

# 2 THREE-LEVEL OPTICAL SYSTEMS

# OUTLINE

2.1 BASIC THEORY

2.1 STIRAP: STIMULATED RAMAN ADIABATIC PASSAGE

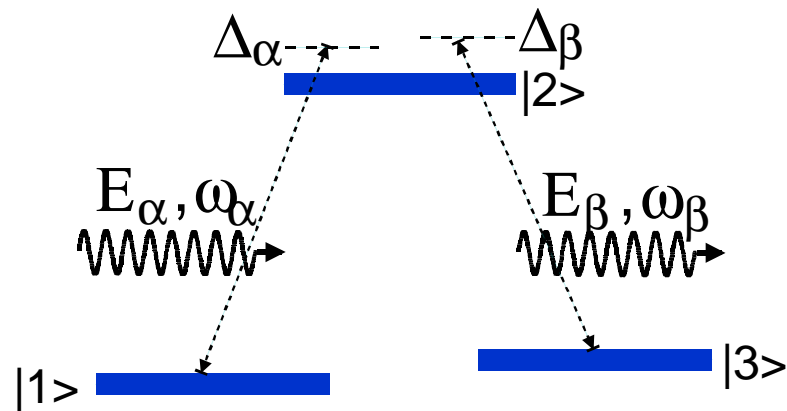
2.2 EIT: ELECTROMAGNETICALLY INDUCED TRANSPARENCY

2.3 CPT: COHERENT POPULATION TRAPPING

2.4 RAP: RAPID ADIABATIC PASSAGE, REVISITED

2.1 BASIC THEORY

► PHYSICAL MODEL



$$\vec{E}_\alpha = \vec{E}_{\alpha 0} \cos \omega_\alpha t$$

$$\vec{E}_\beta = \vec{E}_{\beta 0} \cos \omega_\beta t$$

$$\Delta_\alpha = \omega_{21} - \omega_\alpha$$

$$\Delta_\beta = \omega_{23} - \omega_\beta$$

➡ Electric dipole interaction:  $V^{(ADE)} = -\vec{\mu} \cdot \vec{E}(t) = -(-e)\vec{r} \cdot \vec{E}(t)$

$$\hat{\mu} = \begin{pmatrix} 0 & \vec{\mu}_{12} & 0 \\ \vec{\mu}_{12}^* & 0 & \vec{\mu}_{23} \\ 0 & \vec{\mu}_{23}^* & 0 \end{pmatrix} \quad V = \hbar \begin{pmatrix} 0 & \Omega_\alpha \cos \omega_\alpha t & 0 \\ \Omega_\alpha^* \cos \omega_\alpha t & 0 & \Omega_\beta \cos \omega_\beta t \\ 0 & \Omega_\beta^* \cos \omega_\beta t & 0 \end{pmatrix}$$

$$\Omega_\alpha = -\frac{\vec{\mu}_{12} \cdot \vec{E}_{\alpha 0}}{\hbar} \quad \Omega_\beta = -\frac{\vec{\mu}_{23} \cdot \vec{E}_{\beta 0}}{\hbar}$$

## 2. THREE-LEVEL OPTICAL SYSTEMS (4)

⇒ Total Hamiltonian:  $H = H_0 + V$

$$H = \hbar \begin{pmatrix} 0 & \Omega_\alpha \cos \omega_\alpha t & 0 \\ \Omega_\alpha^* \cos \omega_\alpha t & \omega_{12} & \Omega_\beta \cos \omega_\beta t \\ 0 & \Omega_\beta^* \cos \omega_\beta t & \omega_{12} - \omega_{23} \end{pmatrix}$$

⇒ Interaction Picture:  $\bar{H} = UH_0U^{-1}$

with

$$\left. \begin{aligned} \hat{U} &= e^{i\frac{H_{IP}t}{\hbar}} \\ H_{IP} &= \hbar \begin{pmatrix} 0 & 0 & 0 \\ 0 & \omega_\alpha & 0 \\ 0 & 0 & \omega_\alpha - \omega_\beta \end{pmatrix} \end{aligned} \right\} \begin{array}{c} \text{RWA} \\ \downarrow \\ \longrightarrow \end{array} \bar{H} = \hbar \begin{pmatrix} 0 & \frac{\Omega_\alpha}{2} & 0 \\ \frac{\Omega_\alpha^*}{2} & \omega_{21} & \frac{\Omega_\beta}{2} \\ 0 & \frac{\Omega_\beta^*}{2} & \omega_{21} - \omega_{23} \end{pmatrix}$$

## 2. THREE-LEVEL OPTICAL SYSTEMS (5)

⇒ Density Matrix: coherent dynamics

$$\dot{\rho} = -\frac{i}{\hbar}[H, \rho] \quad \text{In the interaction picture:} \quad \dot{\bar{\rho}} = -\frac{i}{\hbar}[\bar{H} - H_{IP}, \bar{\rho}]$$

With:

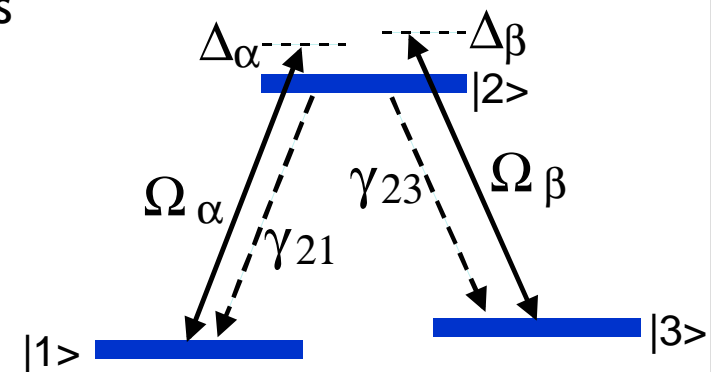
$$\bar{H} - H_{IP} = \frac{\hbar}{2} \begin{pmatrix} 0 & \Omega_{\alpha} & 0 \\ \Omega_{\alpha}^* & 2\Delta_{\alpha} & \Omega_{\beta} \\ 0 & \Omega_{\beta}^* & 2(\Delta_{\alpha} - \Delta_{\beta}) \end{pmatrix}$$

⇒ Density Matrix: adding the incoherent dynamics

$$\dot{\bar{\rho}} = -\frac{i}{\hbar}[\bar{H} - H_{IP}, \bar{\rho}] + L\bar{\rho}$$

where  $L\bar{\rho}$  accounts for:

- spontaneous emission
- incoherent pumping
- elastic and inelastic collisions
- fluctuations in the phase and/or amplitude of the laser fields
- ...



## 2. THREE-LEVEL OPTICAL SYSTEMS (6)

$$\dot{\bar{\rho}} = -\frac{i}{\hbar} [\bar{H} - H_{IP}, \bar{\rho}] + L\bar{\rho}$$

$$\dot{\bar{\rho}}_{11} = -\text{Im}(\Omega_{\alpha}^* \bar{\rho}_{12}) + \gamma_{21}\rho_{22}$$

$$\dot{\bar{\rho}}_{22} = \text{Im}(\Omega_{\alpha}^* \bar{\rho}_{12}) + \text{Im}(\Omega_{\beta}^* \bar{\rho}_{32}) - \gamma_{21}\rho_{22} - \gamma_{23}\rho_{22}$$

$$\dot{\bar{\rho}}_{33} = -\text{Im}(\Omega_{\beta}^* \bar{\rho}_{32}) + \gamma_{23}\rho_{22}$$

$$\dot{\bar{\rho}}_{13} = -i \left[ (\Delta_{\beta} - \Delta_{\alpha}) \bar{\rho}_{13} - \frac{\Omega_{\beta}^*}{2} \bar{\rho}_{12} + \frac{\Omega_{\alpha}}{2} \bar{\rho}_{23} \right] - \Gamma_{13}\rho_{13} \quad \text{with } \Gamma_{13} \geq 0$$

$$\dot{\bar{\rho}}_{12} = -i \left[ (\bar{\rho}_{22} - \bar{\rho}_{11}) \frac{\Omega_{\alpha}}{2} - \Delta_{\alpha} \bar{\rho}_{12} - \frac{\Omega_{\beta}}{2} \bar{\rho}_{13} \right] - \Gamma_{12}\rho_{12} \quad \text{with } \Gamma_{12} \geq (\gamma_{21} + \gamma_{23})/2$$

$$\dot{\bar{\rho}}_{23} = -i \left[ (\bar{\rho}_{22} - \bar{\rho}_{33}) \frac{\Omega_{\beta}^*}{2} - \Delta_{\beta} \bar{\rho}_{23} - \frac{\Omega_{\alpha}^*}{2} \bar{\rho}_{13} \right] - \Gamma_{32}\rho_{32} \quad \text{with } \Gamma_{32} \geq (\gamma_{21} + \gamma_{23})/2$$

$$\dot{\Omega}_{\alpha} = -\kappa\Omega_{\alpha} + ig\bar{\rho}_{12} \quad \kappa: \text{losses and } g: \text{gain constant}$$

For  $\Omega_{\alpha} \in \Re \Rightarrow \text{Im } \bar{\rho}_{12}$  accounts for light absorption/amplification

$\text{Re } \bar{\rho}_{12}$  yields the index of refraction

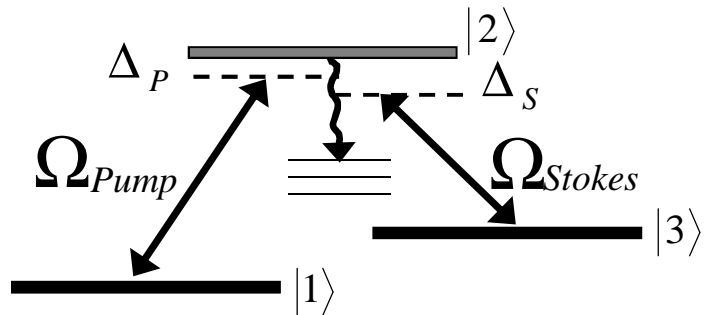
## 2. THREE-LEVEL OPTICAL SYSTEMS (7)

### 2.2 STIRAP: STIMULATED RAMAN ADIABATIC PASSAGE

"Coherent population transfer among quantum states of atoms and molecules"

K. Bergmann, H. Theuer, and B. W. Shore

Rev. Mod. Phys. 70, 1003 (1998)



$$H(t) = \frac{\hbar}{2} \begin{pmatrix} 0 & \Omega_P(t) & 0 \\ \Omega_P(t) & 2\Delta_P & \Omega_S(t) \\ 0 & \Omega_S(t) & 2(\Delta_P - \Delta_S) \end{pmatrix}$$

Energy eigenstates:

$$|+\rangle = \frac{1}{\sqrt{2}} [\sin \Theta |1\rangle + |2\rangle + \cos \Theta |3\rangle] \quad \tan \Theta = \Omega_P(t) / \Omega_S(t)$$

$$|D\rangle = \cos \Theta |1\rangle - \sin \Theta |3\rangle \quad \omega^0 = 0$$

$$|-\rangle = \frac{1}{\sqrt{2}} [\sin \Theta |1\rangle - |2\rangle + \cos \Theta |3\rangle] \quad \omega^\pm = \pm \sqrt{\Omega_P^2 + \Omega_S^2}$$

$\Delta_P = \Delta_S = 0$

For  $\Delta_P = \Delta_S \neq 0$  (Raman resonance condition) we still have  $|D\rangle = \cos \Theta |1\rangle - \sin \Theta |3\rangle$

For  $\Delta_P \neq \Delta_S$ , there is no dark state

**STIRAP:** adiabatically following the dark state from  $|1\rangle$  to  $|3\rangle$ , i.e.,  $\Theta(t_0) = 0^\circ \rightarrow \Theta(t_f) = 90^\circ$

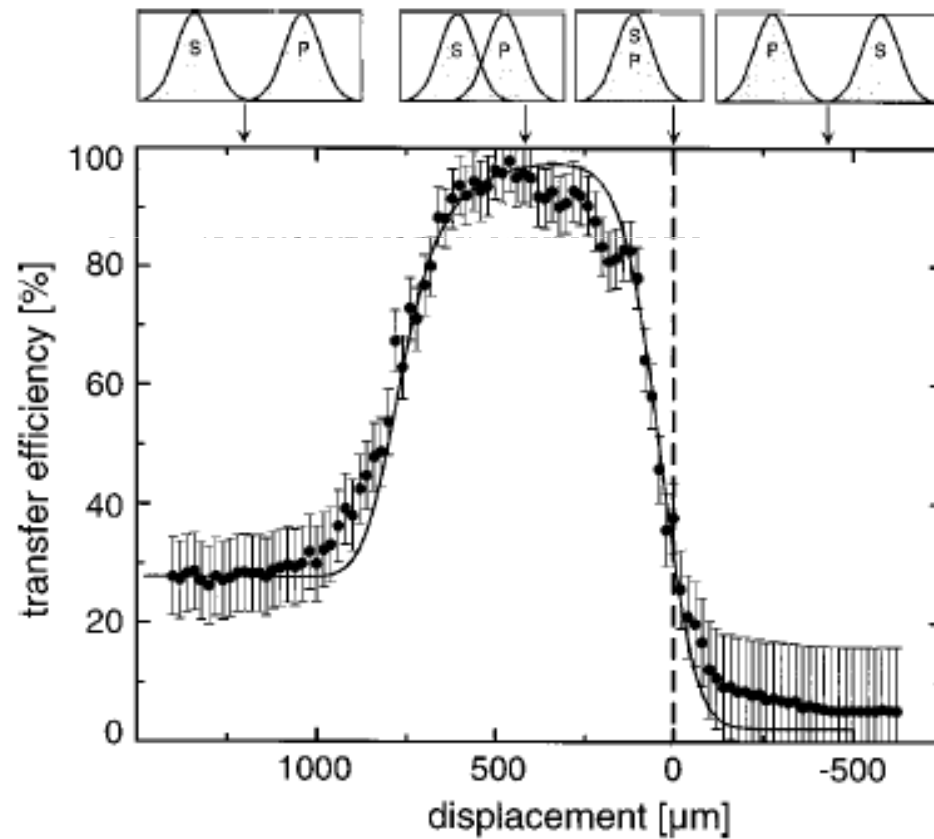
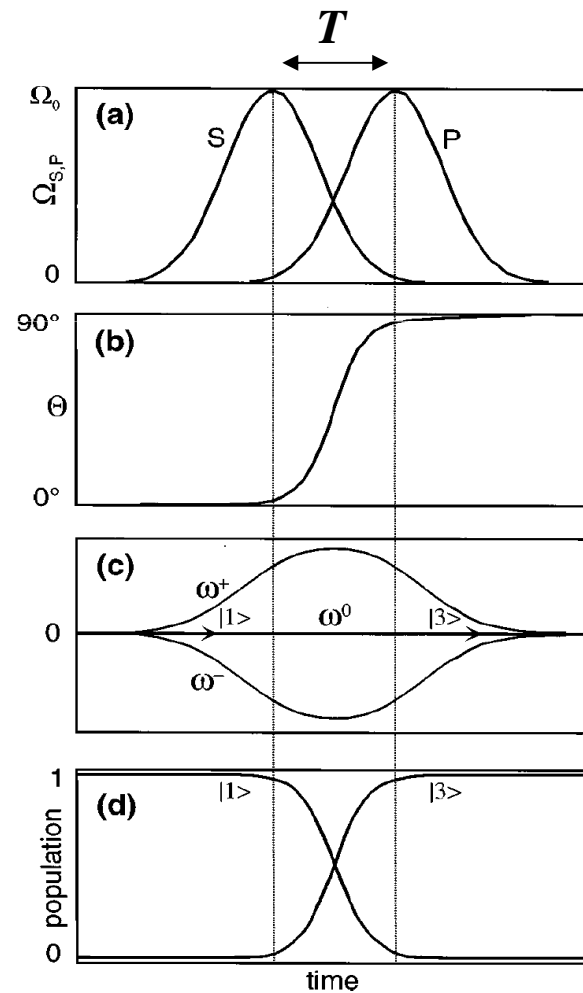
## 2. THREE-LEVEL OPTICAL SYSTEMS (8)

Reviews of Modern Physics, Vol. 70, No. 3, July 1998

### Coherent population transfer among quantum states of atoms and molecules

K. Bergmann, H. Theuer, and B. W. Shore\*

Fachbereich Physik der Universität Kaiserslautern, 67653 Kaiserslautern, Germany

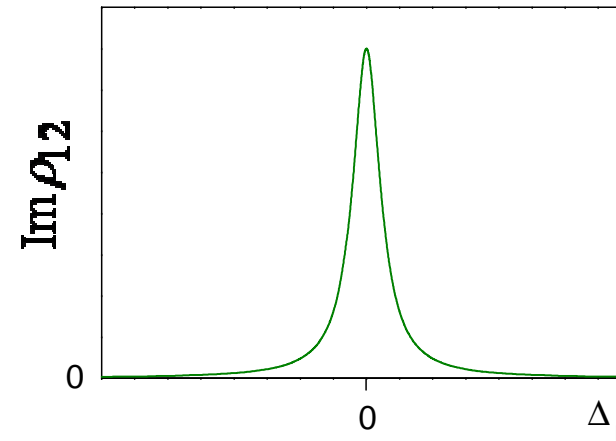
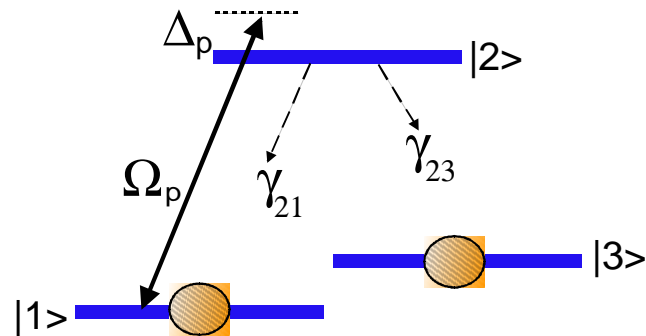




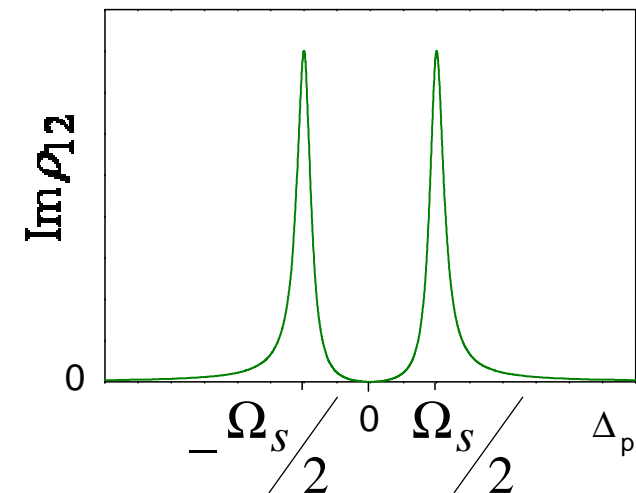
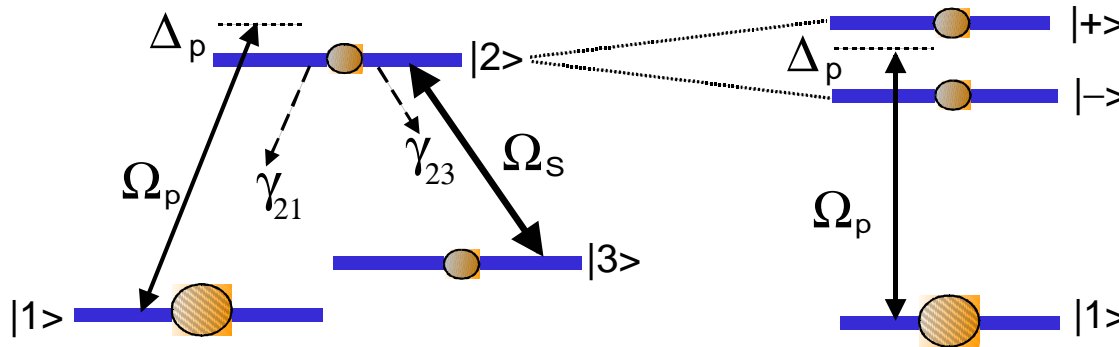
## 2. THREE-LEVEL OPTICAL SYSTEMS (9)

### 2.3 EIT: ELECTROMAGNETICALLY INDUCED TRANSPARENCY

➡ For  $\Omega_s = 0$ , the probe absorption profile is Lorentzian

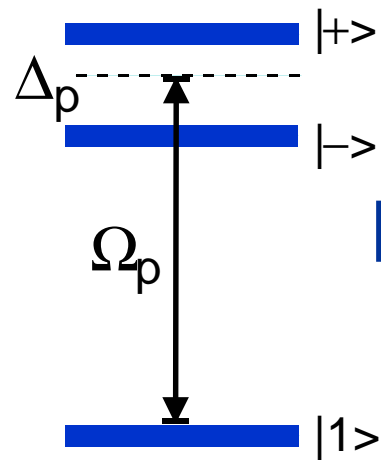


➡ For  $\Omega_s \neq 0$ ,  $\Delta_s = 0$  and  $\Omega_p \ll \Omega_s$



K. J. Boller *et al.*, Phys. Rev. Lett. **66**, 2593 (1991)  
 J. E. Field *et al.*, Phys. Rev. Lett. **67**, 3062 (1991)  
 J. R. Bochler *et al.*, Phys. Rev. A **57**, 1323 (1998)

## 2. THREE-LEVEL OPTICAL SYSTEMS (10)



$$P_{abs} \propto |A_{1-} + A_{1+}|^2 = |A_{1-}|^2 + |A_{1+}|^2 + 2 \operatorname{Re}\{A_{1-} A_{1+}^*\}$$

Interference term due to quantum interference

⇒ Steady-state solution for  $\Omega_p \ll \Omega_s \in \Re$  with  $\Delta_s = 0$

$$\left( \frac{\operatorname{Im} \bar{\rho}_{12}}{\Omega_p} \right)_{\text{steady state}} \equiv K_1 + K_2$$

Two Lorentzian resonances  $\longrightarrow K_1 = (\bar{\rho}_{11} - \bar{\rho}_{22}) \frac{(\Omega_s/2)^2 \Gamma_{13} + (\Delta_p^2 + \Gamma_{13}^2) \Gamma_{12}}{\left( (\Omega_s/2)^2 - \Delta_p^2 + \Gamma_{12} \Gamma_{13} \right)^2 + \Delta_p^2 (\Gamma_{12} + \Gamma_{13})^2}$

Two dispersive resonances = quantum interference contribution  $\longrightarrow K_2 = -\frac{\Omega_s}{2} \operatorname{Im} \bar{\rho}_{23} \frac{(\Omega_s/2)^2 - \Delta_p^2 + \Gamma_{12} \Gamma_{13}}{\left( (\Omega_s/2)^2 - \Delta_p^2 + \Gamma_{12} \Gamma_{13} \right)^2 + \Delta_p^2 (\Gamma_{12} + \Gamma_{13})^2}$

## 2. THREE-LEVEL OPTICAL SYSTEMS (11)

K. J. Boller, A. Imamoglu, S. Harris, Phys. Rev. Lett. **66**, 2593 (1991)

VOLUME 66, NUMBER 20

PHYSICAL REVIEW LETTERS

20 MAY 1991

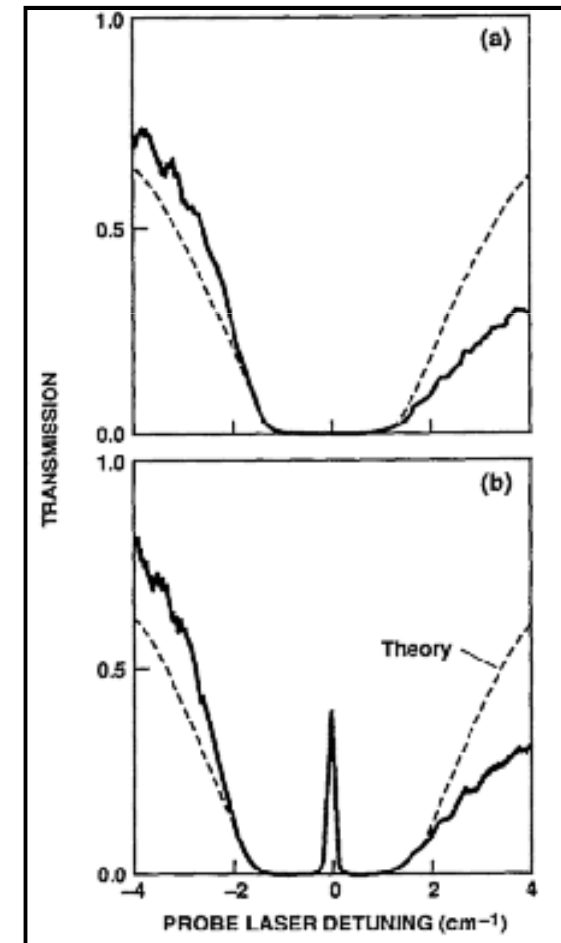
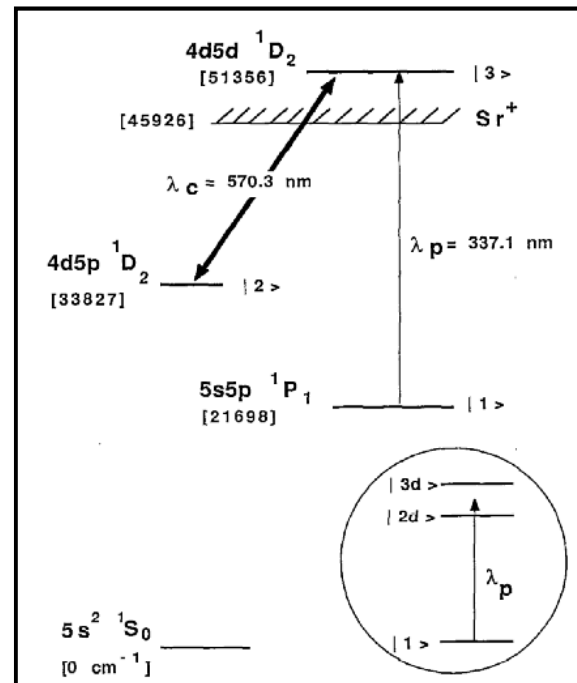
### Observation of Electromagnetically Induced Transparency

K.-J. Boller, A. Imamoglu, and S. E. Harris

*Edward L. Ginzton Laboratory, Stanford University, Stanford, California 94305*

(Received 12 December 1990)

We report the first demonstration of a technique by which an optically thick medium may be rendered transparent. The transparency results from a destructive interference of two dressed states which are created by applying a temporally smooth coupling laser between a bound state of an atom and the upper state of the transition which is to be made transparent. The transmittance of an autoionizing (ultraviolet) transition in Sr is changed from  $\exp(-20)$  without a coupling laser to  $\exp(-1)$  in the presence of a coupling laser.

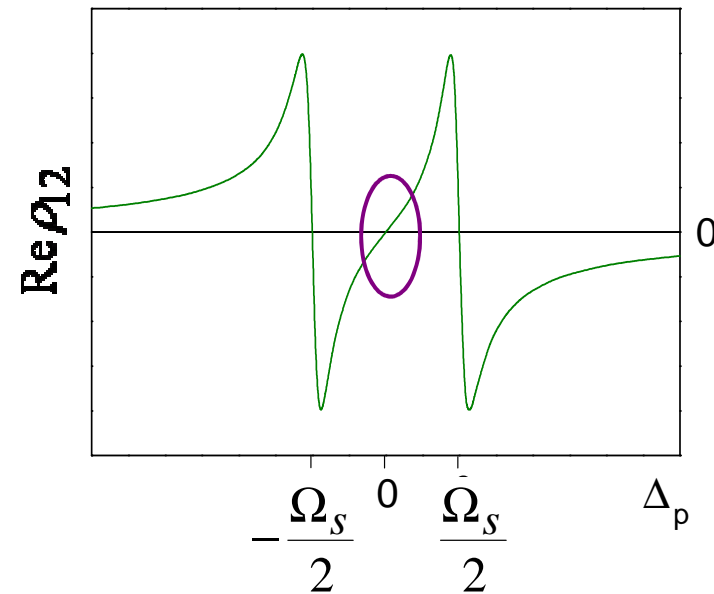
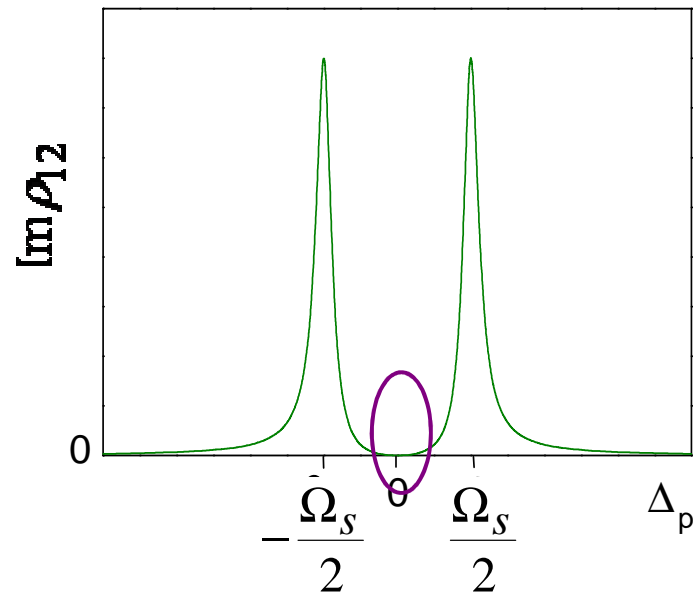


## 2. THREE-LEVEL OPTICAL SYSTEMS (12)

### ➡ Slow light. Reducing group's velocity via EIT

L. H. Hau et al., Nature **397**, 594 (1999).

M. M. Kash et al., Phys. Rev. Lett. **82**, 5229 (1999).



Phase velocity:  $v = c/n$

Group velocity:  $v_g = \frac{c}{n(v) + v \frac{dn}{dv}}$   $\xrightarrow{\frac{dn}{dv} > 0}$   $v_g \ll c$

## 2. THREE-LEVEL OPTICAL SYSTEMS (13)

L. H. Hau *et al.*, Nature 397, 594 (1999).

**letters to nature**

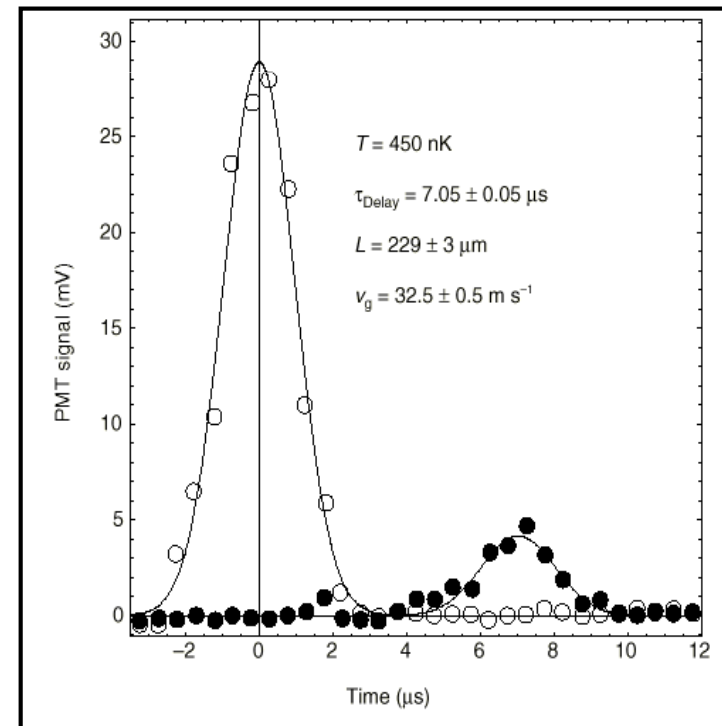
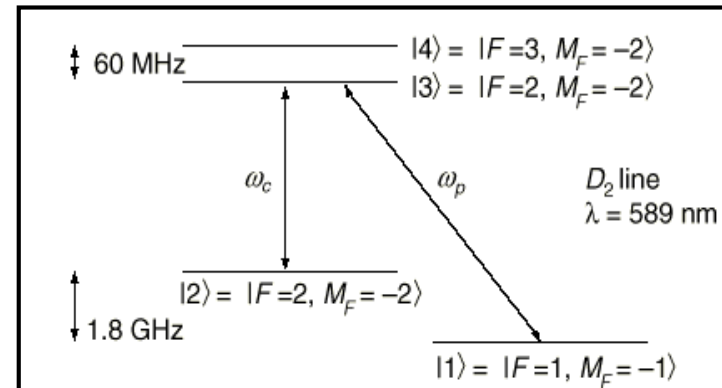
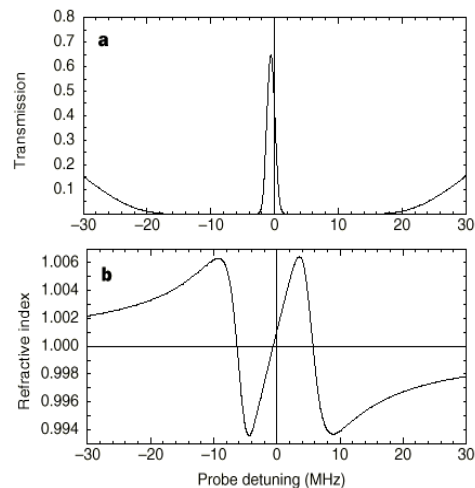
### Light speed reduction to 17 metres per second in an ultracold atomic gas

Lene Vestergaard Hau<sup>†</sup>, S. E. Harris<sup>‡</sup>, Zachary Dutton<sup>††</sup>  
& Cyrus H. Behroozi<sup>§</sup>

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Harvard University, Cambridge, Massachusetts 02138, USA

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USA



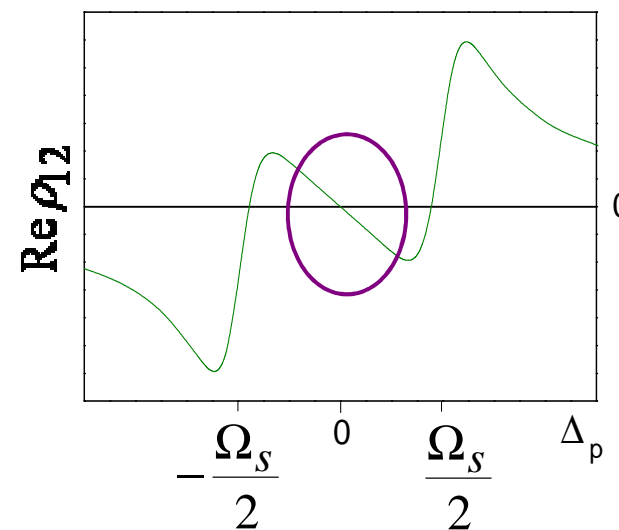
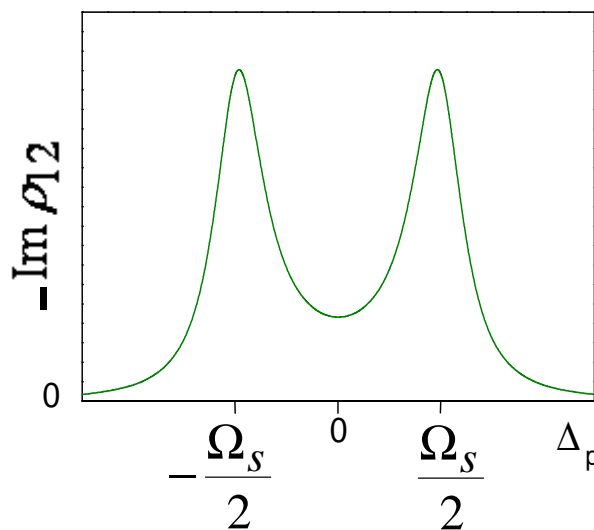
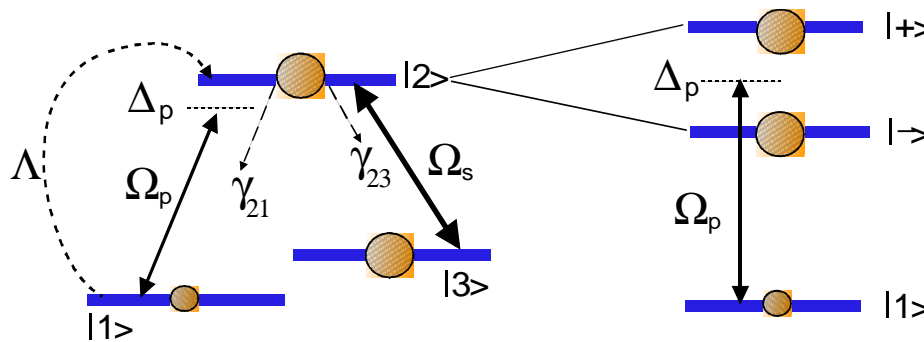
## 2. THREE-LEVEL OPTICAL SYSTEMS (14)

### Superluminal light

$$v_g = \frac{c}{n(\nu) + \nu \frac{dn}{d\nu}}$$

$\frac{dn}{d\nu} < 0$

$v_g \gg c$



D. Mugnai *et al.*, Phys. Rev. Lett. **84**, 4830 (2000).

L. J. Wang *et al.*, Nature **406**, 277 (2000).

microwaves

visible

## 2. THREE-LEVEL OPTICAL SYSTEMS (15)

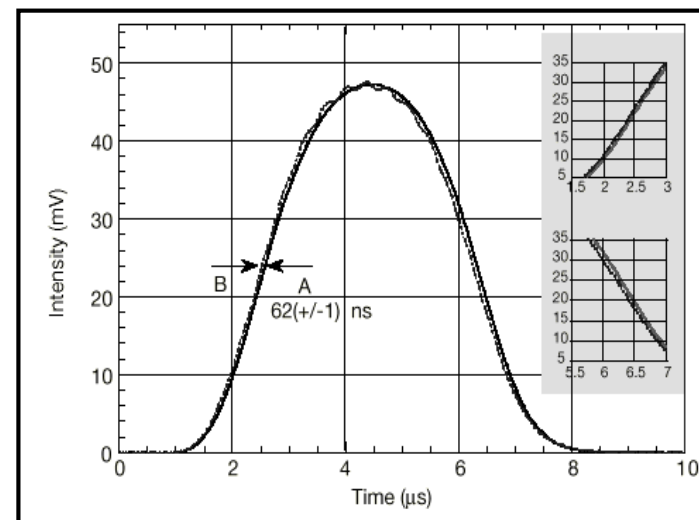
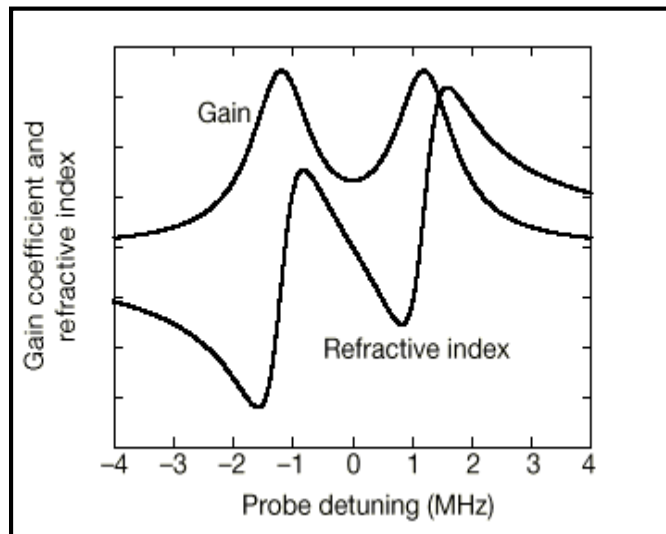
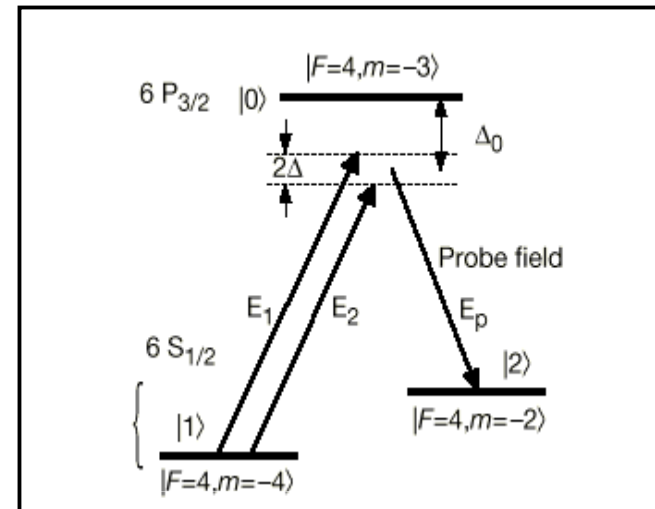
L. J. Wang *et al.*, Nature 406, 277 (2000)

**letters to nature**

### Gain-assisted superluminal light propagation

L. J. Wang, A. Kuzmich & A. Dogariu

NEC Research Institute, 4 Independence Way, Princeton, New Jersey 08540, USA



...other non-linear optics induced by atomic coherences

VOLUME 82, NUMBER 23

PHYSICAL REVIEW LETTERS

7 JUNE 1999

**Nonlinear Optics at Low Light Levels**

S. E. Harris

*Edward L. Ginzton Laboratory, Stanford University, Stanford, California 94305*

Lene Vestergaard Hau

*Rowland Institute for Science, 100 Edwin H. Land Boulevard, Cambridge, Massachusetts 02142  
and Department of Physics, Harvard University, Cambridge, Massachusetts 02138*

(Received 21 December 1998)

We show how the combination of electromagnetically induced transparency based nonlinear optics and cold atom technology, under conditions of ultraslow light propagation, allows nonlinear processes at energies of a few photons per atomic cross section.

VOLUME 84, NUMBER 7

PHYSICAL REVIEW LETTERS

14 FEBRUARY 2000

**Nonlinear Optics and Quantum Entanglement of Ultraslow Single Photons**

M. D. Lukin<sup>1</sup> and A. Imamoglu<sup>2</sup>

<sup>1</sup>*ITAMP, Harvard-Smithsonian Center for Astrophysics, Cambridge, Massachusetts 02138*

<sup>2</sup>*Department of Electrical and Computer Engineering, and Department of Physics, University of California, Santa Barbara, California 93106*

(Received 19 October 1999)

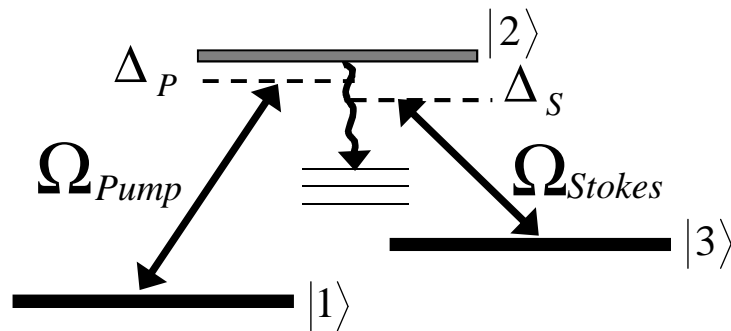
Two light pulses propagating with slow group velocities in a coherently prepared atomic gas exhibit dissipation-free nonlinear coupling of an unprecedented strength. This enables a single-photon pulse to coherently control or manipulate the quantum state of the other. Processes of this kind result in generation of entangled states of radiation field and open up new perspectives for quantum information processing energies of a few photons per atomic cross section.



## 2. THREE-LEVEL OPTICAL SYSTEMS (17)

⇒ EIT from an adiabatic point of view.

Let us assume that the Stokes laser is a continuous wave (cw) laser:



$$\Delta_P = \Delta_S$$

$$|D\rangle = \cos \Theta |1\rangle - \sin \Theta |3\rangle$$

In this case:

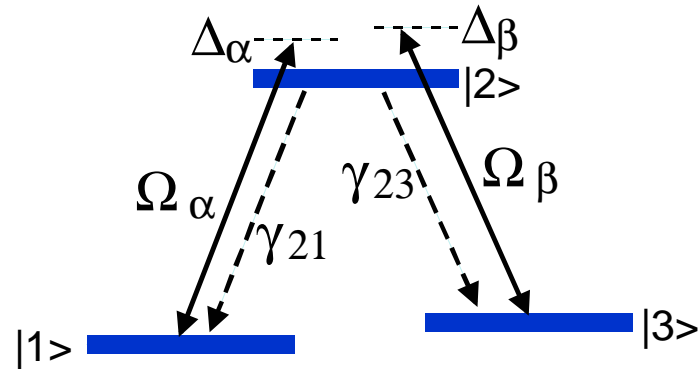
$$\Theta = 0^\circ \rightarrow \Theta = X^\circ \rightarrow \Theta = 0^\circ \quad \longrightarrow \quad |1\rangle \rightarrow a|1\rangle + b|3\rangle \rightarrow |1\rangle$$

$$X^\circ = \tan^{-1} \frac{(\Omega_{Pump})_{MAX}}{\Omega_{Stokes}}$$

The atom starts in state  $|1\rangle$ , interacts with the laser fields and, eventually, it ends up again in state  $|1\rangle$ , without absorbing any photon.

ELECTROMAGNETICALLY INDUCED TRANSPARENCY

## 2.4 CPT: COHERENT POPULATION TRAPPING



Let us assume now:

- $\Omega_\alpha, \Omega_\beta$  are continuous wave
- The initial state of the atom is not known
- $\gamma_{21} = \gamma_{23}$  for simplicity

In the interaction picture, the Hamiltonian of the three-level system is:

$$H_{3L} = \bar{H} - H_{IP} = \frac{\hbar}{2} \begin{pmatrix} 0 & \Omega_\alpha & 0 \\ \Omega_\alpha^* & 2\Delta_\alpha & \Omega_\beta \\ 0 & \Omega_\beta^* & 2(\Delta_\alpha - \Delta_\beta) \end{pmatrix}$$

Let's define the dark and bright states as:

$$|D\rangle \equiv \frac{1}{N} [\Omega_\beta |1\rangle - \Omega_\alpha^* |3\rangle]$$

$$|B\rangle \equiv \frac{1}{N} [\Omega_\alpha |1\rangle + \Omega_\beta^* |3\rangle]$$

$$N \equiv \sqrt{|\Omega_\alpha^2|^2 + |\Omega_\beta^2|^2}$$

$$H_{3L}|D\rangle = -\frac{\hbar}{N} (\Delta_\alpha - \Delta_\beta) \Omega_\alpha^* |3\rangle = 0$$

$$H_{3L}|B\rangle = \frac{\hbar}{2N} (|\Omega_\alpha|^2 + |\Omega_\beta|^2) |2\rangle$$

$$+ \frac{\hbar}{N} (\Delta_\alpha - \Delta_\beta) \Omega_\beta^* |3\rangle$$

$$= \frac{\hbar}{2} \sqrt{|\Omega_\alpha|^2 + |\Omega_\beta|^2} |2\rangle$$

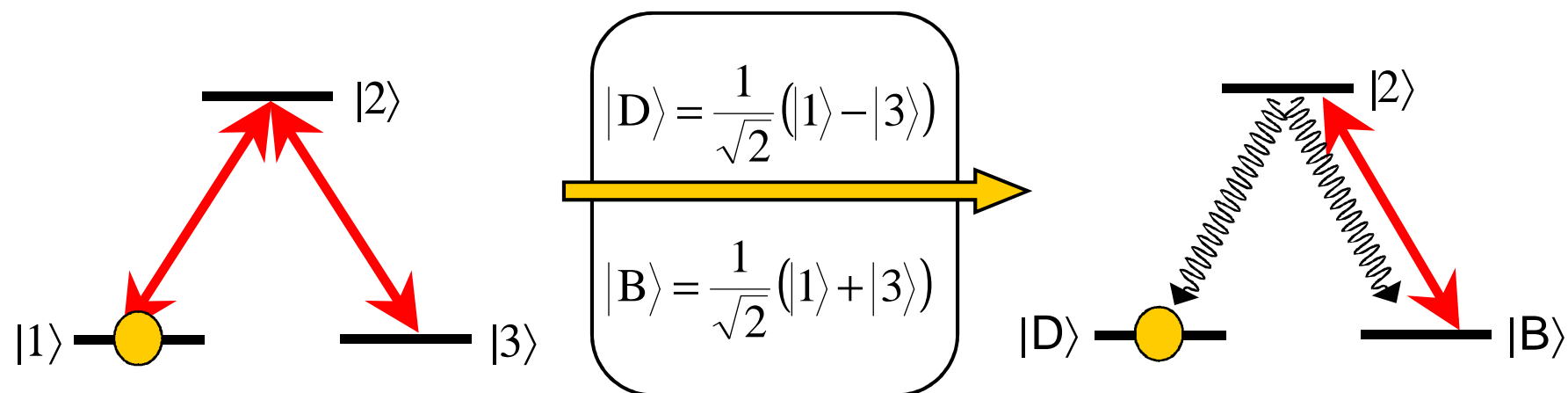
## 2. THREE-LEVEL OPTICAL SYSTEMS (19)

$$\Delta_\alpha = \Delta_\beta$$

$$H_{3L}|D\rangle = -\frac{\hbar}{N}(\Delta_\alpha - \Delta_\beta)\Omega_\alpha^*|3\rangle = 0$$

$$H_{3L}|B\rangle = \frac{\hbar}{2N}(|\Omega_\alpha|^2 + |\Omega_\beta|^2)|2\rangle + \frac{\hbar}{N}(\Delta_\alpha - \Delta_\beta)\Omega_\beta^*|3\rangle = \frac{\hbar}{2}\sqrt{|\Omega_\alpha|^2 + |\Omega_\beta|^2}|2\rangle$$

⇒ Let us assume, for simplicity:  $\Omega_\alpha = \Omega_\beta \in \Re$ ;  $\Delta_\alpha = \Delta_\beta$ ;  $\gamma_{21} = \gamma_{23}$



⇒ After several cycles of absorption and spontaneous emission, the atom is eventually trapped in the dark state

## 2. THREE-LEVEL OPTICAL SYSTEMS (20)

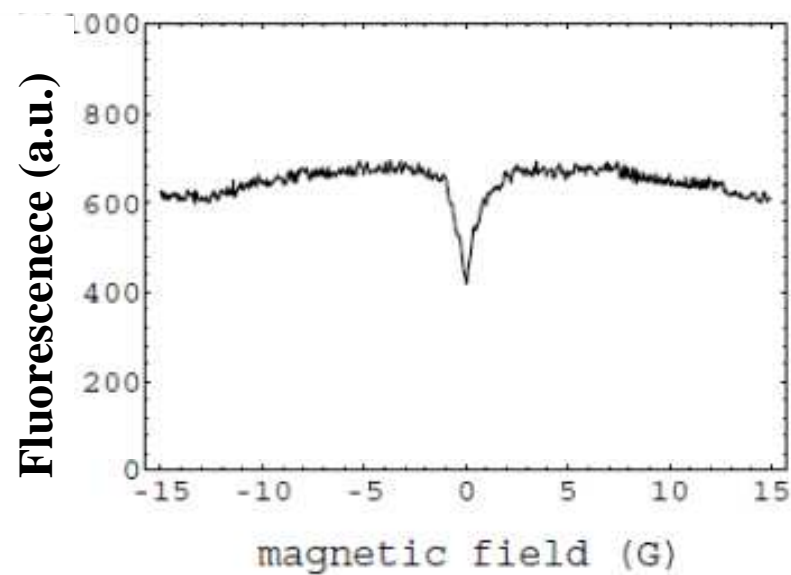
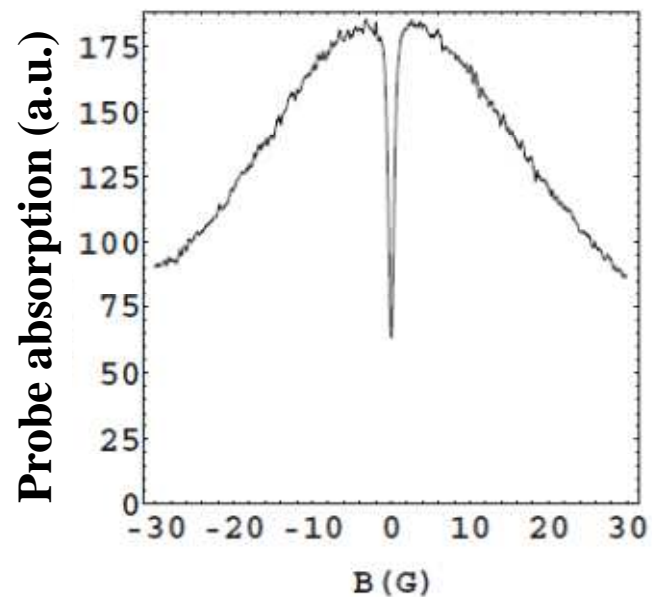
G. Alzetta, A. Gozzini, L. Moi and G. Orriols, *Nuovo Cimento B* **36** (1976) 5.

E. Arimondo, and G. Orriols, *Nuovo Cimento Lett.* **17** (1976) 333.

G. Orriols, *Nuovo Cimento B* **53** (1979) 1.

E. Arimondo, Coherent population trapping in laser spectroscopy, *Progress in Optics*, vol **35**, ed. E. Wolf (Amsterdam: Elsevier) 1996.

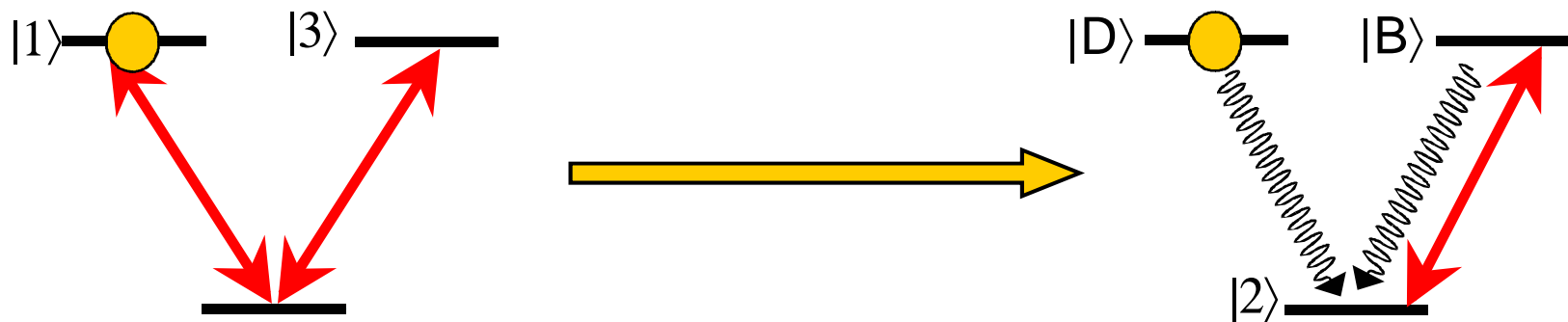
F. Renzoni, W. Maichen, L. Windholz, and E. Arimondo, *Phys. Rev. A* **55**, 3710 (1997)



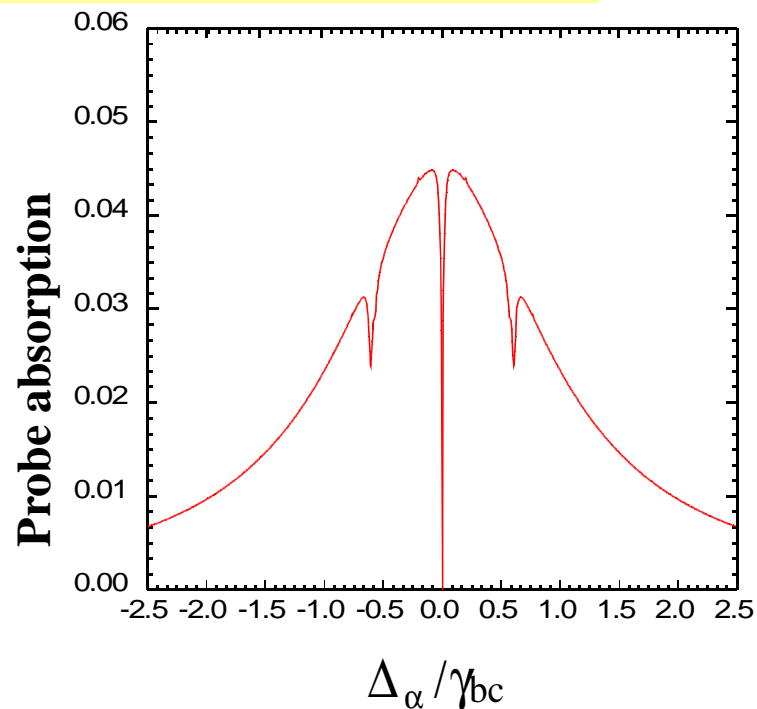
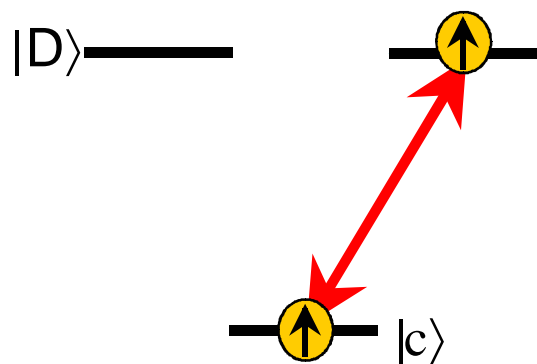
Coherent population trapping on the  $D_1$  line of a thermal sodium beam

## 2. THREE-LEVEL OPTICAL SYSTEMS (21)

⇒ In the V-scheme, there is no CPT due to spontaneous emission.

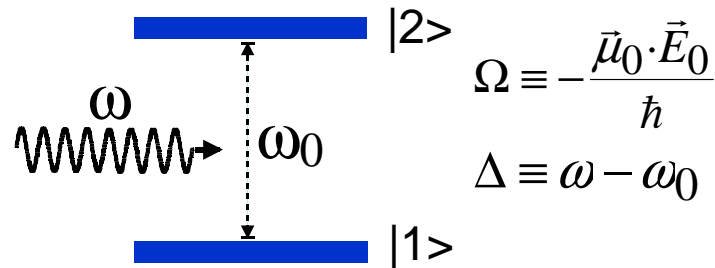


Coherent population trapping in two-electron three-level systems with aligned spins  
 J. Mompert, R. Corbalán, L. Roso, Phys. Rev. Lett. **88**, 023603 (2002).



## 2.5 RAP: RAPID ADIABATIC PASSAGE, REVISITED

N. V. Vitanov and B. W. Shore. Stimulated Raman adiabatic passage in a two-state system.  
 Phys. Rev. A **73**, 053402 (2006)



$$|\psi(t)\rangle = a_1(t)e^{-i\omega_1 t}|1\rangle + a_2(t)e^{-i(\omega_1+\omega)t}|2\rangle$$

$$i \begin{pmatrix} \dot{a}_1 \\ \dot{a}_2 \end{pmatrix} = \begin{pmatrix} 0 & -\Omega/2 \\ -\Omega/2 & -\Delta \end{pmatrix} \begin{pmatrix} a_1 \\ a_2 \end{pmatrix}$$

We define new variables:  $u = 2 \operatorname{Re}\{a_1 a_2^*\} = 2 \operatorname{Re} \rho_{12}$

$$u^2 + v^2 + w^2 = 1$$

$$v = 2 \operatorname{Im}\{a_1 a_2^*\} = 2 \operatorname{Im} \rho_{12}$$

$$w = |a_2|^2 - |a_1|^2 = \rho_{22} - \rho_{11}$$

Following:

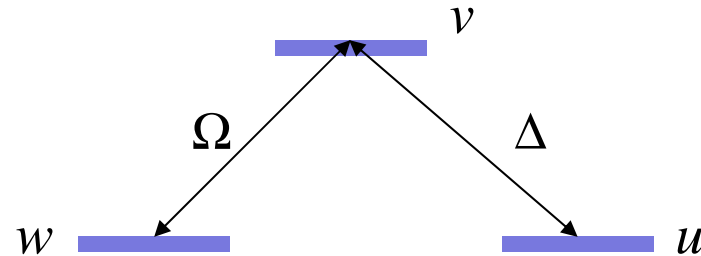
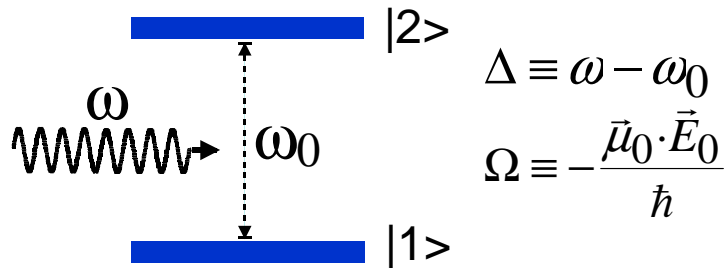
There is one eigenvector with null eigenvalue:

$$\frac{d}{dt} \begin{pmatrix} u \\ v \\ w \end{pmatrix} = \begin{pmatrix} 0 & -\Delta & 0 \\ \Delta & 0 & -\Omega \\ 0 & \Omega & 0 \end{pmatrix} \begin{pmatrix} u \\ v \\ w \end{pmatrix}$$

$$d(\theta) = w \cos \vartheta - u \sin \theta = 0$$

$$\text{with } \tan \theta = \frac{\Omega}{\Delta}$$

2.5 RAP: RAPID ADIABATIC PASSAGE, REVISITED



$$u = 2 \operatorname{Re}\{a_1 a_2^*\} = 2 \operatorname{Re} \rho_{12}$$

$$v = 2 \operatorname{Im}\{a_1 a_2^*\} = 2 \operatorname{Im} \rho_{12}$$

$$w = |a_1|^2 - |a_2|^2 = \rho_{22} - \rho_{11}$$

$$u^2 + v^2 + w^2 = 1$$

$$\frac{d}{dt} \begin{pmatrix} u \\ v \\ w \end{pmatrix} = \begin{pmatrix} 0 & -\Delta & 0 \\ \Delta & 0 & -\Omega \\ 0 & \Omega & 0 \end{pmatrix} \begin{pmatrix} u \\ v \\ w \end{pmatrix}$$

$$d(\theta) = w \cos \vartheta - u \sin \theta = 0 \quad \text{with} \quad \tan \theta = \frac{\Omega}{\Delta}$$

RAP, revisited:

The atom is initially in the ground state with:

$$\Delta > 0; |\Delta| \gg \Omega \Rightarrow \theta(t_0) = 0$$

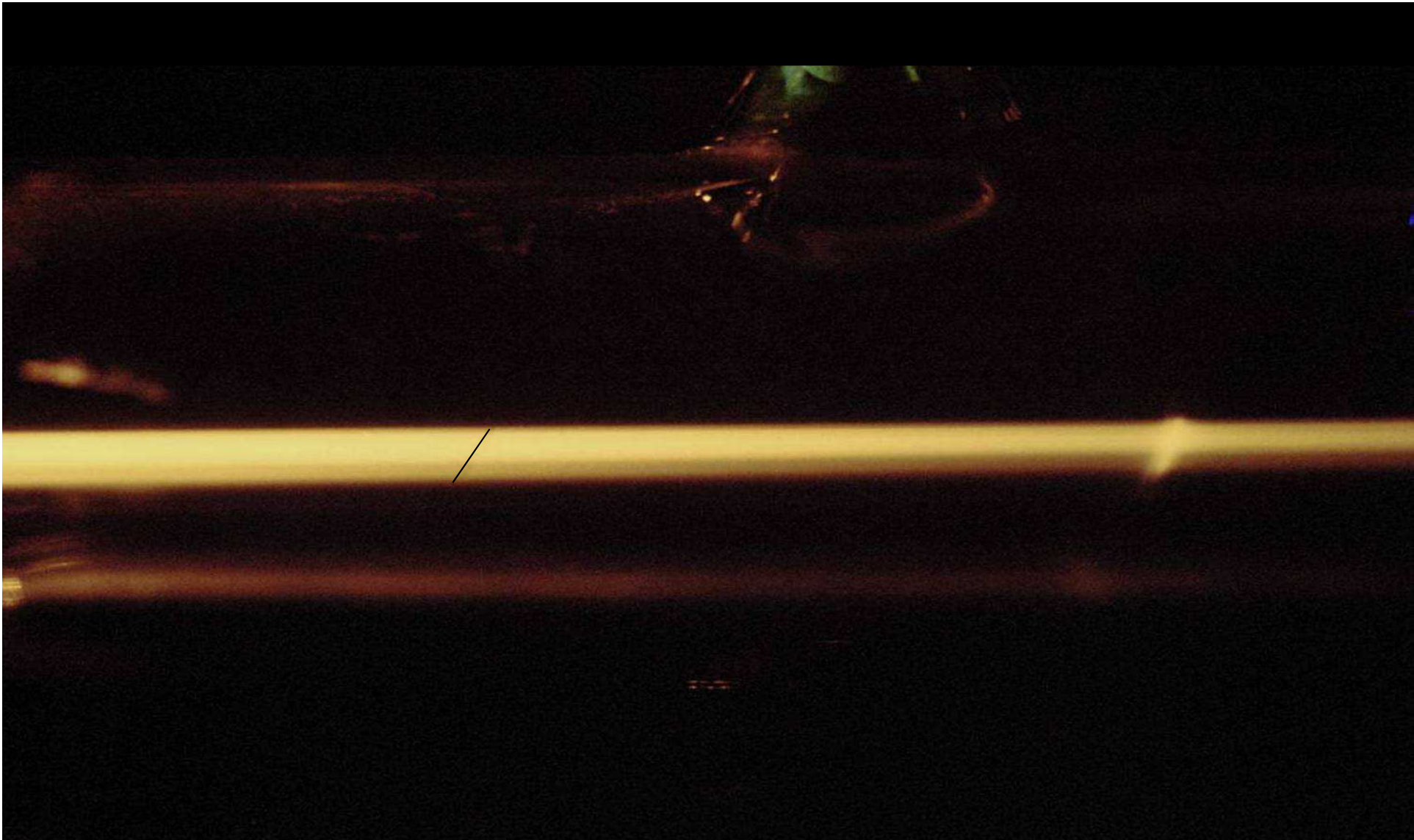
$$w = -1, u = v = 0 \Rightarrow d(t_0) = 0$$

$$\text{At the end: } \Delta < 0; |\Delta| \gg \Omega \Rightarrow \theta(t_f) = \pi$$

$$\text{As: } d(t) = 0 \quad \forall t$$

Then, at the end:

$$w = 1, u = v = 0 \Rightarrow \rho_{22}(t_f) = 1$$



**3** LA  
**'RIGA NERA'**



# MAIN ARTICLES

## FIRST EXPERIMENT

G. Alzetta, A. Gozzini, L. Moi and G. Orriols, *Nuovo Cimento B* 36 (1976) 5.

## FIRST THEORY

E. Arimondo, and G. Orriols, *Nuovo Cimento Lett.* 17 (1976) 333.

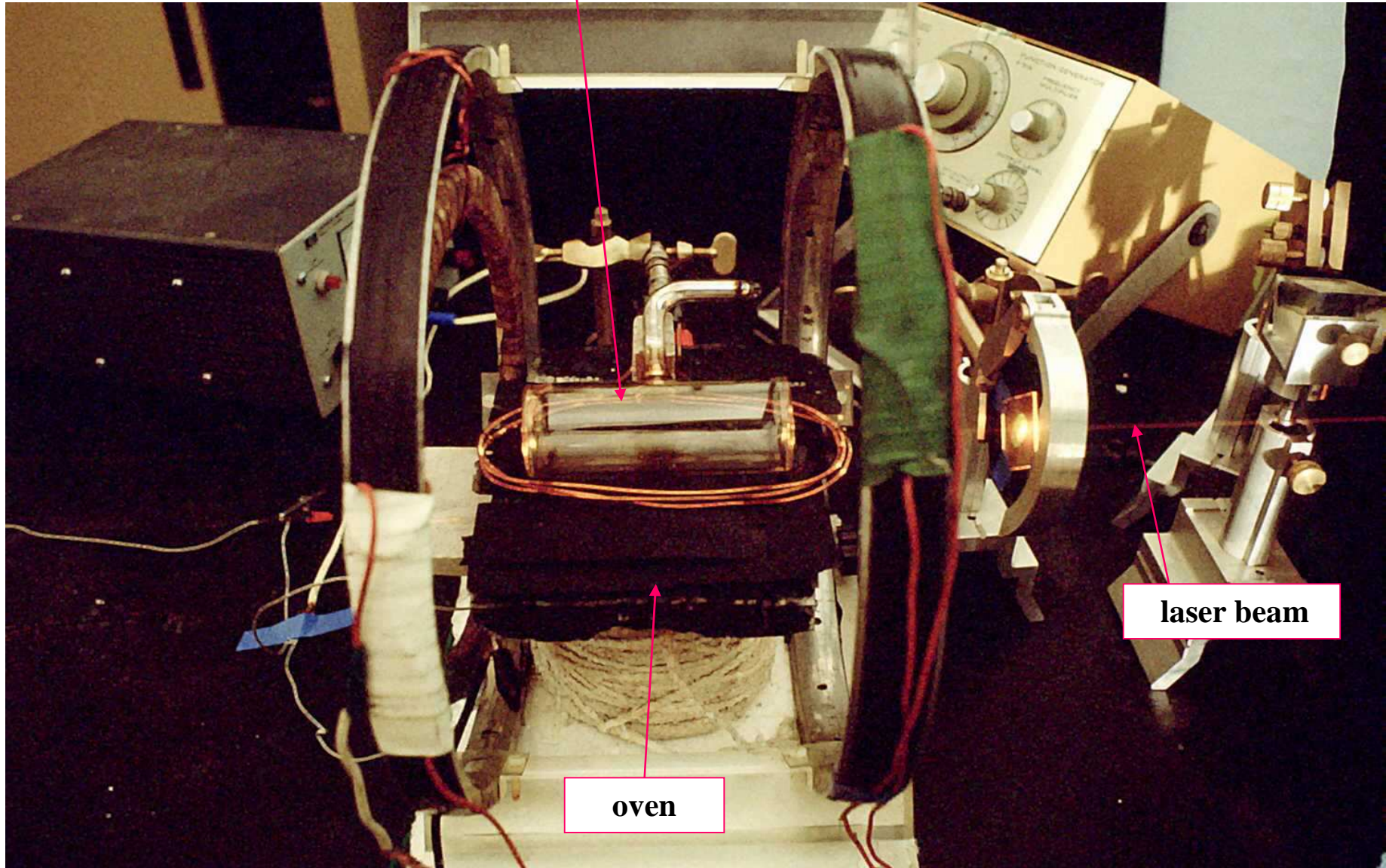
G. Orriols, *Nuovo Cimento B* 53 (1979) 1.

## MAIN REVIEW ARTICLE

E. Arimondo, Coherent population trapping in laser spectroscopy, *Progress in Optics*, vol 35, ed. E. Wolf (Amsterdam: Elseveier) 1996.

## Experiments with a sodium vapor cell

Na vapor cell



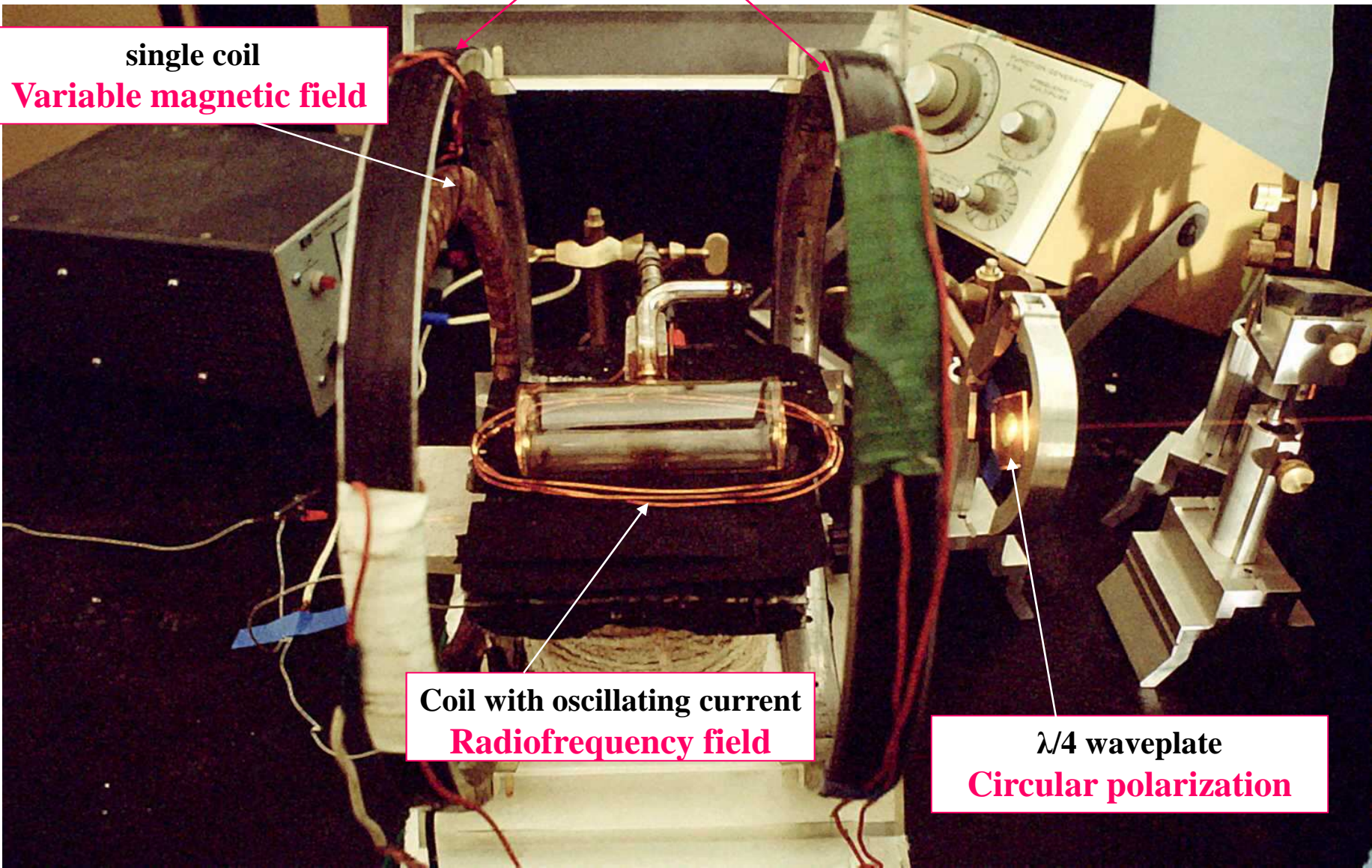


**Hemholtz coils**  
**Uniform magnetic field**

**single coil**  
**Variable magnetic field**

**Coil with oscillating current**  
**Radiofrequency field**

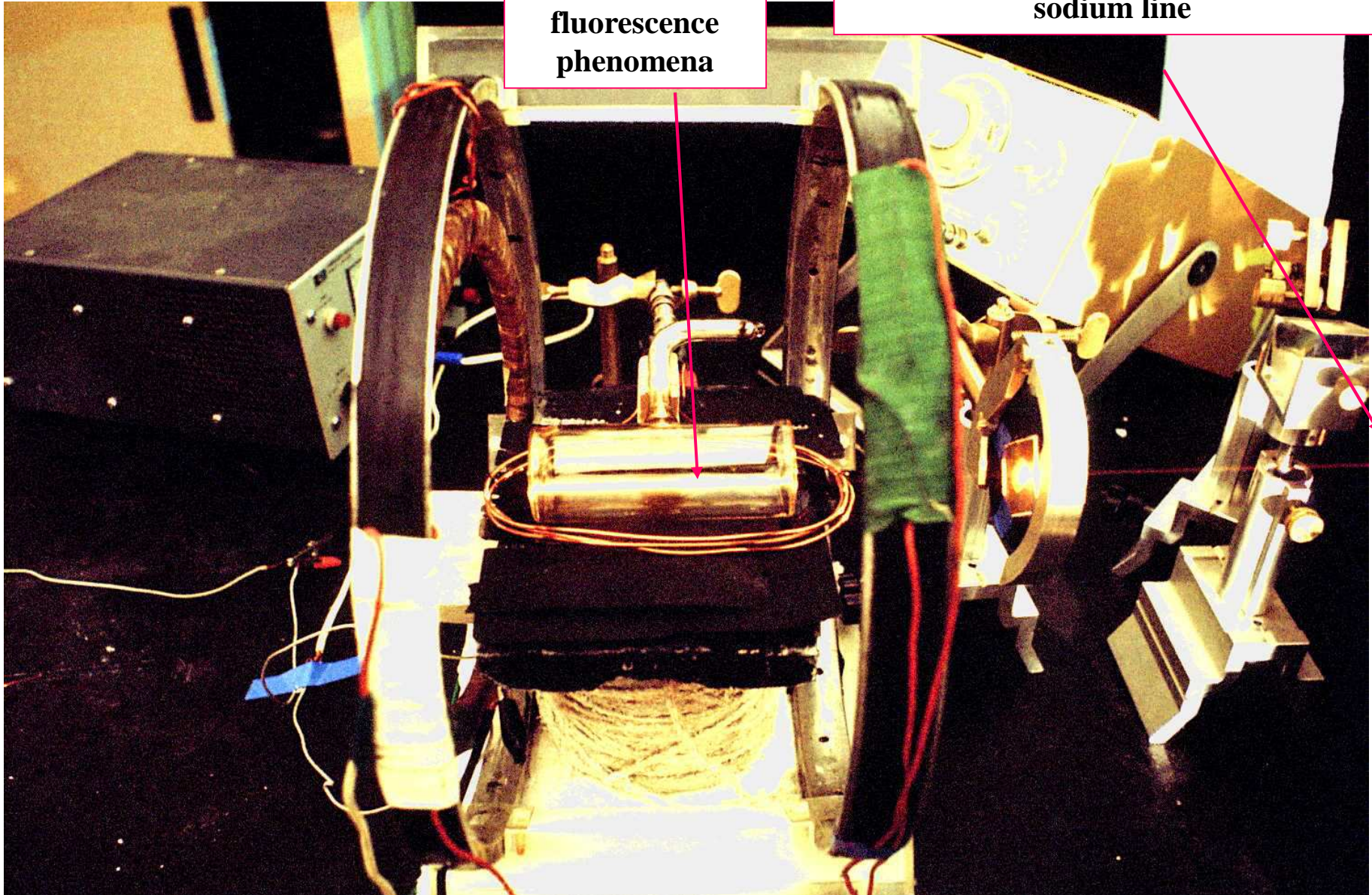
**$\lambda/4$  waveplate**  
**Circular polarization**



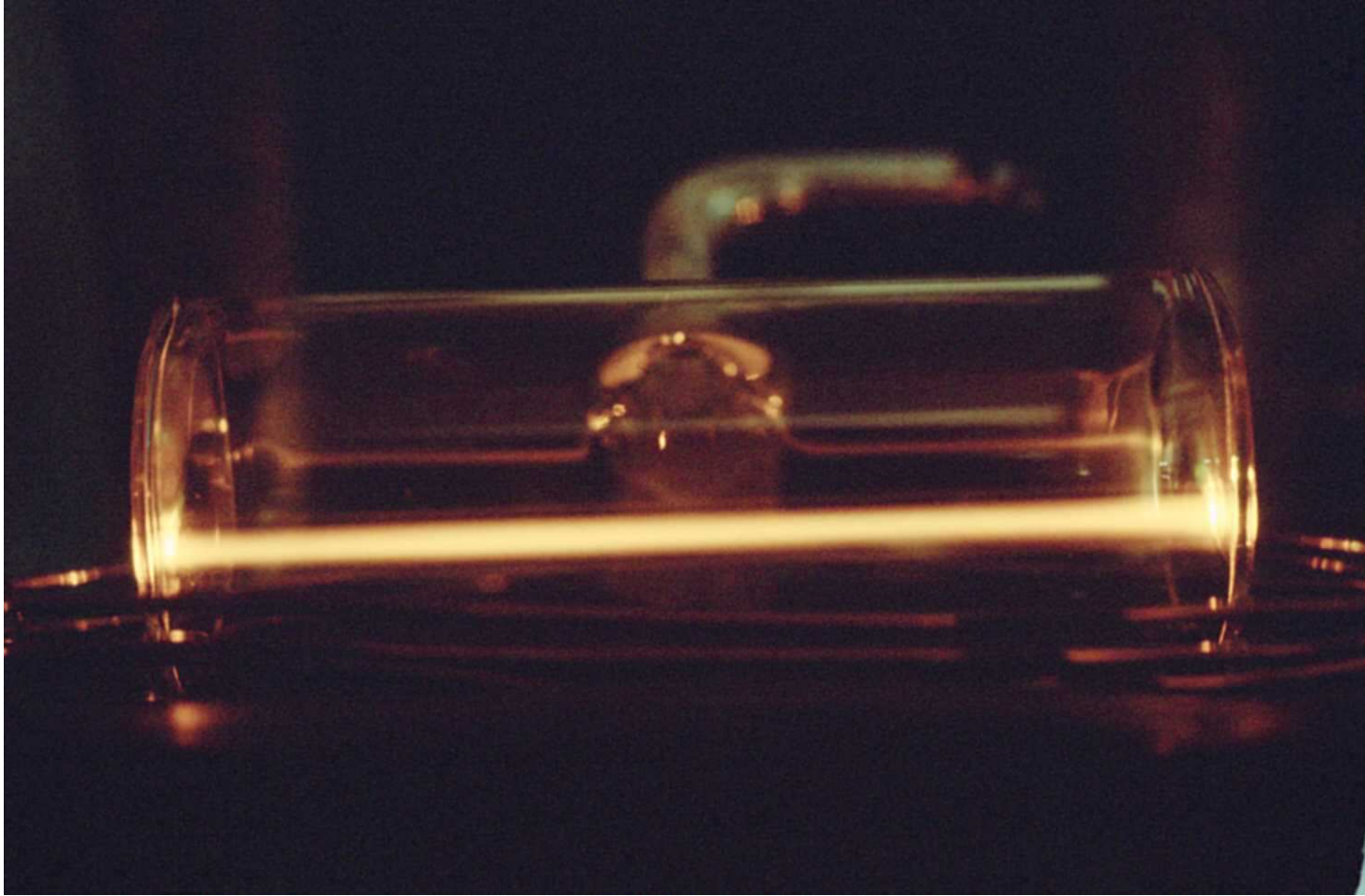


**resonant  
fluorescence  
phenomena**

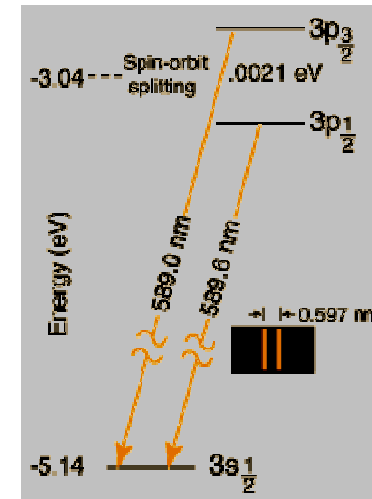
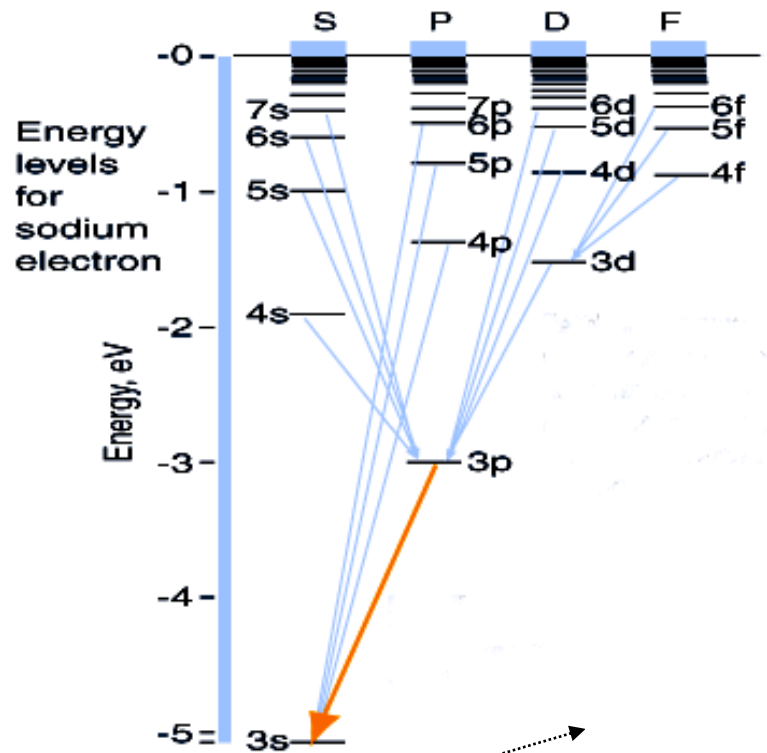
**Tuning the laser wavelength to the  $D_1$   
sodium line**



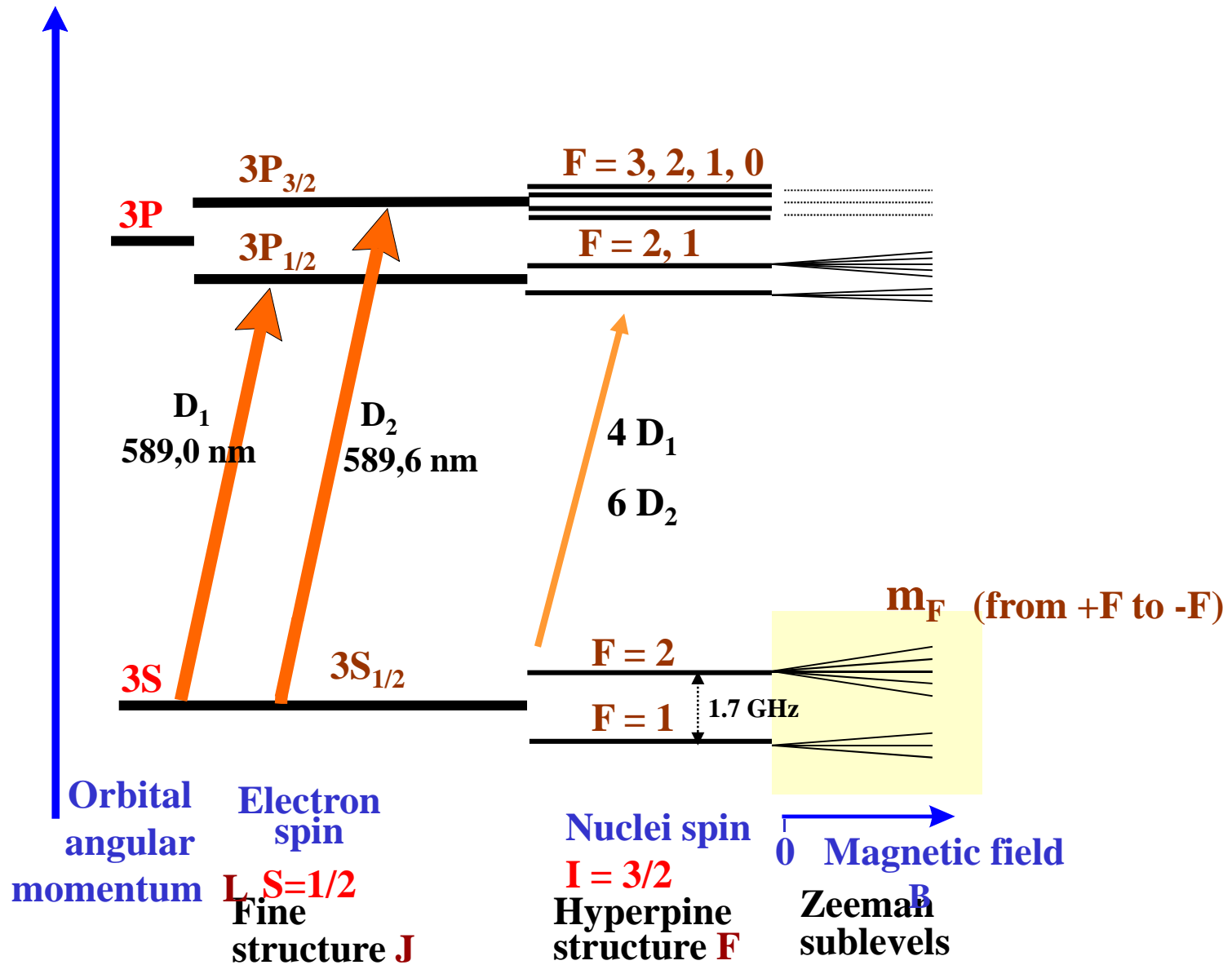




# Sodium atom

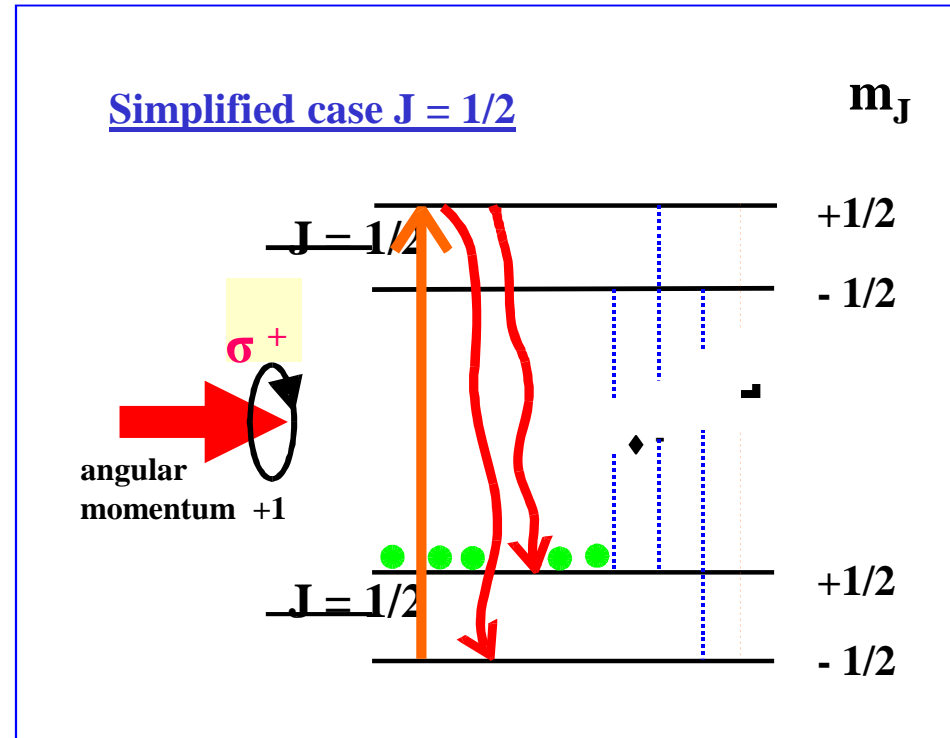
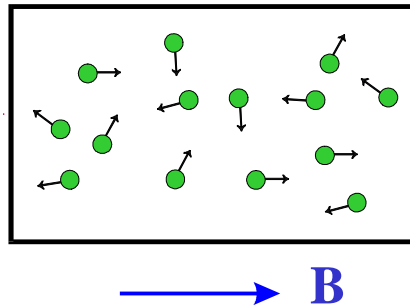


# Energy levels of the Na electron (ground and first excited)



# Orientation of an atomic vapor by optical pumping

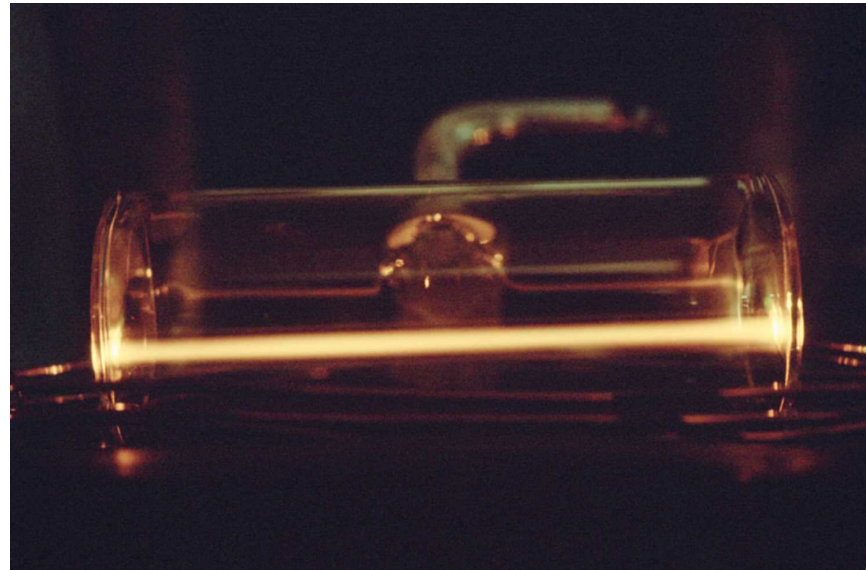
## Orientation of the atomic angular momenta



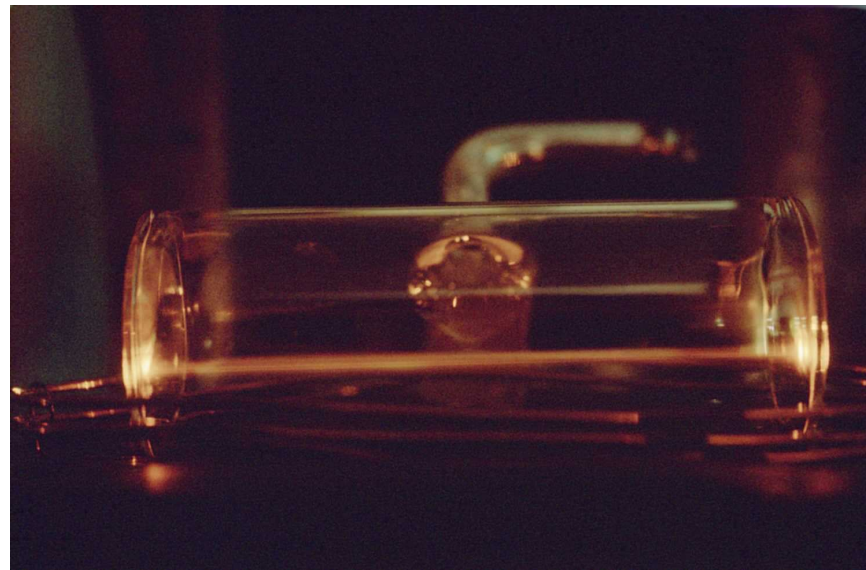
- conservation of angular momentum  $\rightarrow$  selective excitation
- spontaneous emission to all states
- atoms accumulate in a particular Zeeman sublevel that corresponds to an orientation of the angular momentum
- atoms do not absorb light and, eventually, do not produce fluorescence



**Linearly polarized  
laser beam tuned to  
the sodium D<sub>1</sub> line**

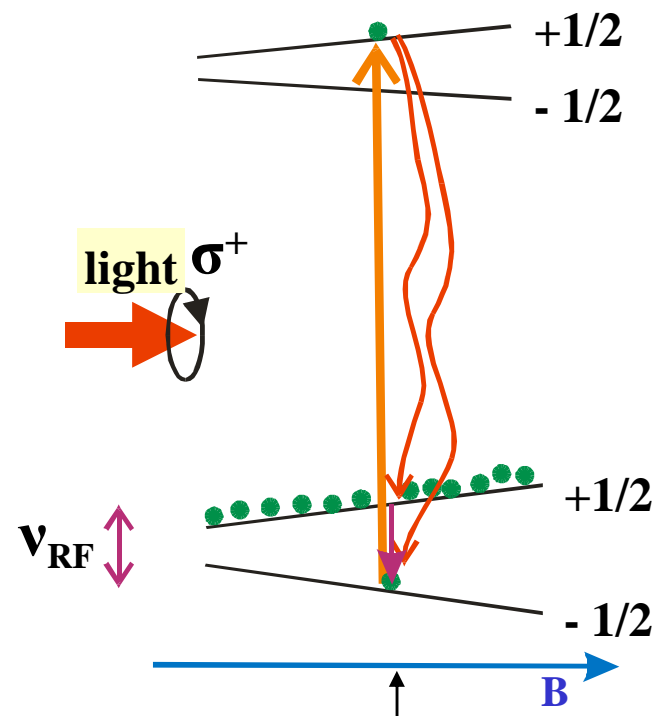
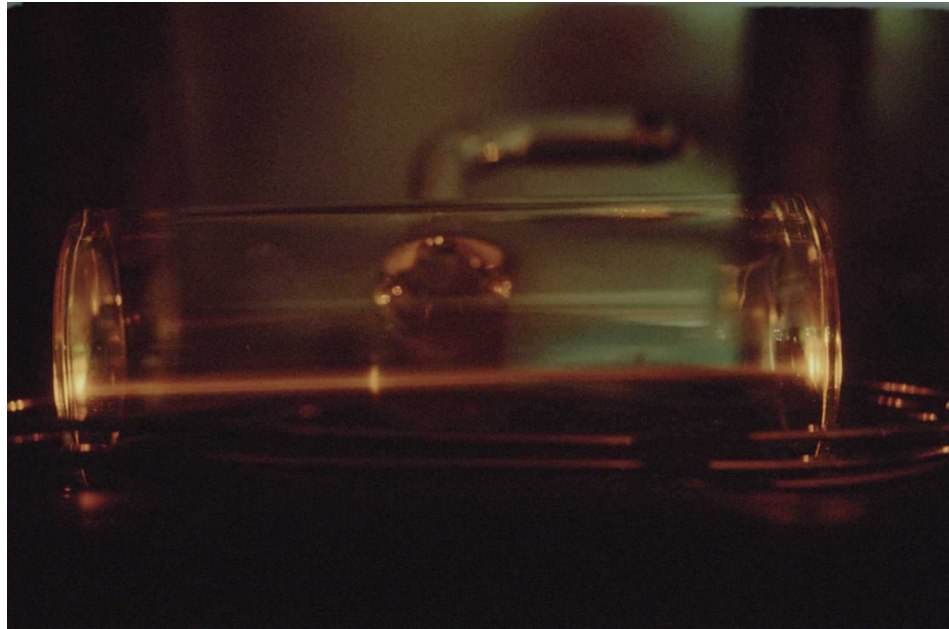


**Circularly polarized  
beam (by means of a  
 $\lambda/4$  waveplate)**



## Magnetic resonance induced by the radiofrequency field





**Resonance condition**

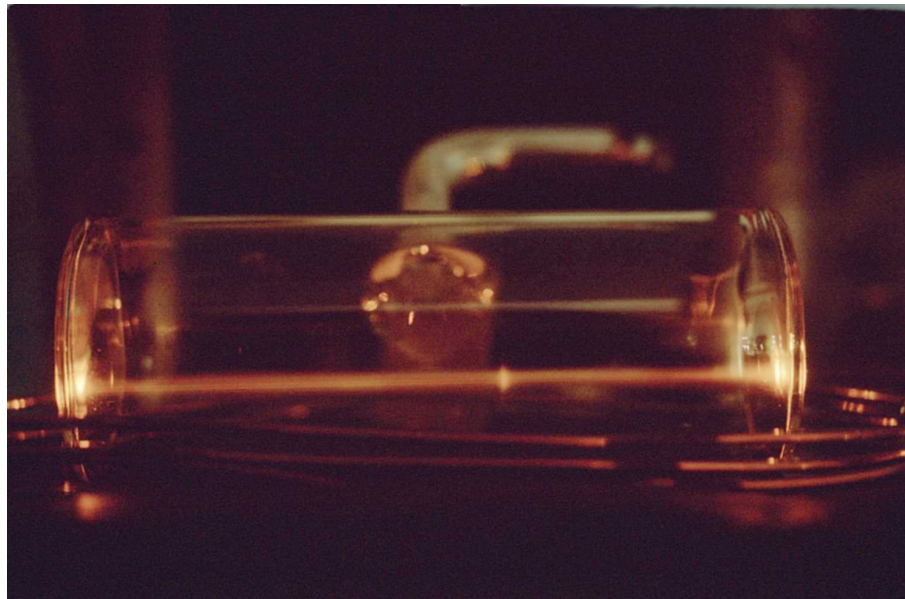
$$v_{\text{RF}} = v_{\text{atom}} = (E_{+1/2} - E_{-1/2})/h$$

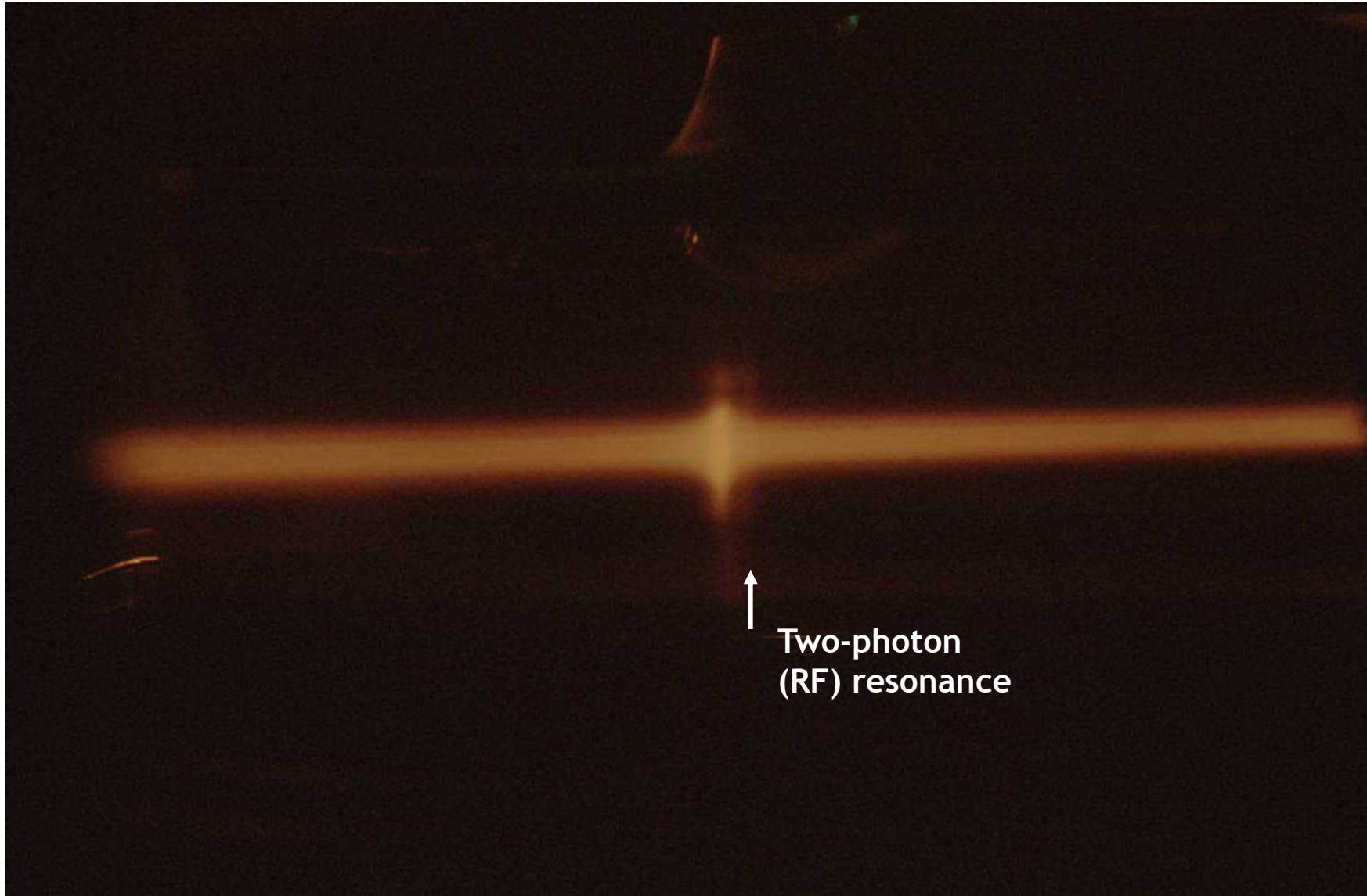


**Modifying the frequency**

**or**

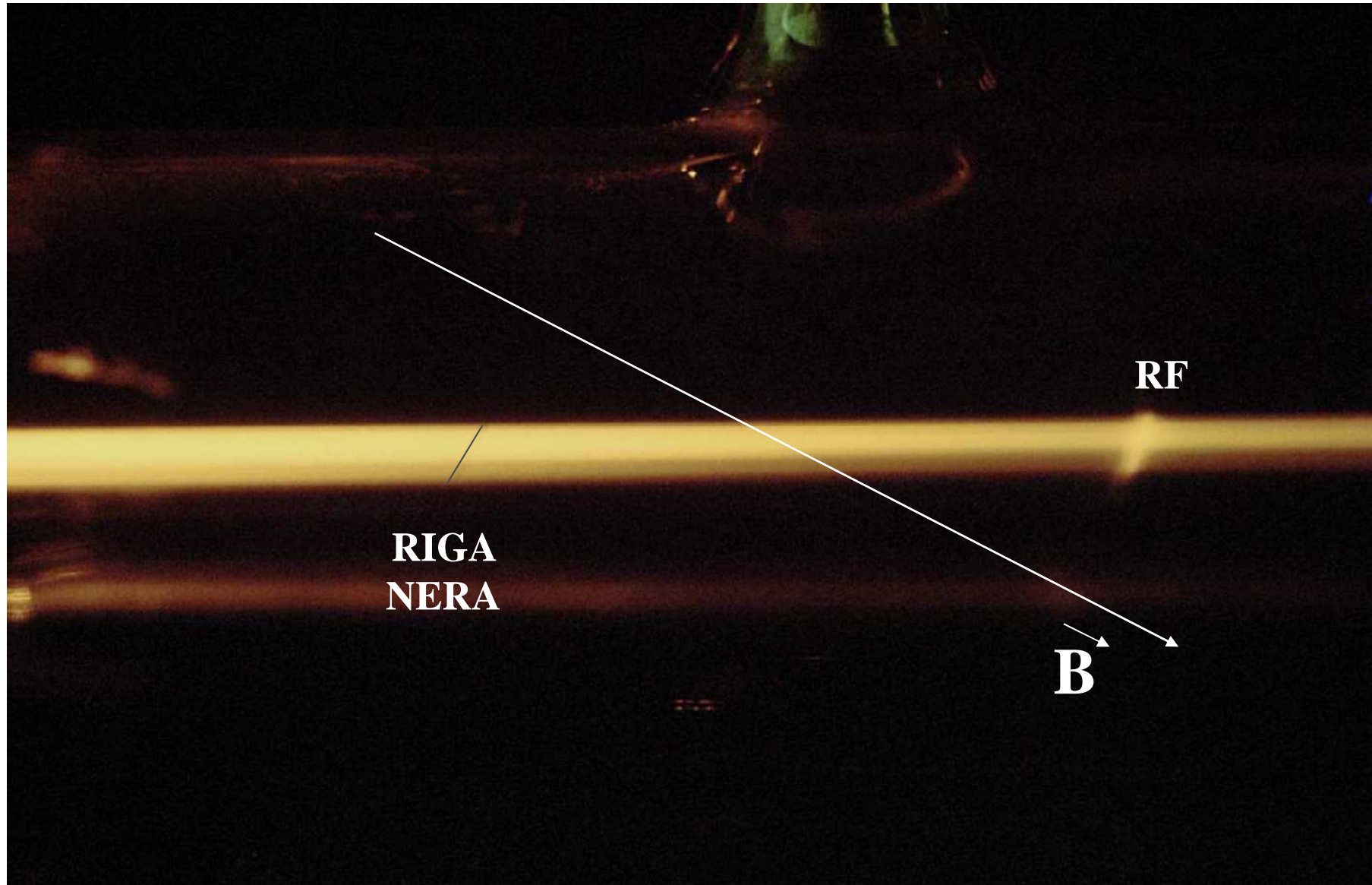
**Modifying the magnetic field**





Two-photon  
(RF) resonance

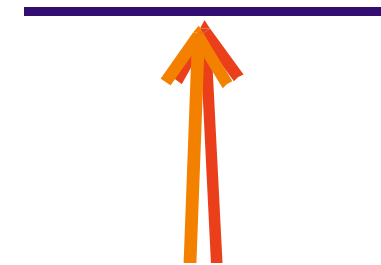
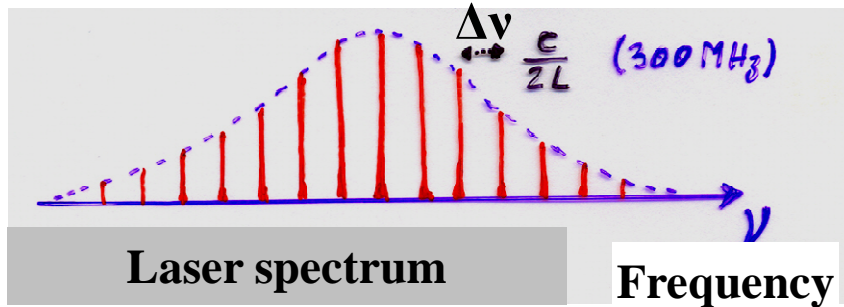
## Laser induced non-absorbing resonance



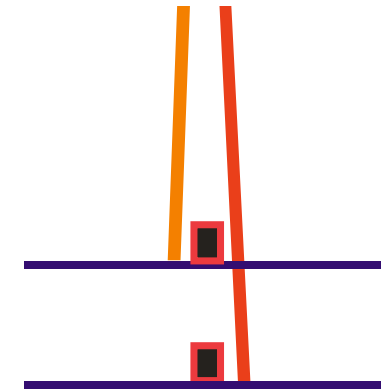




At the “Riga Nera”, there is a resonance between the  $\Delta\nu$  hyperfine splitting and the frequency of two consecutive light modes



Destructive interference between the two absorbing pathways



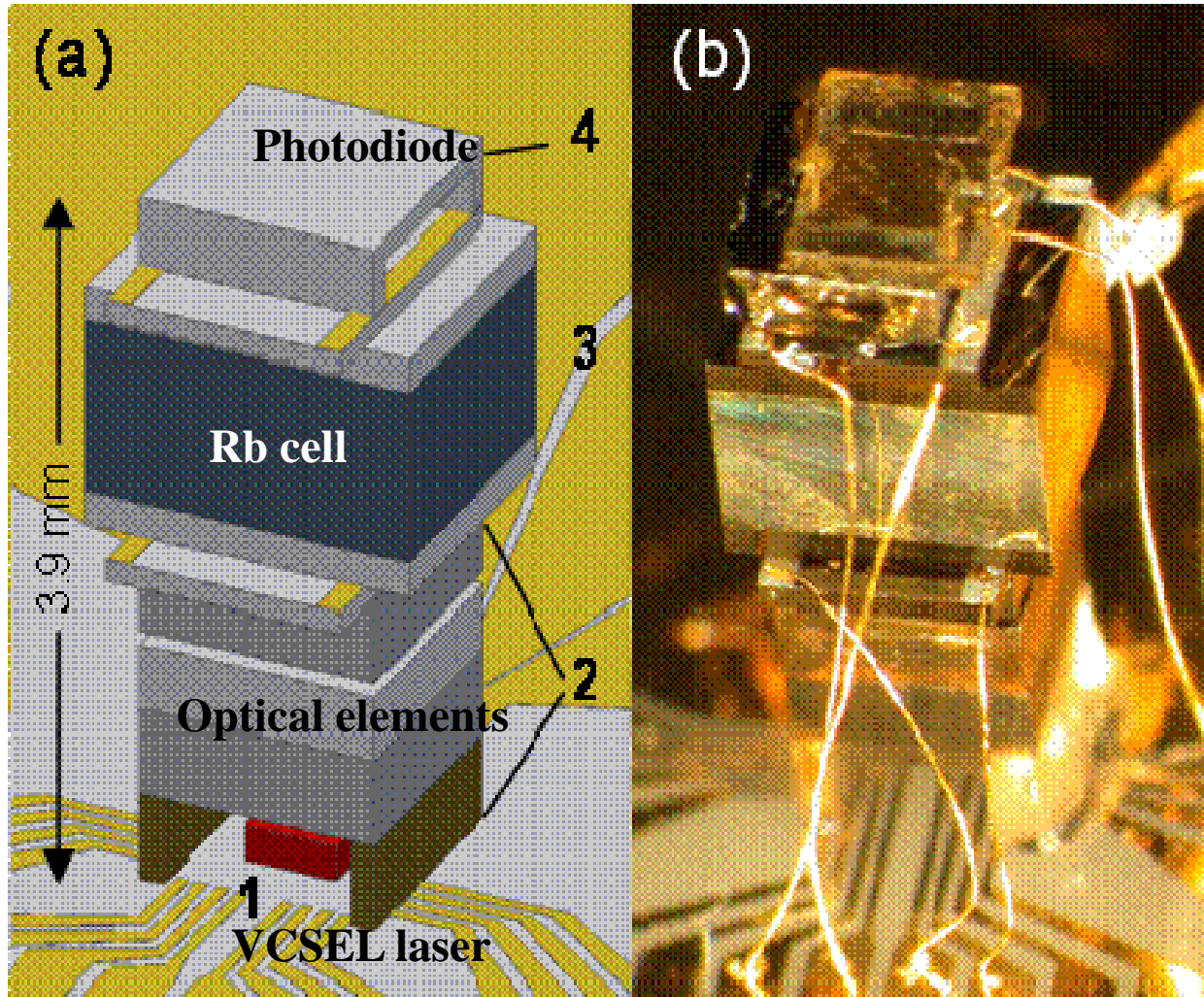
**Dark state = non absorbing superposition**

## Frequency standards and atomic clocks based on the dark line





## Micromagnetometer and atomic clocks based on the D1 line



NIST,  
Boulder