>Panorama B



>Fluxes and applications



>Flux compactifications

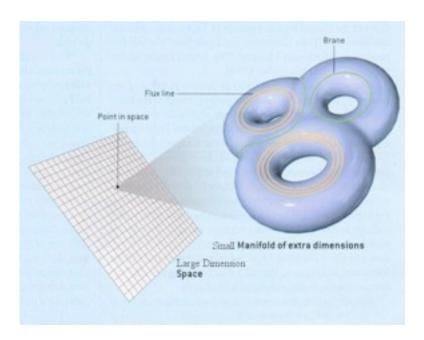
- >Flux compactifications
- >Moduli stabilization

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Moduli stabilization

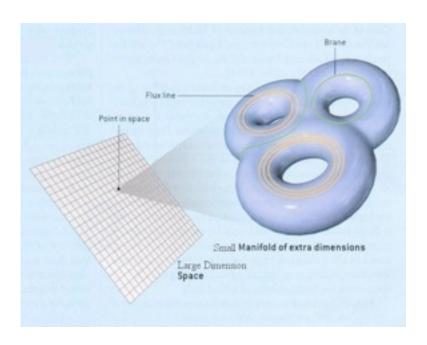
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- Cosmological problems unless massive enough
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Focus on flux compactifications



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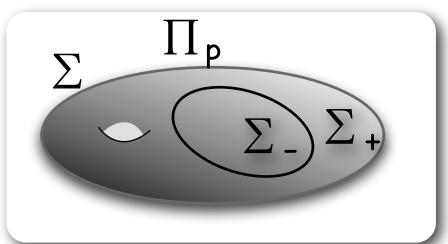
For Topological sector defined by cohomology class

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$$\int_{\Lambda_k} F_{p+1} = N_k$$

Flux quantization



Fluxes introduce moduli dependence in potential energy

Closed string moduli are stabilized

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Dating back to Freund-Rubin

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Vacua need not be Minkowski, but also AdS (or dS??)

Focus on M_4 , or in (A)dS₄ with hierarchycal length scales



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Specify integrals, and local sources, satisfying RR tapole condition

$$Q_{flux} + Q_{D3} + Q_{O3} = 0$$



Flux "tension" and charge

$$\mathcal{L}_{G} = -\frac{1}{24\kappa_{10}^{2}} \int_{\mathbf{X}_{6}} d^{6}y \ g^{\frac{1}{2}} \frac{(G_{3})_{mnp} (\bar{G}_{3})^{mnp}}{\operatorname{Im} \tau} = -\frac{1}{8\kappa_{10}^{2}} \int_{\mathbf{X}_{6}} d^{6}y \ \frac{G_{3} \wedge *_{6}\bar{G}_{3}}{\operatorname{Im} \tau}$$

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"BPS-like" for ISD flux

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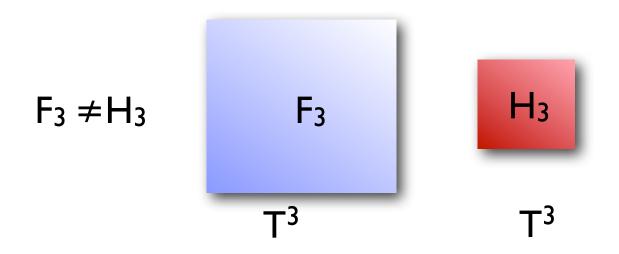
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- Stabilizes complex structure moduli (and dilaton)

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$$\begin{split} ds^2 &= Z(x^m)^{1/2} \ ds_{4d}^2 + Z(x^n)^{1/2} \ g_{mn}^{CY} \ dx^m \ dx^n \\ F_5 &= (I + *_{I0d}) \ dZ^{-I} \ dx^0 \ dx^I \ dx^2 \ dx^3 \\ \nabla^2 \ Z(x^n) &= g_s \ |G_3|^2 + g_s \ \sum \delta(D3/O3) \end{split}$$

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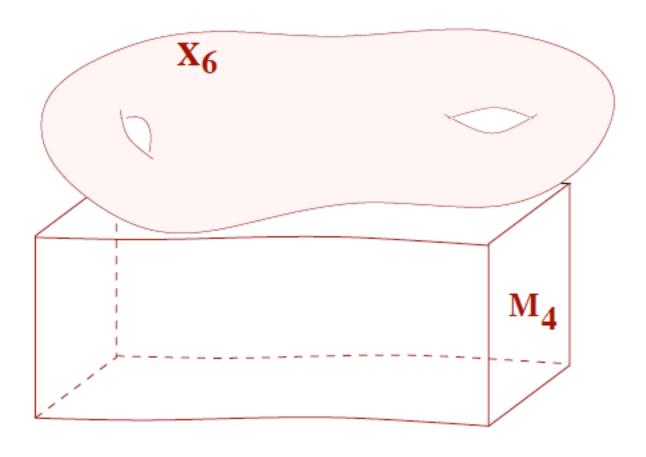
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Underlying CY makes life easy \Rightarrow Many explicit models

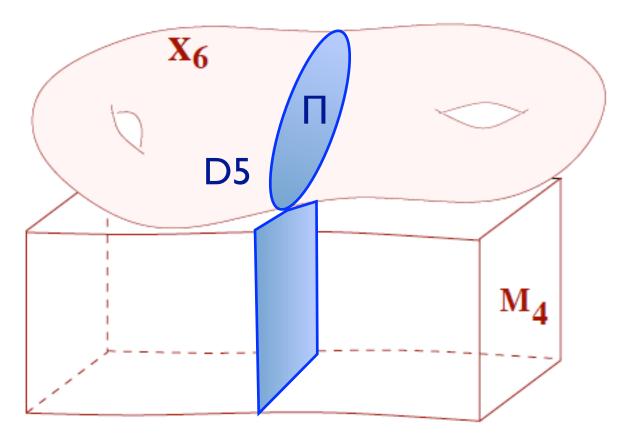
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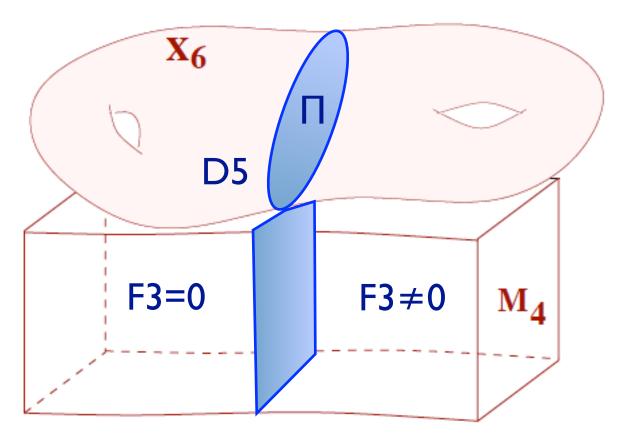
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Compute W_{flux} from tension of domain wall introducing flux

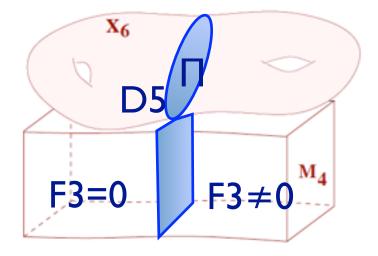


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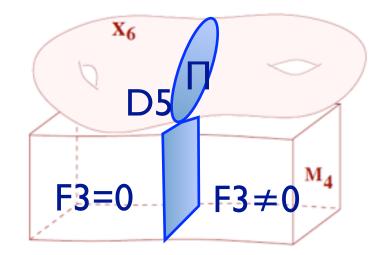
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$$dF_3 = \delta_3(\Pi) \wedge \delta_0(x^3) dx^3$$

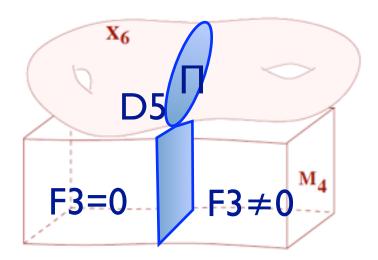




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Integrate over dual 3-cycle Π' x interval in x3

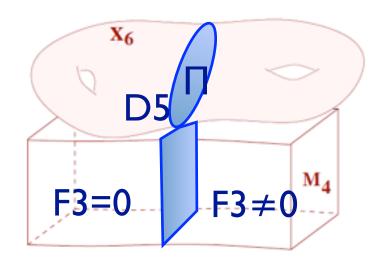
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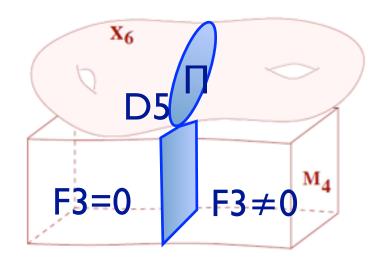
$$W_{F_3} = \int_{\Pi} \Omega_3 = \int_{\mathbf{X}_6} F_3 \wedge \Omega_3$$



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For general F3, H3 fluxes

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- Also from 4d effective theory

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Scalar potential
$$V = e^K \left(g^{a \bar{b}} D_a W D_{\bar{b}} \overline{W} - 3|W|^2 \right)$$

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Vacuum: G4 is SD

Susy: G4 is (2,2)

MSSM from magnetized D7s

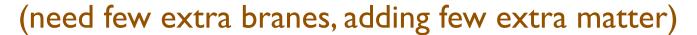
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 Stabilizes at $\tau_1=\tau_2=\tau_3=\tau=e^{2\pi i/3}$

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Stabilizes at $au_1 = au_2 = au_3 = au = e^{2\pi i/3}$

Non-susy
$$G_3 = 2(d\overline{z}_1dz_2dz_3 + dz_1d\overline{z}_2dz_3 + dz_1dz_2d\overline{z}_3 + d\overline{z}_1d\overline{z}_2d\overline{z}_3)$$

Stabilizes e.g. at
$$au_1 = au_2 = au_3 = au = i$$





Corrections

- Earlier no-scale structure disappears upon including corrections
- Perturbative and non-perturbative, in α and g_s
- Corrections may be small in large volume, small g_s regime, but not compared to zero!



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Generalized fluxes

- Above set of fluxes is not really the most general
- Geometric, non-geometric, U-dual fluxes
- Superpotentials depending on all moduli

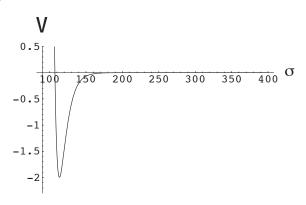
Use non-perturbative effects from D3-brane instantons

One-modulus toy model

$$W = W_{0,\text{flux}} + A(z_0)e^{-T}$$

Susy AdS vacua with stabilized moduli

[Kachru, Kallosh, Linde, Trivedi]



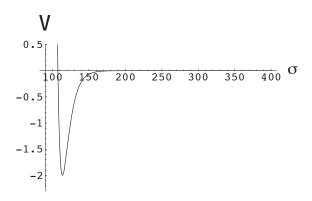
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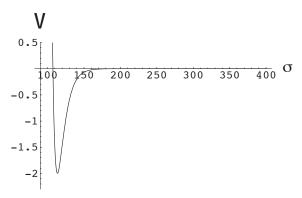
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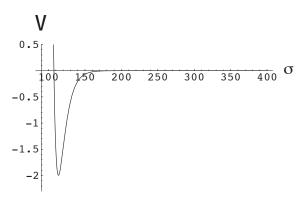
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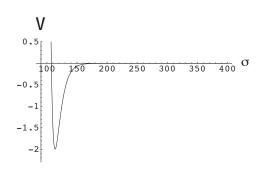


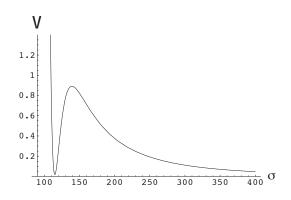
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- Clash with SM arising from D7's

Intersections of instanton with D7's lead to supos involving SM fields

$$W = e^{-T} \rightarrow W = e^{-T} \Phi_1 \dots \Phi_n$$

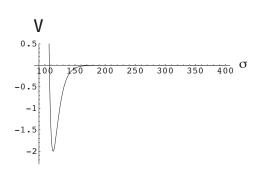
Proposal to add sources of extra tension for uplifting to deSitter

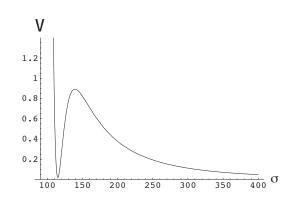




- Anti D3-branes

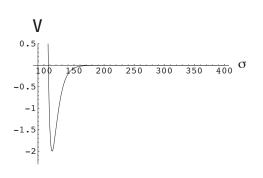
Proposal to add sources of extra tension for uplifting to deSitter

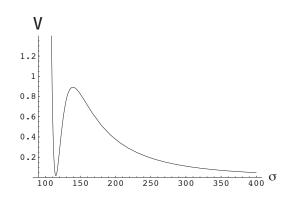




- Anti D3-branes
- D-terms: anti-instantons on D7s
- F-terms fon flux supo itself
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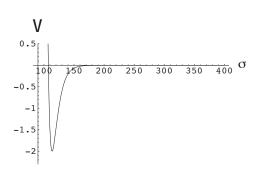
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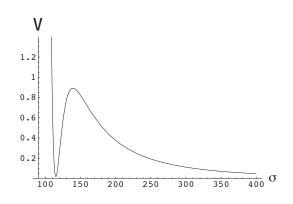




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Proposal to add sources of extra tension for uplifting to deSitter





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Generalized fluxes

- Flux compactifications in type IIA involve even and odd forms
- → Talk both to Kahler and complex structure moduli!

What about mirror symmetry?

- \checkmark Using T-duality in local T³ fibration, H₃ turns e.g. into geometric twist
- ⇒ Geometric fluxes
- Compactification on non-CY geometries, possibly 4d N=1
 - SU(3) holonomy $\rightarrow SU(3)$ structure
 - ⇒ Generalized complex geometry, mirror symmetry, ...
 - Painful lack of explicit compact examples

Generalized fluxes

Generalized geometric and non-geometric fluxes from T-duality

Regard T³ as T² (trivially) fibered over S¹

H₃ is monodromy b \rightarrow b+1 for b= \int_{T_2} B

Particular SL(2,Z) monodromy on T=A_{T2}+ib

One T-duality along T2 gives $\tau \rightarrow \tau + 1$ in SL(2,Z) of τ

⇒ Geometric twisting, geometric flux

One SI non-trivially fibered over two directions ω^a_{bc}

Two T-dualities give non-geometric SL(2,Z) monodromy on T

 \Rightarrow Non-geometric twisting, non-geometric flux Q^{ab}_c

Full T-duality covariance suggests

⇒ locally non-geometric Rabc

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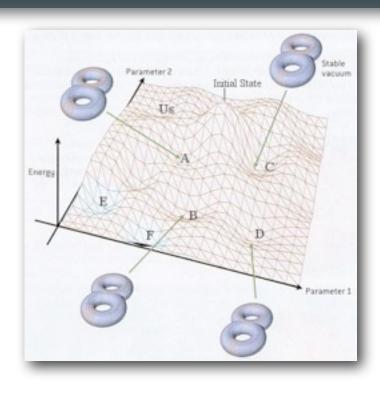
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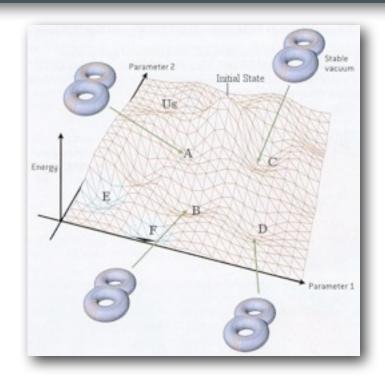


The general picture is compelling enough

Figure 1 The general picture is compelling enough



The general picture is compelling enough Internal data determine 4d physics symmetries, spectrum, couplings

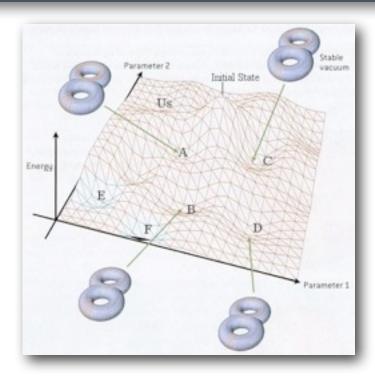


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Many choices: "Landscape"



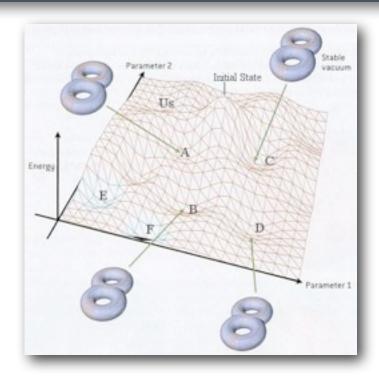
Flux landscape

Figure 1 The general picture is compelling enough

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Flux landscape, part of full string landscape

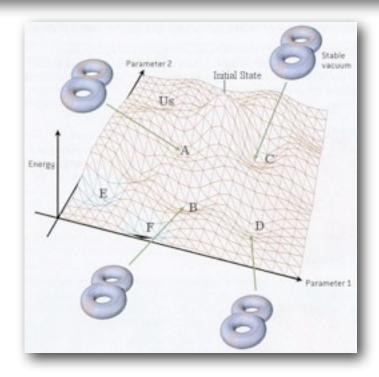
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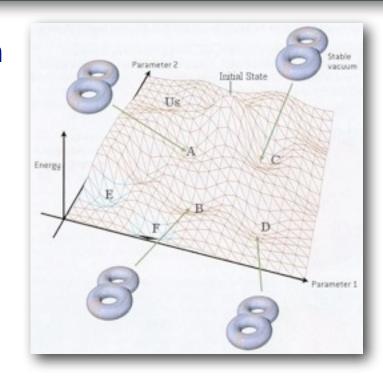
Flux landscape, part of full string landscape

Various estimates by flux counting

Flux landscape

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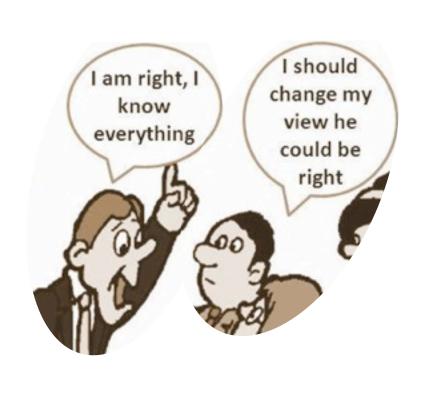
Revision of "naturalness": cosmological constant, hierarchy,...



















Yeah, but...

Yeah, but...



What about some real Physics?



What about some real Physics?





Keep rocking

After all, we are dealing with a theory which is much more clever than any of us

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- Focus on inter-relations between (field strength) fluxes and D-branes

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- Efects at several levels
 - Topological: Freed-Witten consistency conditions
 - (Susy) Open string moduli stabilization
 - Susy breaking

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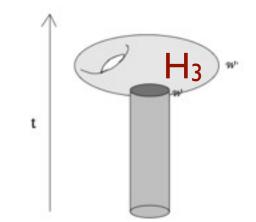
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Must be cancelled by boundaries of outgoint D4's



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Analogous statements for RR fluxes



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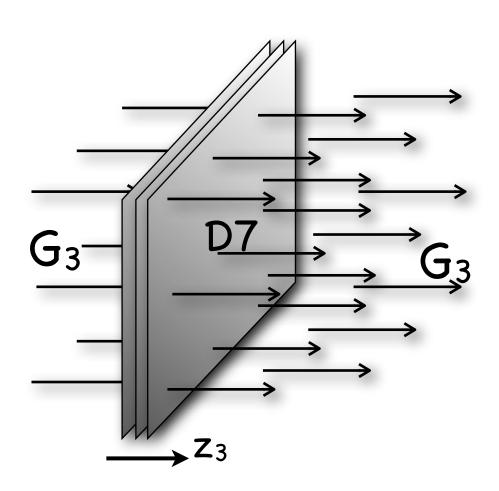
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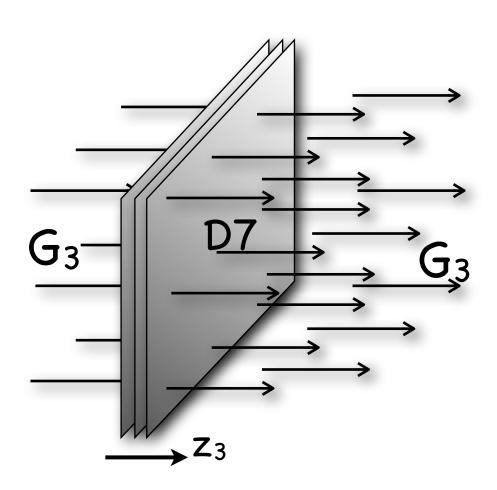
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Can also do Zk domain walls. See later

An appealing scenario: Susy MSSM D-brane sector and non-susy flux

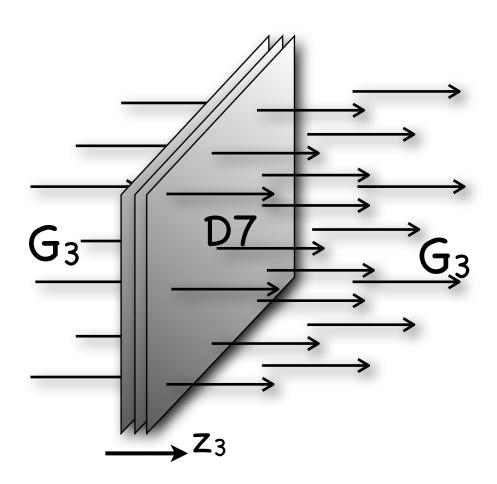


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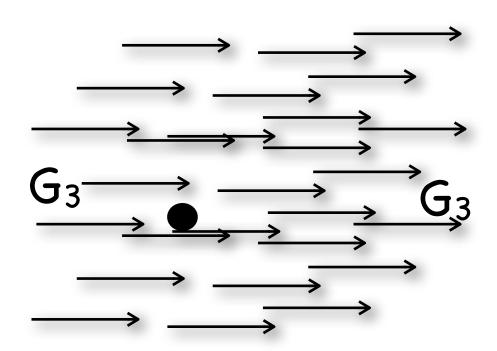


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Explicitly computable using D-brane world-volume action in general supergravity background, or using 4d effective theory approach

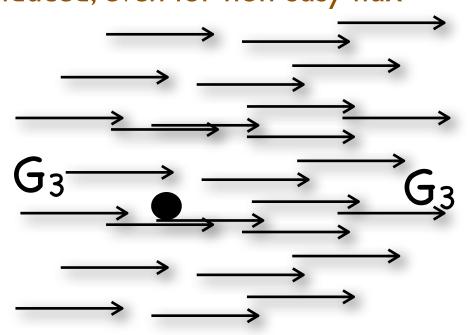


D3s in ISD 3-form flux background



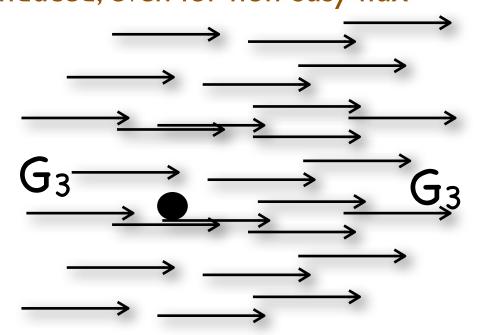
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ISD flux background: same tension and 4-form charge as a D3-brane Gravitational attraction cancels against Coulomb repulsion: No terms induced, even for non-susy flux



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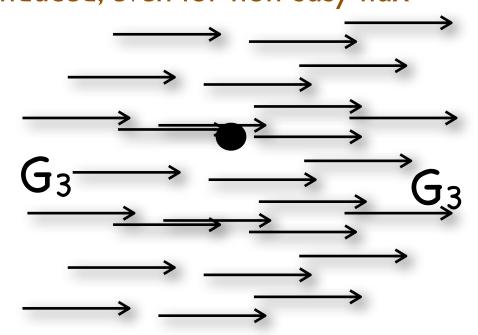


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Effects add up instead of cancelling Scalars stabilize at max of flux density

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$$m^2 \sim |G_{(0,3)}|^2$$
 $M \sim G_{(0,3)}$
 $A \sim G_{(0,3)}$

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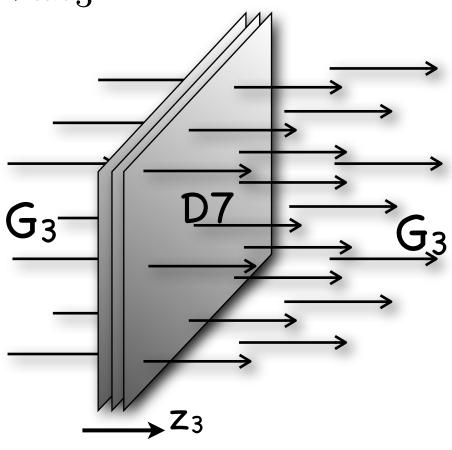
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D7s in ISD 3-form flux background

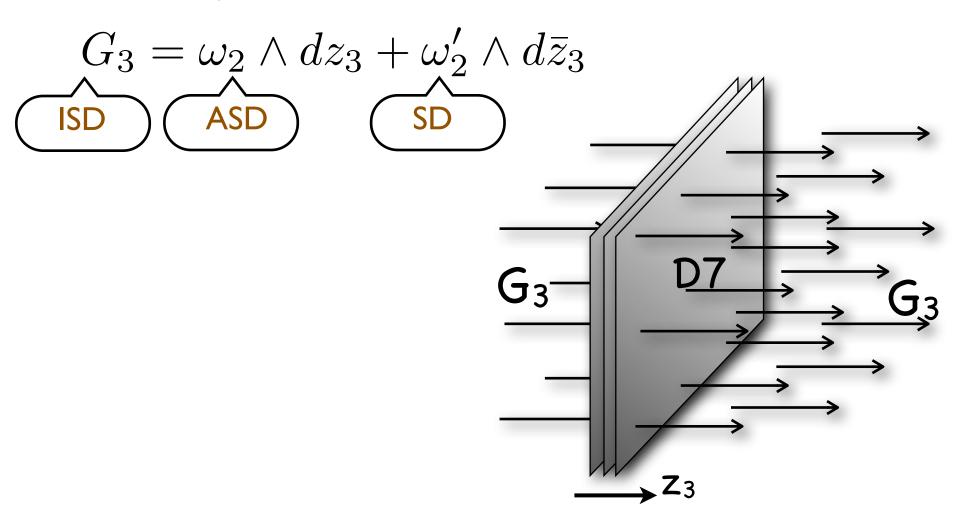
Position in ISD 3-form flux background

PD7s in ISD 3-form flux background

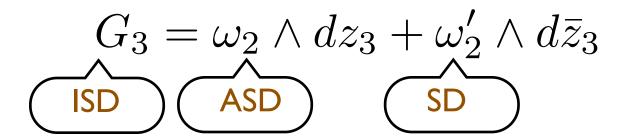
$$G_3 = \omega_2 \wedge dz_3 + \omega_2' \wedge d\bar{z}_3$$



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Can recover both D3 and D7 results from effective theory

Flux components are vevs for moduli auxiliary fields: spurions

$$D_{\tau}W \sim \int_{X} \overline{G}_{3} \wedge \Omega \quad D_{z_{i}}W \sim \int_{X} G_{3} \wedge \chi_{(2,1),i} \quad D_{\rho}W \sim \int_{X} G_{3} \wedge \Omega$$

Gravity mediation (in general, not universal, no mSUGRA)

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Scales $M_{SUSY} \sim f \frac{\alpha'}{R^3} \sim f \frac{M_c^2}{M_p}$ f: possible local suppression

LowE Susy: TeV soft terms from $M_c \sim 10^{11} {\rm GeV}$

Low-Susy: Choose $M_c \sim 10^{14} {\rm GeV}$ then $M_{SUSY} \sim 10^{10} {\rm GeV}$

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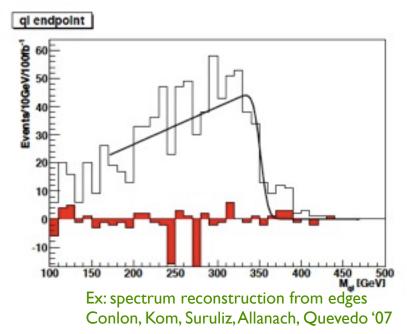
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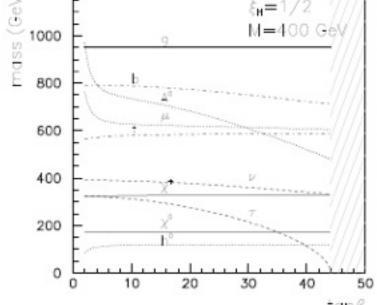
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Can get to make plots



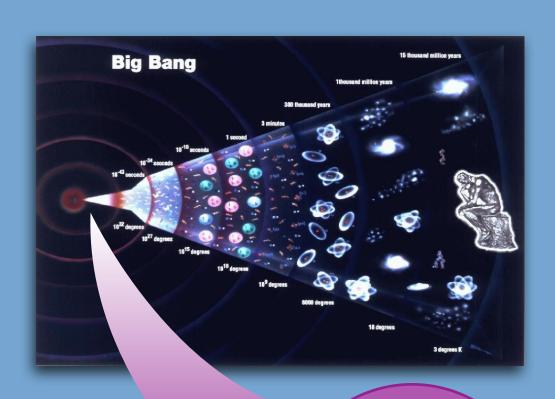


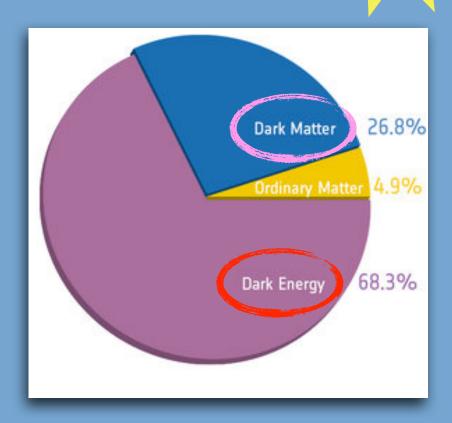
Ex: MSSM parameters Aparicio, Cerdeno, Ibanez '08

Cosmological Standard Model

(Λ CDM, "concordance model")







inflation cf. Shiu's lectures



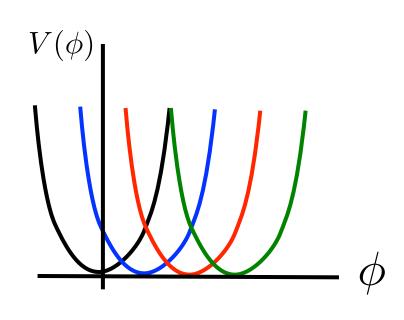
Recent interest in large field inflation

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- Scalars with shift symmetry (axions) are well protected continuous symmetry broken by non-pert effects to a discrete periodicity
- String theory axions have sub-Planckian decay constant

Axion monodromy: Potential is periodic but multivalued

Field theory analogue:
theta dependent vacuum energy
in large N pure gluodynamics Witten







Discrete gauge symmetries





Discrete gauge symmetries

Zn particles, Zn strings, ...









Discrete gauge symmetries

Zn particles, Zn strings, ...



Figure 1 There are Zn gauge symmetries associated to 4d domain walls

Zn symmetry of a 3-form that eats up a 2-form

$$\frac{1}{2}|F_4|^2 + |db_2 - n c_3|^2$$

Gauge invariance

$$c_3 \rightarrow c_3 + d\Lambda_2$$
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Dualizing b2 to an axion, get Kaloper-Sorbo description of axion monodromy models.



Can consider other Zn charged objects in 4d

Lagrangian for 3-form eating up a 2-form

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Gauge transformation

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Can arise in D-brane & flux models



Structure is automatic in flux compactifications

After all, fluxes produce the stabilization of axions in moduli!!



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10d Chern-Simons ⇒ modified field strengths

$$\int_{10d} B_2 \wedge F_p \wedge F_{p+2} \qquad \Rightarrow \qquad \tilde{F}_{p+2} = dC_{p+1} + B_2 \wedge F_p$$



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Integrating over fluxed CY with $\ \phi = \int_{\Sigma_2} B_2$, $\ M = \int_{\Pi_p} F_p$

Change in axion induces extra flux

$$\Delta \phi \to \Delta \int_{\Sigma_2 \times \Pi_p} \tilde{F}_{p+2} = \phi M$$

A nice class: axions in flux compactifications

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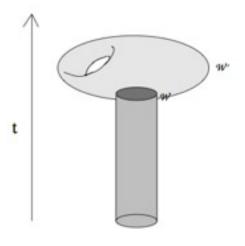


Monodromy

Multiple branches connected by domain walls changing (p+2)-form flux. They are D(6-p) on (4-p)-cycle



Many other realizations



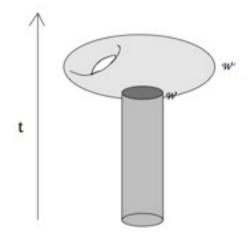


Many other realizations

Ex: IIB with NSNS flux on A-cycle

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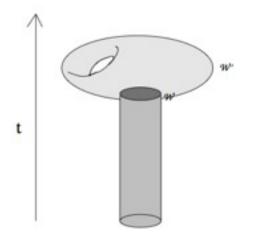




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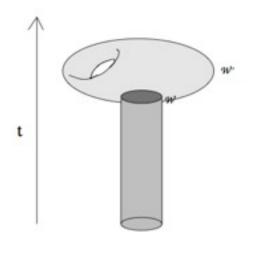
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I0d IIB axion has a monodromy. Origin of energetic cost? GVW supo $W=\int_{X_6}(F_3-\tau\overline{H}_3)\wedge\Omega$

Period of C0 changes n units of F3 flux on A 4d Domain Wall is D5 on B 4d instanton is D(-1) (cosine modulation)

It is amazing that something close to the SM can be realized in string theory

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Branes provide a tractable setup for SM model building in string theory

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- Program is not closed: Continuous progress
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 - Neutrino masses, non-perturbative operators
 - Discrete symmetries. Fluxed inflation models.
- Expect continuous progress and new results and useful input from LHC & cosmo

To all organizers & hosts & participats of

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