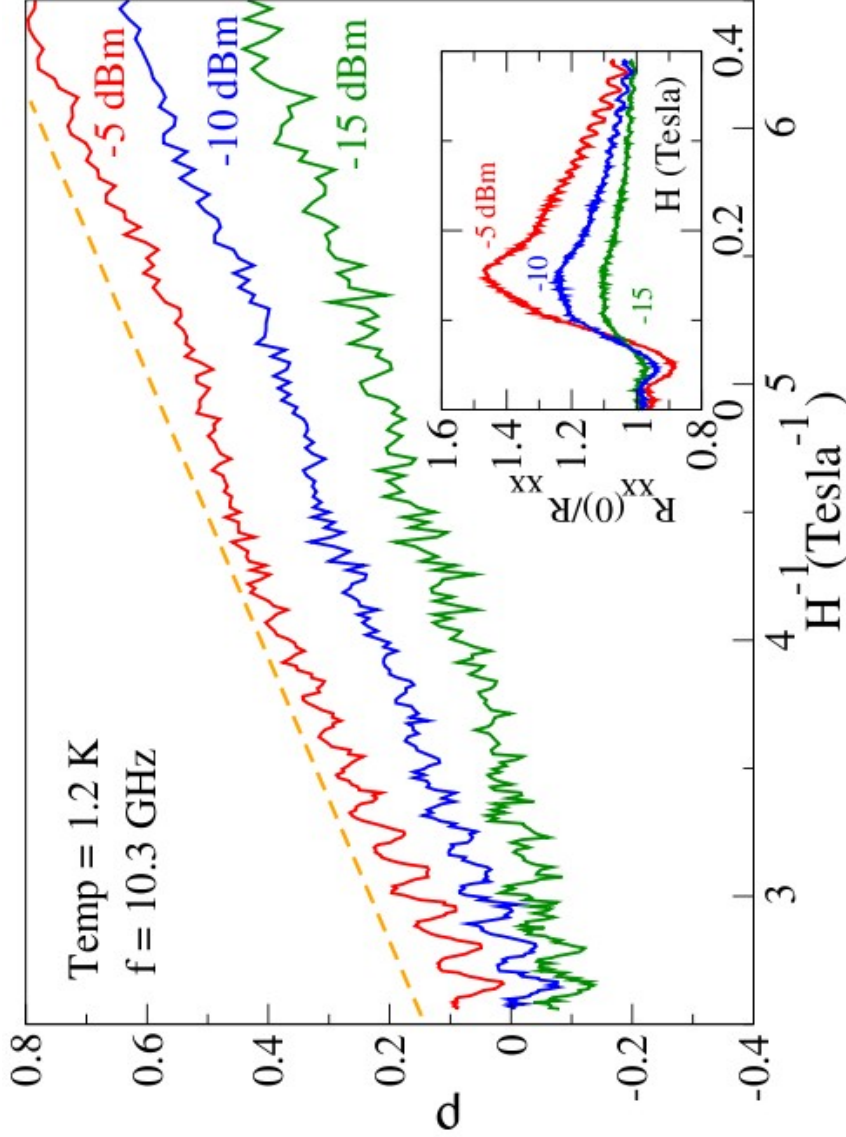
and lower  $R_{xx}$

$$\frac{R_{xx}(0)}{R_{xx}} = \frac{\langle V_g \rangle}{V_g(0)}$$

with microwave

$$\frac{\langle V_g \rangle}{V_g(0)} - 1 \propto \frac{E_\omega}{\omega_c} \propto \frac{\sqrt{P_\omega}}{H}$$

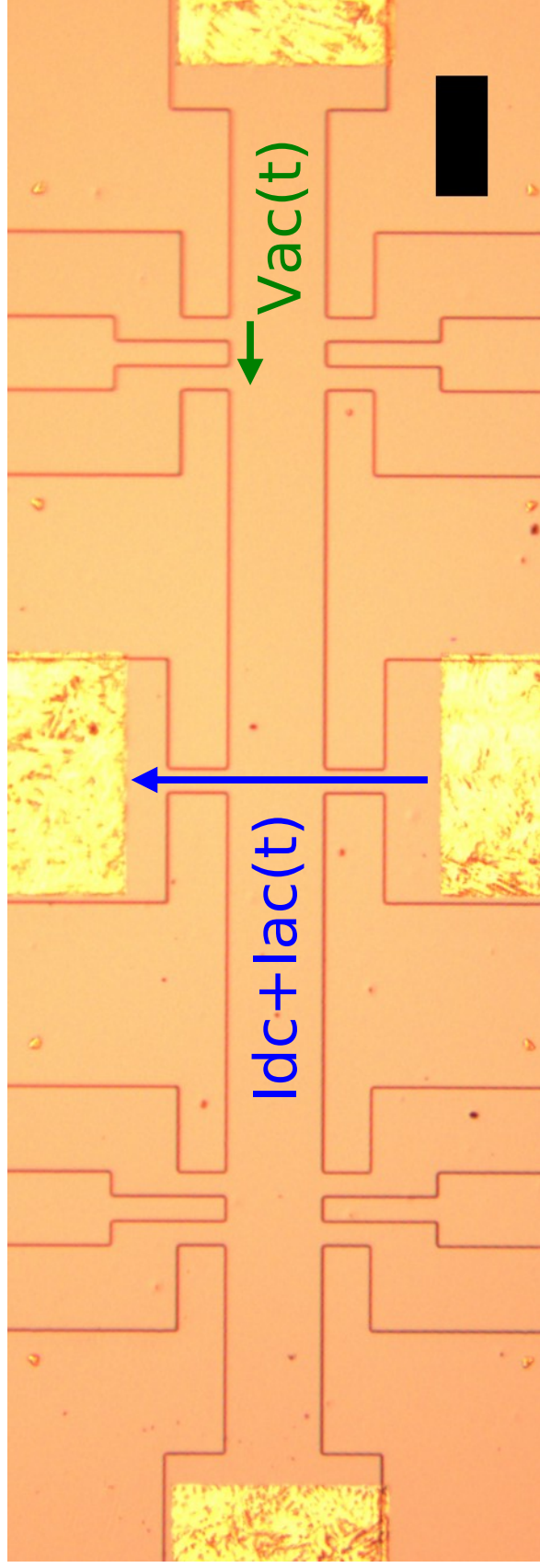
$$\rho = \frac{1}{\sqrt{P_\omega}} \left( \frac{R_{xx}(0)}{R_{xx}} - 1 \right) \propto \frac{1}{H}$$

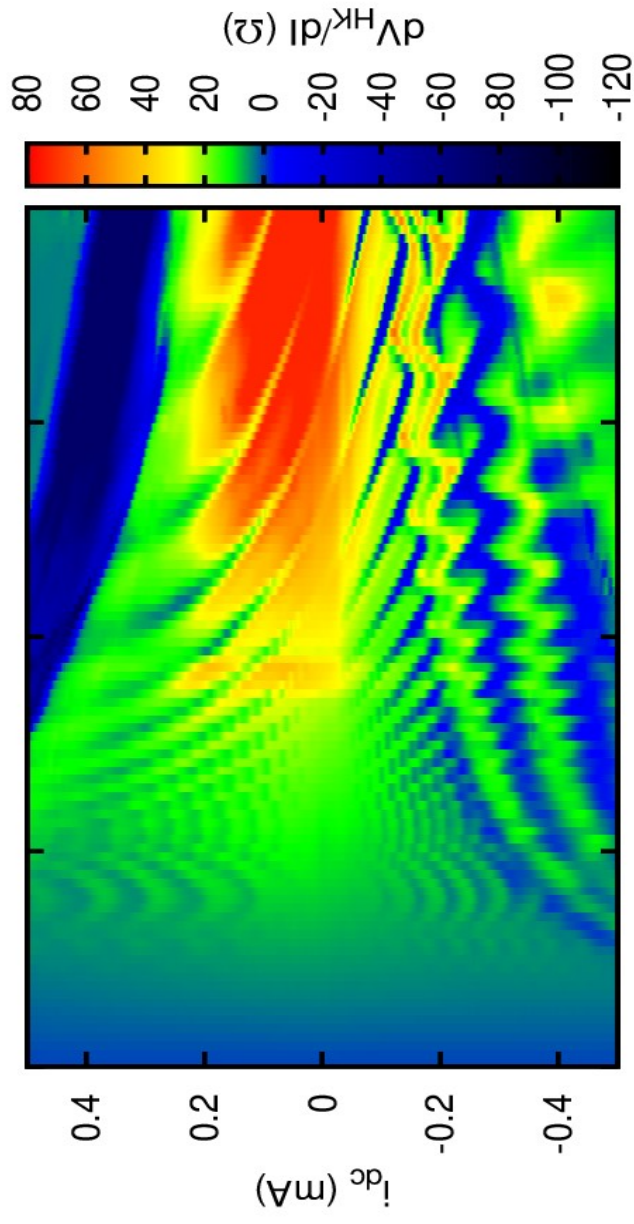


It works !

## Role of edge channels ?

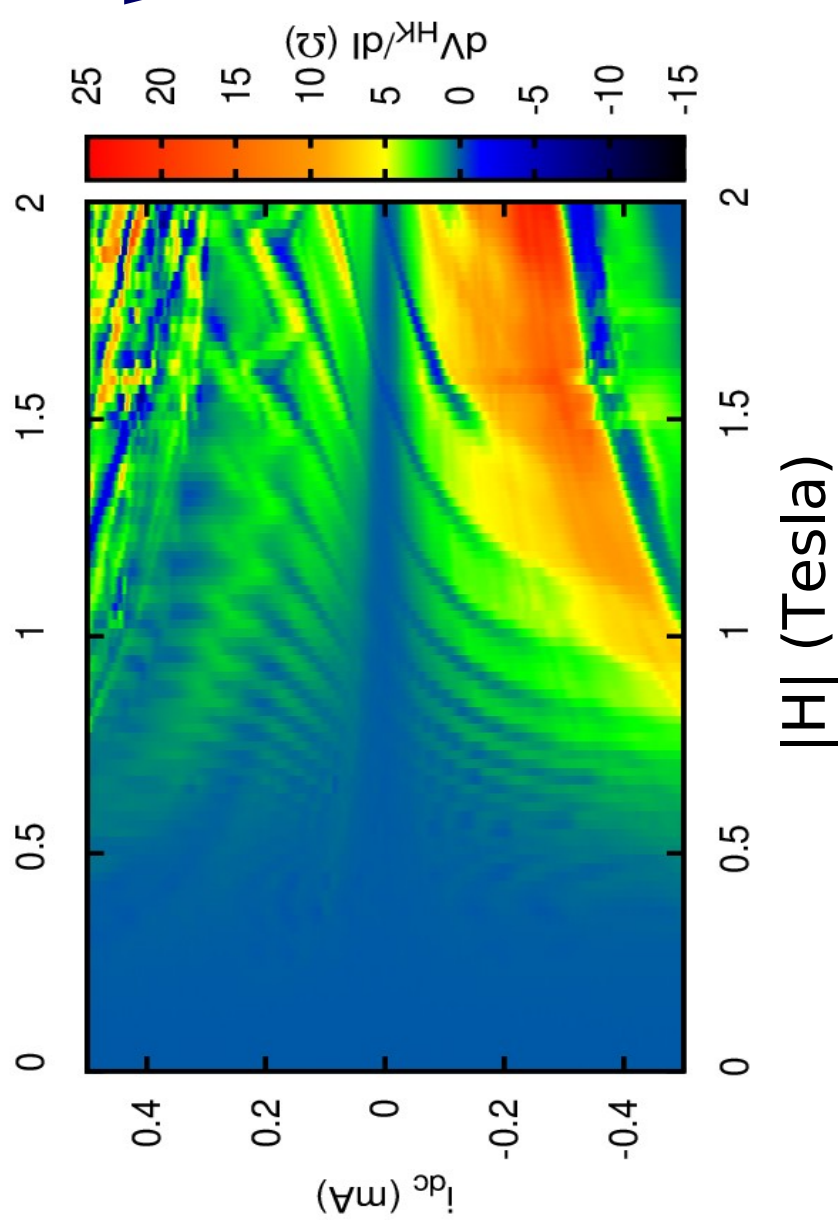
- Objection : I overestimate the role of edge channels in the transport
- Experiment : Try non local measurements ...





$B > 0$

$I_{dc} = 0$   
Strong  $B \rightarrow -B$   
asymmetry

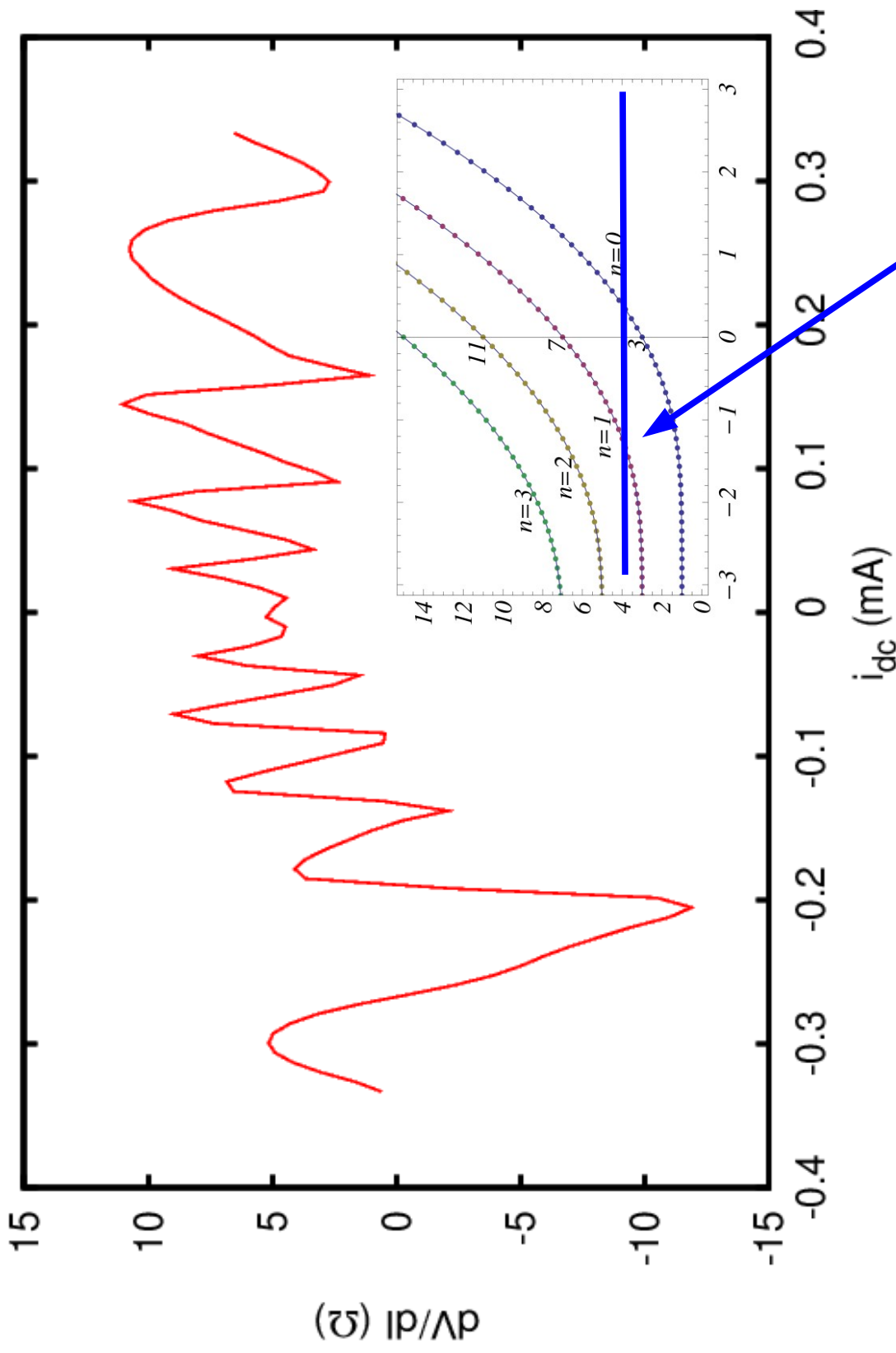


$B < 0$

Finite  $I_{dc}$   
Weak symmetry  
 $B \rightarrow -B$   
 $I_{dc} \rightarrow -I_{dc}$

# Very non harmonic features in $dV/dI$

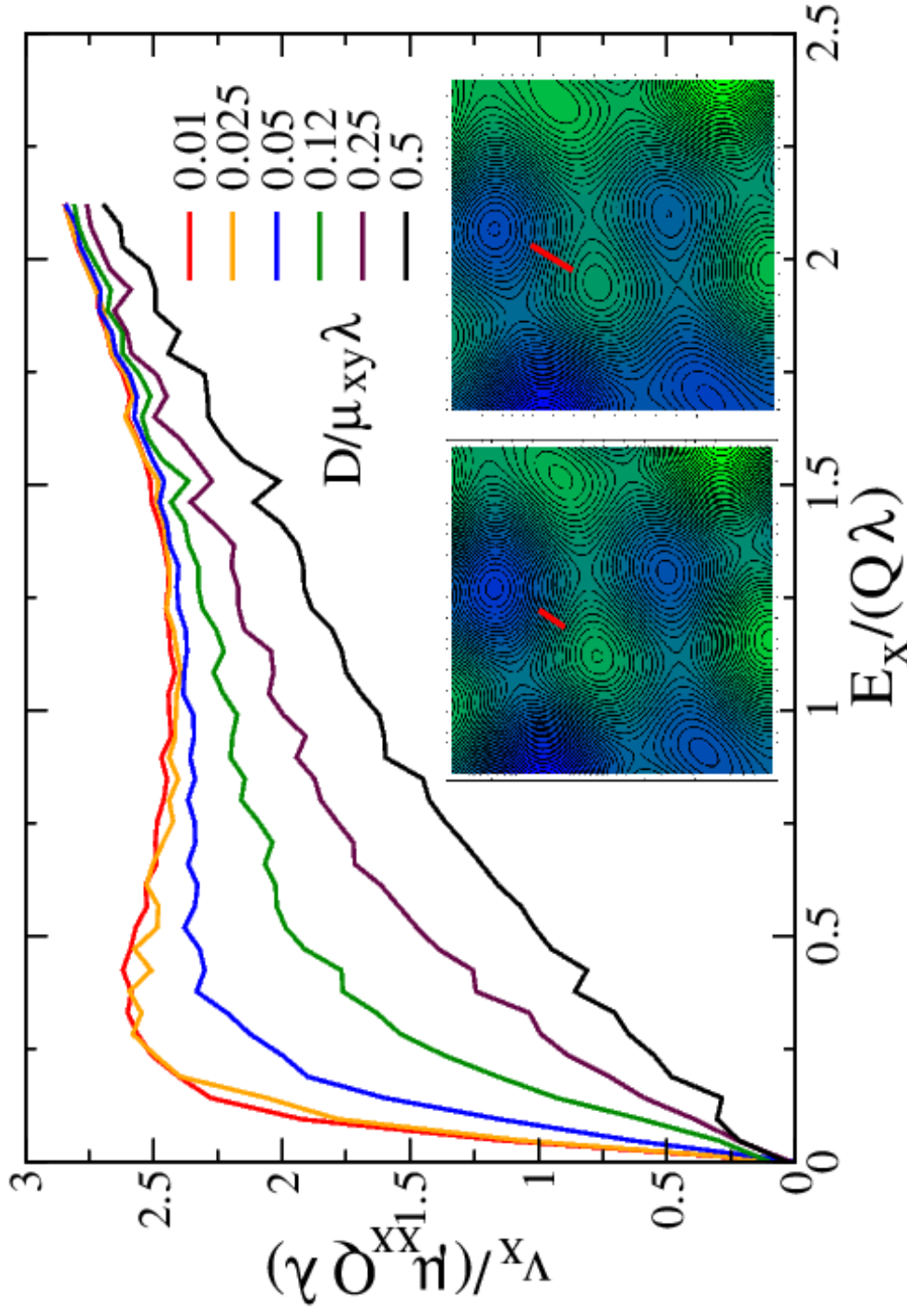
1.4K, 3  $\mu$ A, 32 Hz, 0.6 Tesla



An electric field will tilt the edge states, and suppress the intersection with the Fermi level

# Non linear transport in the sample bulk

$$\partial_t P = \text{div} (\hat{\mu}[\text{grad } U - \mathbf{E}]P) + D\Delta P$$

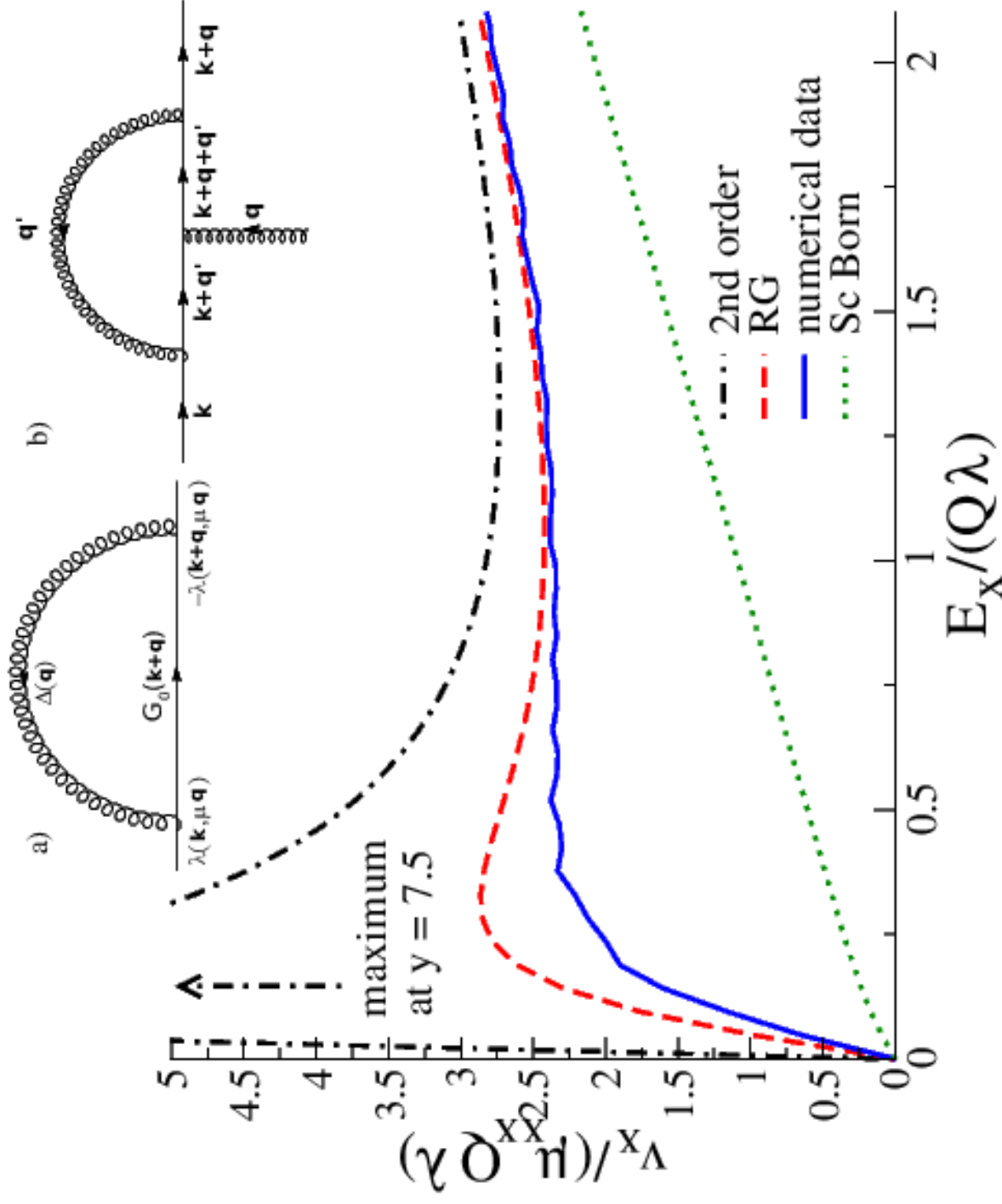


$U(x,y)$  Gaussian correlated disorder potential

Potential  $\lambda$  RMS amplitude;  $Q^{-1}$  correlation length



# Theoretical modelling



Theory does not work great, comparison with simulation important !

## Summary on 2DEG

- THz illumination → photovoltage/“bistability”  
but no ZRS/MIRO so far
  - Experiments in the low frequency limit,  
and non local transport (spectroscopy of edge channels ?)
  - Theory of non linear transport in drift diffusion equations  
in random media (macroscopic diffusion rate determined  
by long range and not microscopic noise)
  - Probably ZRS in GaAs non trivial mixture  
of edge and bulk effects  
(as QHE : edge channels vs percolating paths)
- Many questions, not many answers ...

**Thank you !**



**A Cambridge experimentalist !**